

# Introduction to formal models of argumentation



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# What is argumentation?

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- Giving reasons to support claims that are open to doubt
- Defending these claims against attack
- NB: Inference + dialogue





# Why study argumentation?

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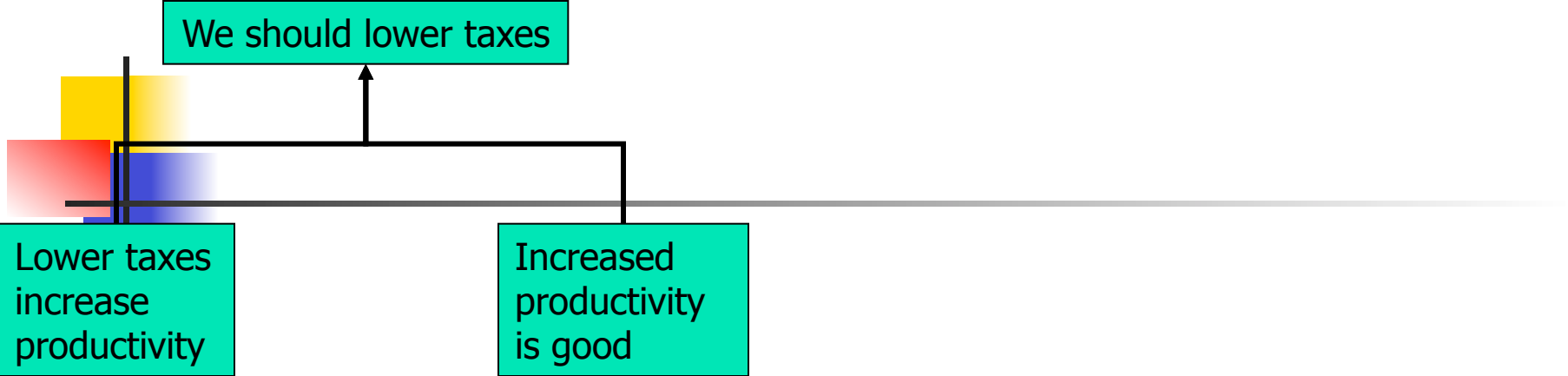
- In **linguistics**:
  - Argumentation is a form of **language use**
- In **Artificial Intelligence**:
  - Our applications have **humans** in the loop
    - We want to model **rational reasoning** but with standards of rationality that are **attainable** by humans
    - Argumentation is natural for humans
  - **Trade-off** between rationality and naturalness
- In **Multi-Agent Systems**:
  - Argumentation is a form of **communication**



# Today: **formal** models of argumentation

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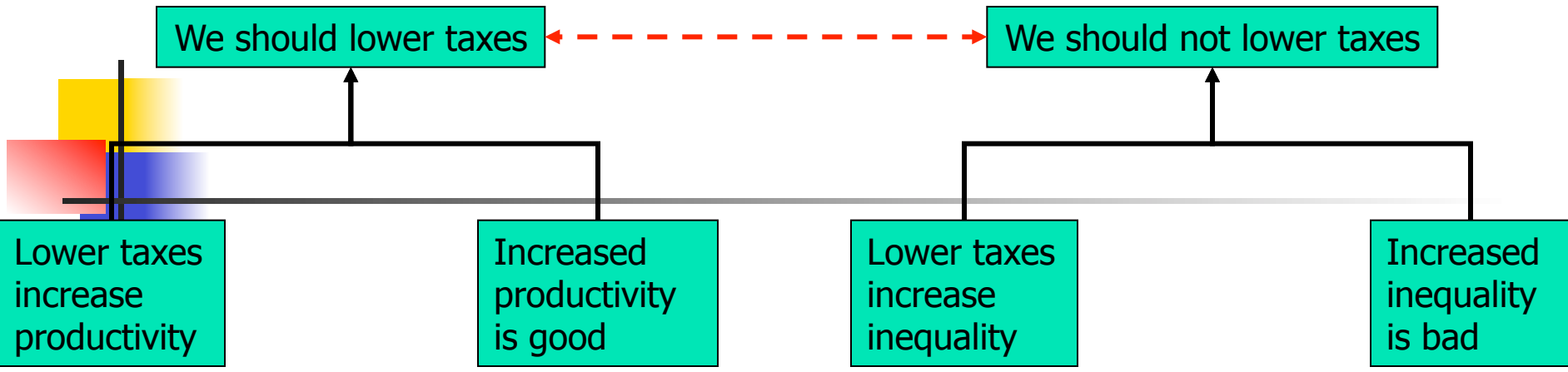
- **Abstract** argumentation
- Argumentation as **inference**
  - Frameworks for structured argumentation
    - Deductive vs. defeasible inferences
  - Argument schemes
- Argumentation as **dialogue**



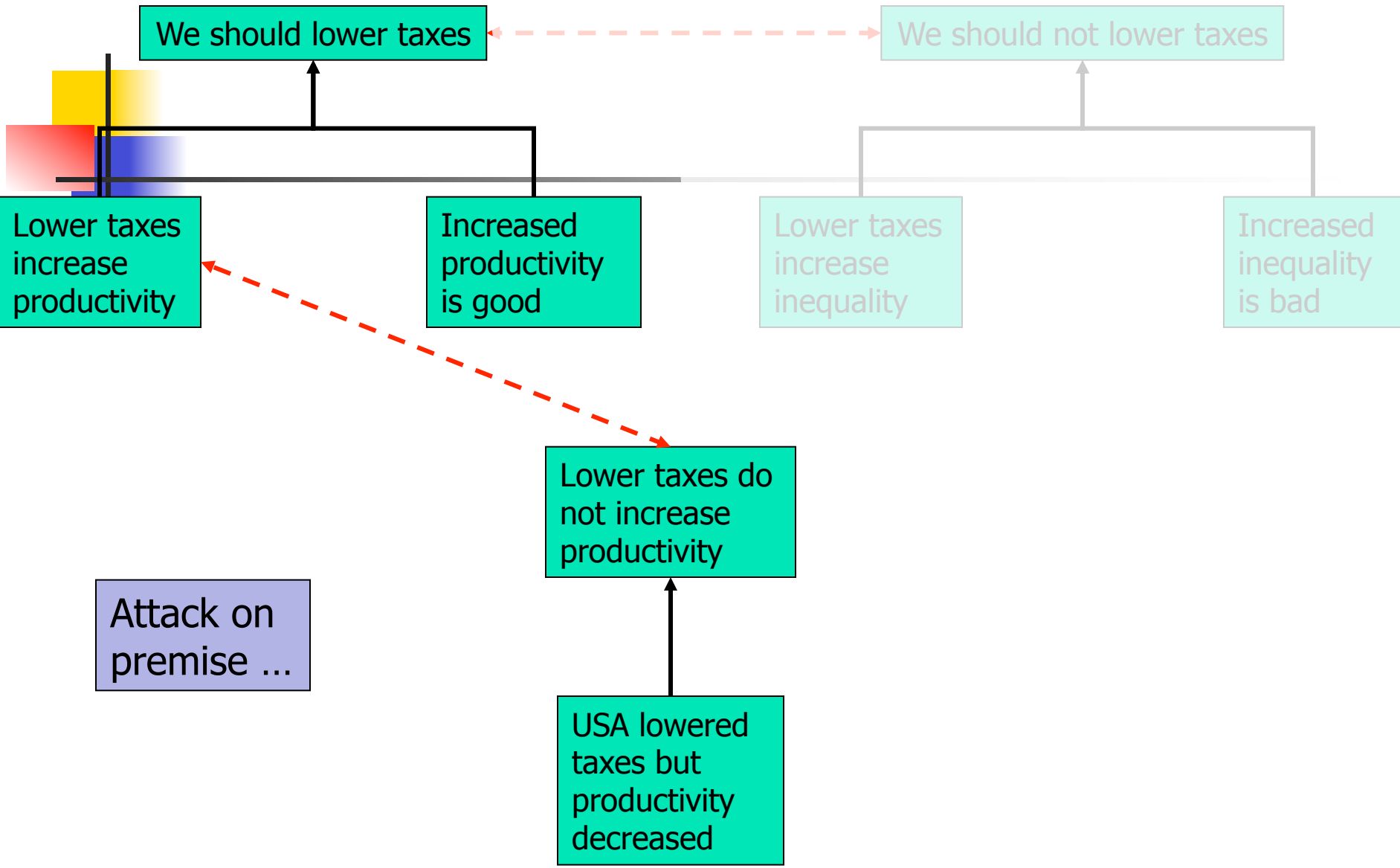
Lower taxes  
increase  
productivity

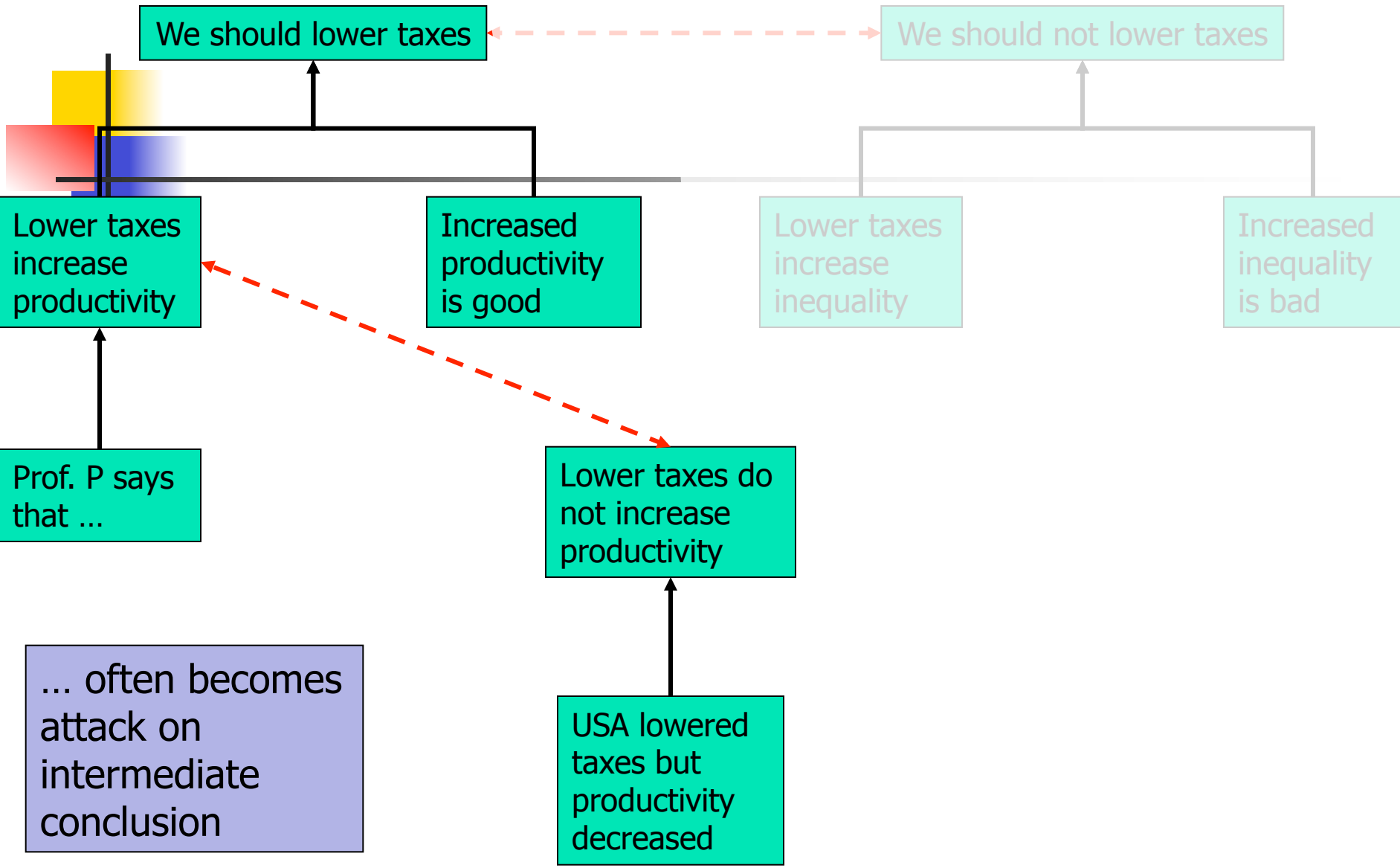
Increased  
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We should lower taxes

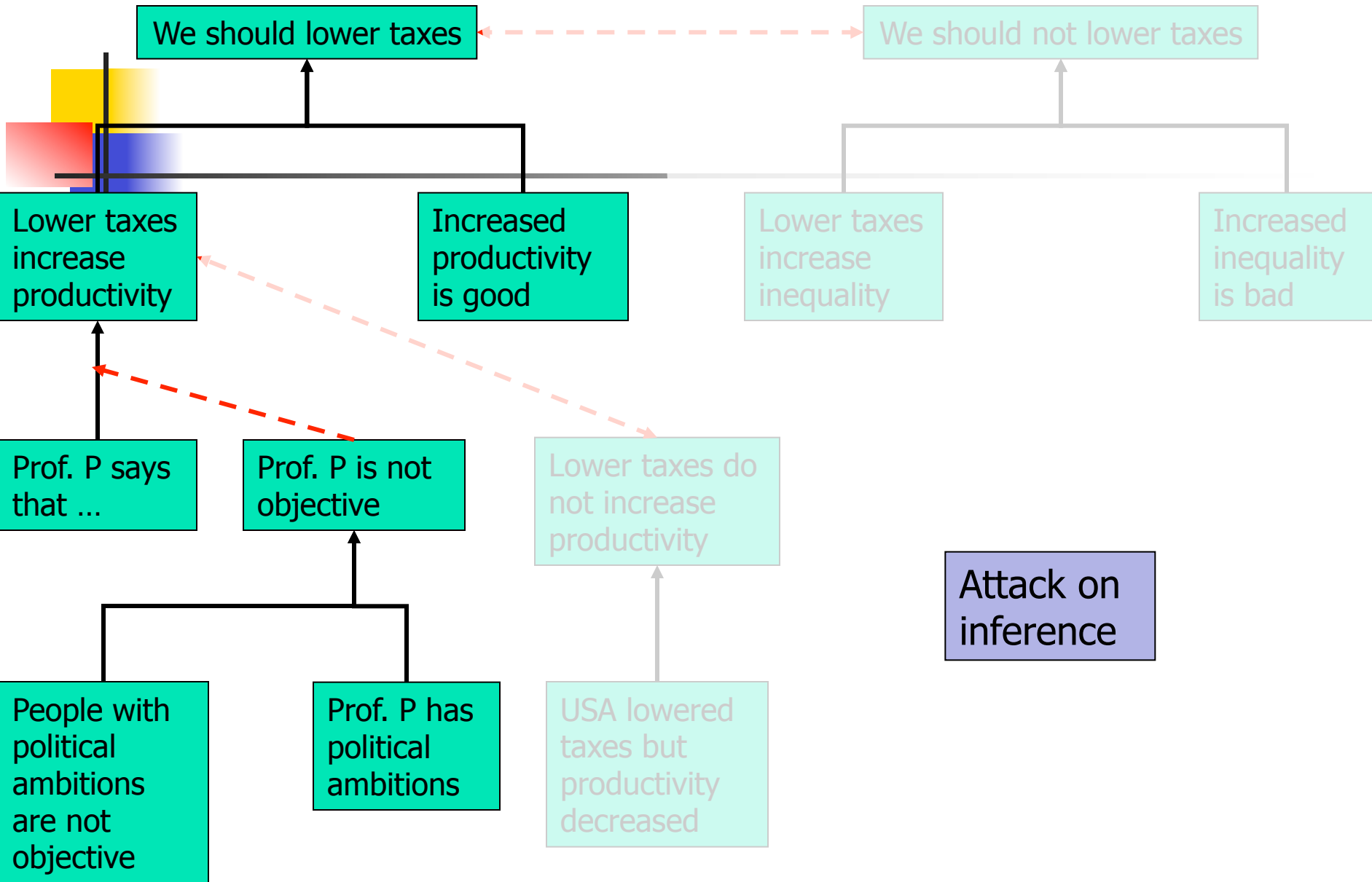


Attack on conclusion









We should lower taxes

We should not lower taxes

Lower taxes increase productivity

Increased productivity is good

Lower taxes increase inequality

Increased inequality is bad

Prof. P says that ...

Prof. P is not objective

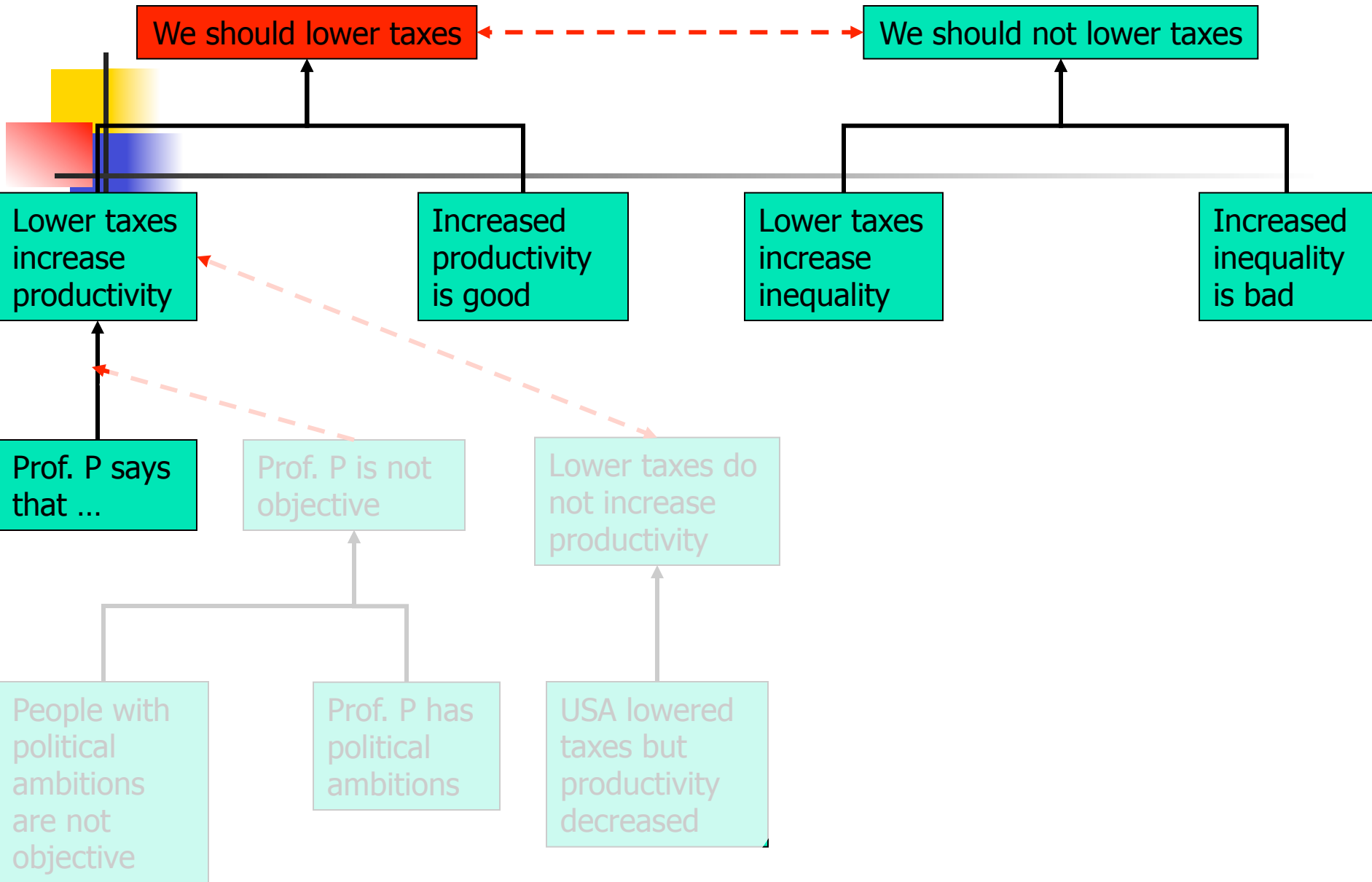
Lower taxes do not increase productivity

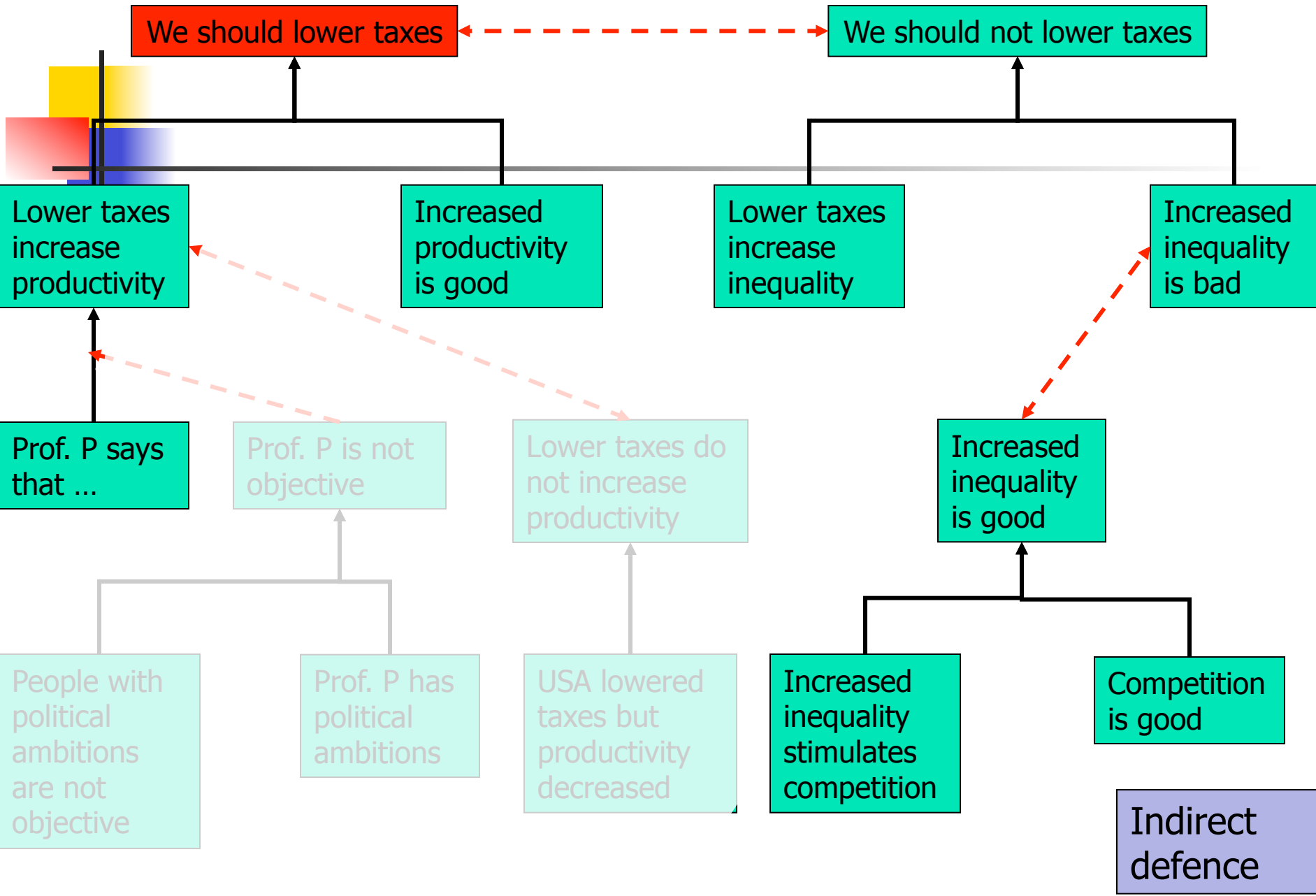
People with political ambitions are not objective

Prof. P has political ambitions

USA lowered taxes but productivity decreased

Attack on inference





We should lower taxes

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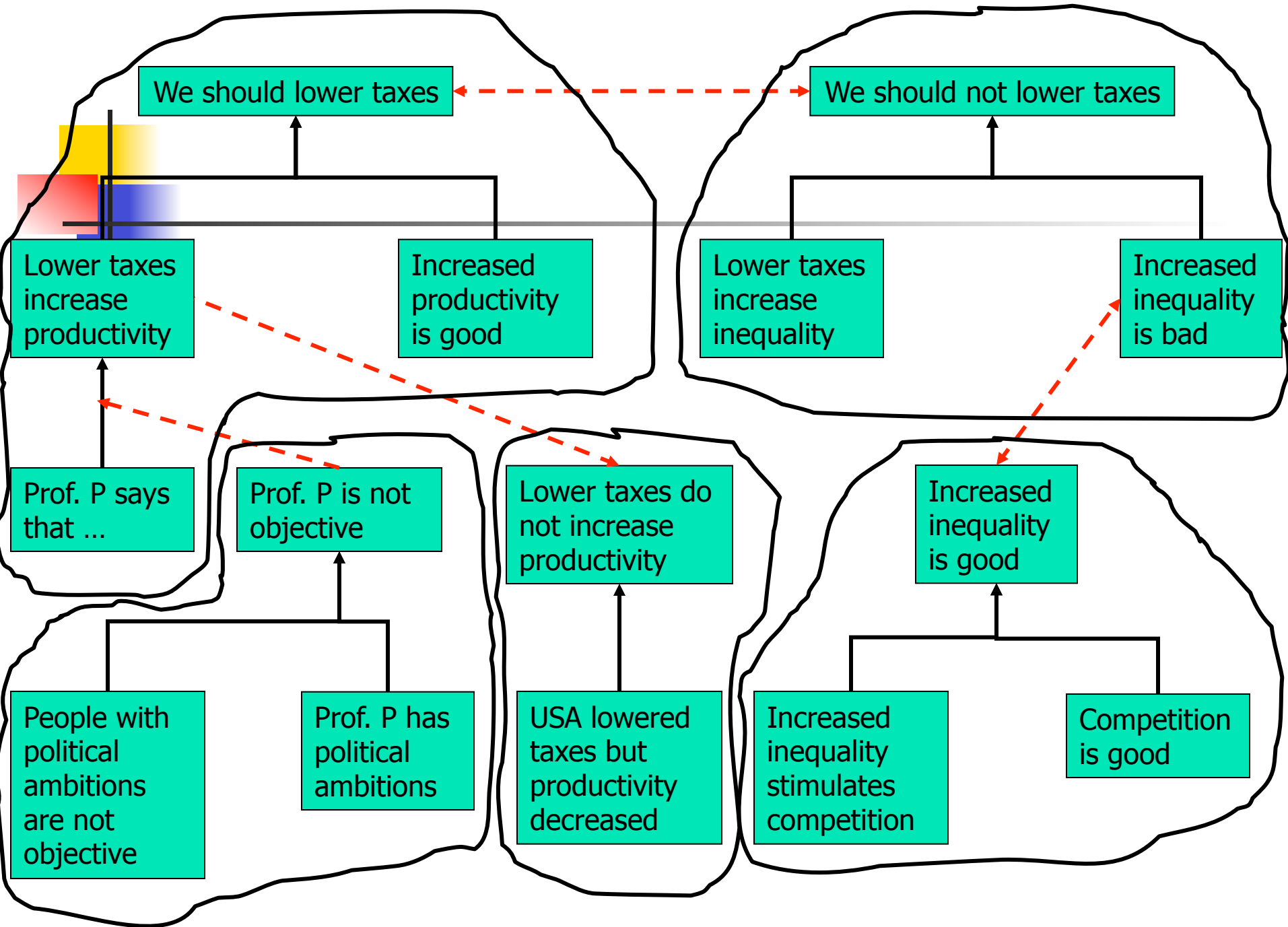
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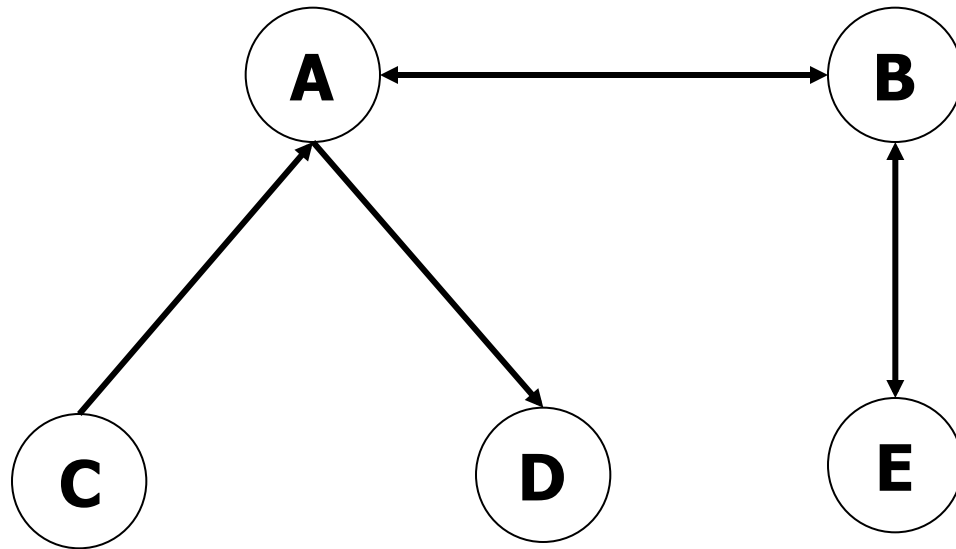
USA lowered taxes but productivity decreased

Increased inequality stimulates competition

Competition is good

Indirect defence



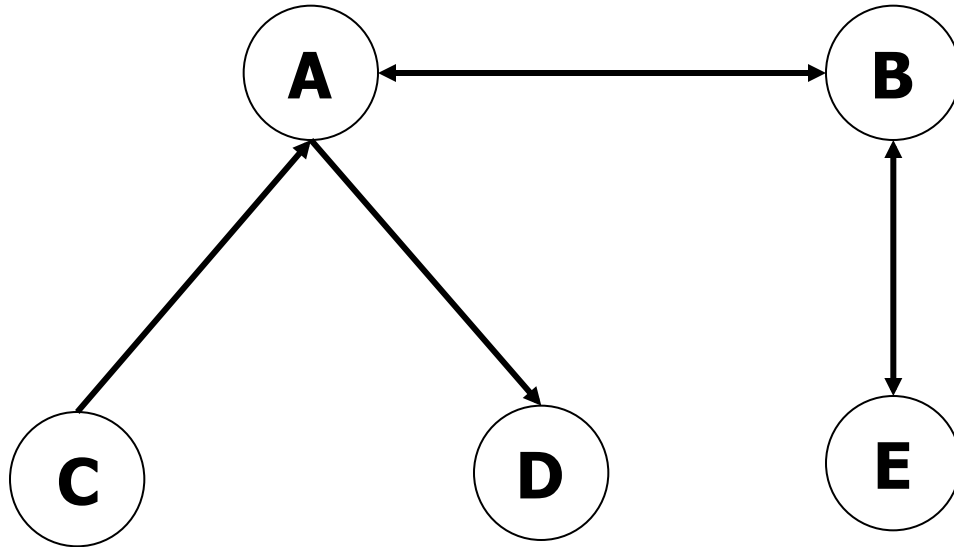


P.M. Dung, On the acceptability of arguments and its fundamental role in nonmonotonic reasoning, logic programming, and  $n$ -person games. *Artificial Intelligence*, 77:321–357, 1995.



1. An argument is *In* iff all arguments that attack it are *Out*.
2. An argument is *Out* iff some argument that attacks it is *In*.

Grounded semantics *minimises In* labelling  
Preferred semantics *maximises In* labelling  
Stable semantics labels *all* nodes





# Properties

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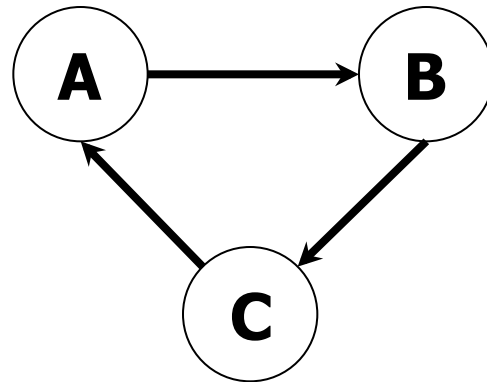
- There always exists exactly one grounded labelling
- There exists at least one preferred labelling
- Every stable labelling is preferred (but not v.v.)
- The grounded labelling is a subset of all preferred and stable labellings
- Every finite Dung graph without attack cycles has a unique labelling (which is the same in all semantics)
- ...

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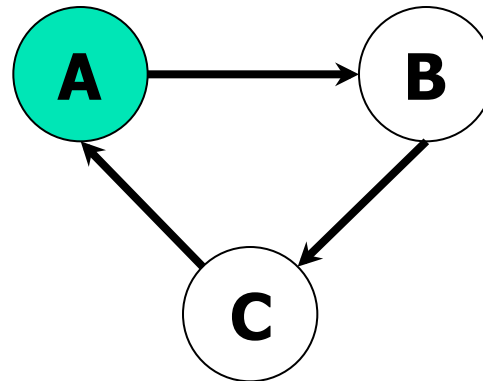


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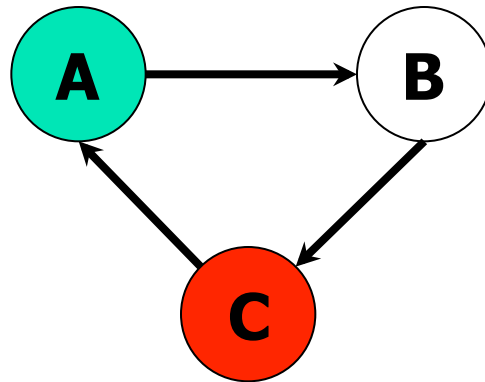


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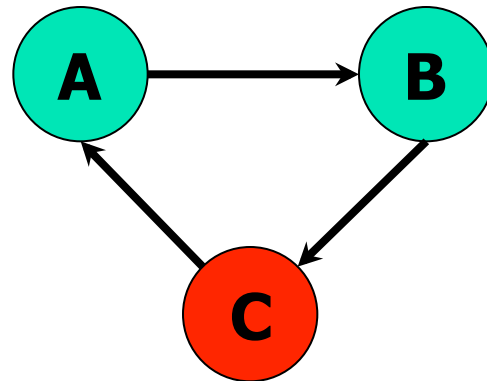


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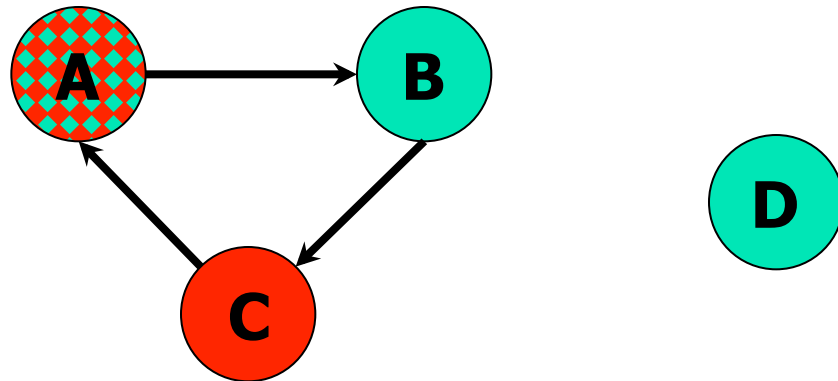


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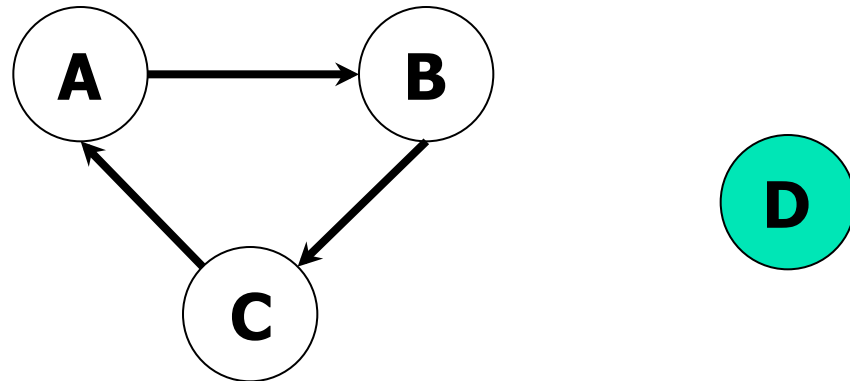


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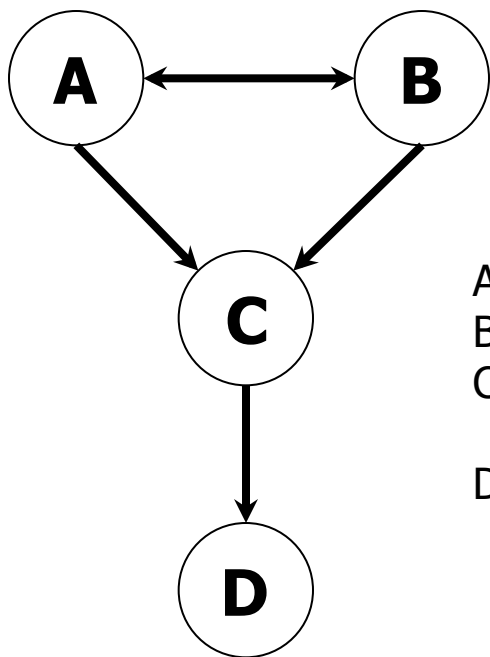
Preferred semantics *maximises In* labelling





# Difference between grounded and preferred labellings

1. An argument is *In* iff all arguments that attack it are *Out*.
2. An argument is *Out* iff some argument that attacks it is *In*.

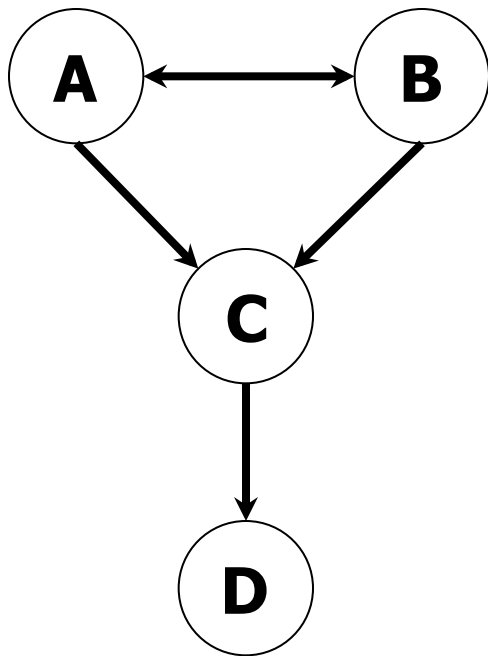


- A = Merkel is German since she has a German name
- B = Merkel is Belgian since she is often seen in Brussels
- C = Merkel is a fan of Oranje since she wears an orange shirt (unless she is German or Belgian)
- D = Merkel is not a fan of Oranje since she looks like someone who does not like football

(Generalisations are left implicit)

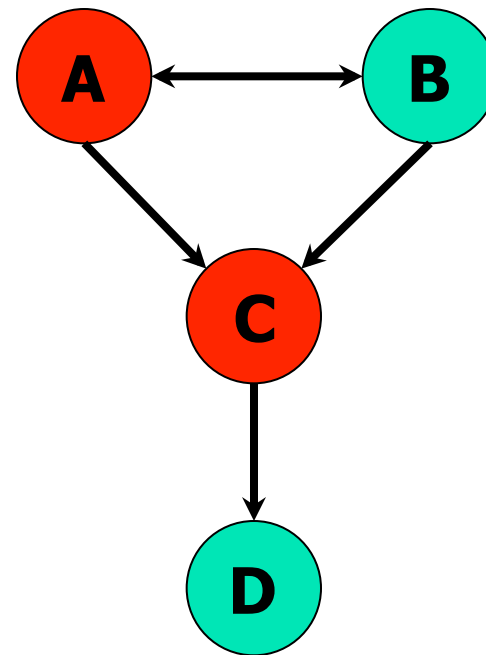
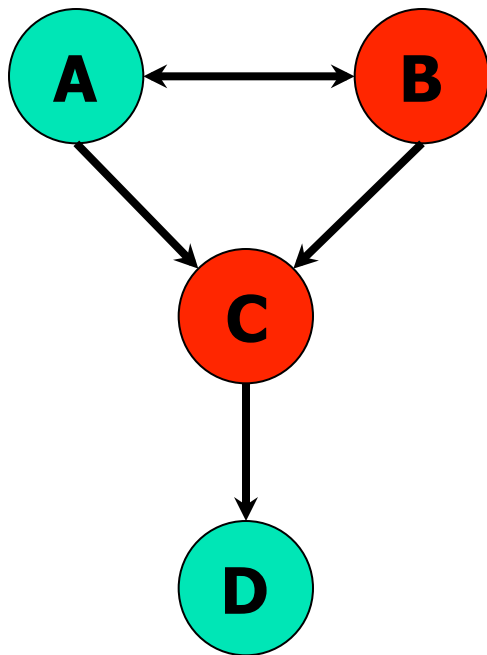
# The grounded labelling

1. An argument is *In* iff all arguments that attack it are *Out*.
2. An argument is *Out* iff some argument that attacks it is *In*.



# The preferred labellings

1. An argument is *In* iff all arguments that attack it are *Out*.
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# Justification status of arguments

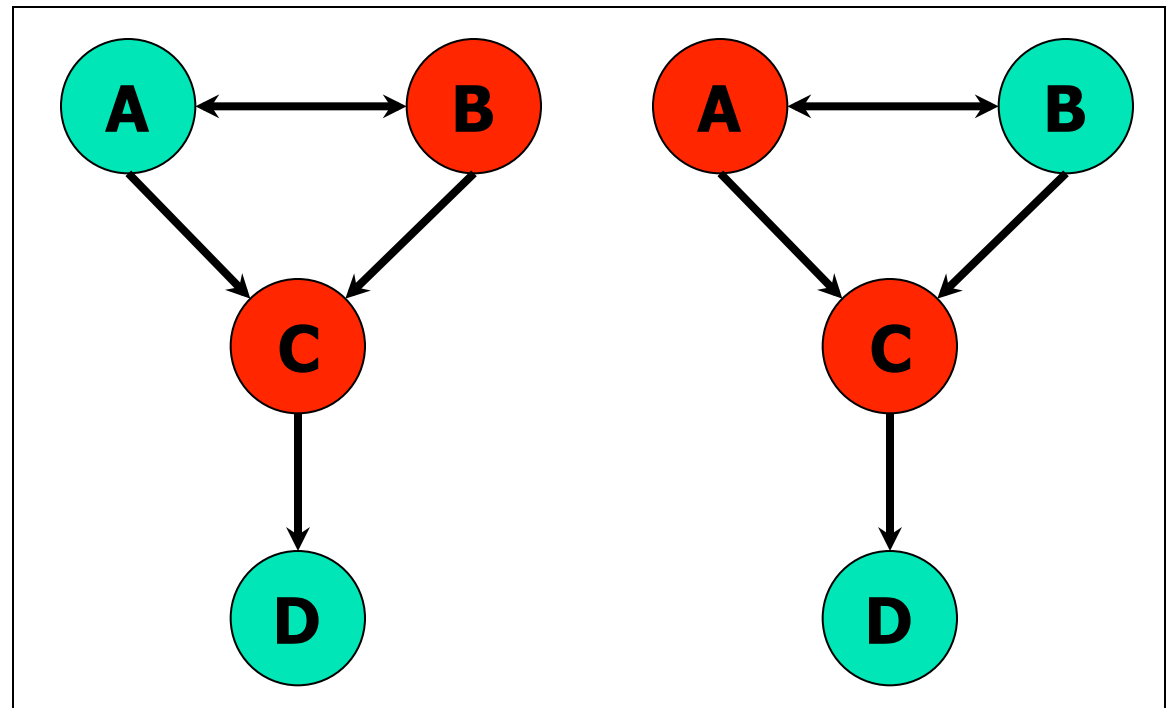
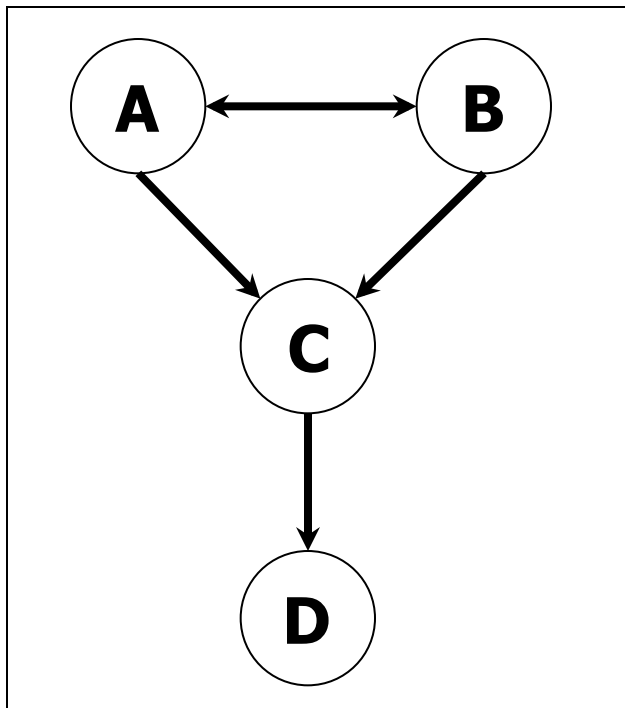
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- A is **justified** if A is *In* in all labellings
- A is **overruled** if A is *Out* in all labellings
- A is **defensible** otherwise

# Argument status in grounded and preferred semantics

**Grounded** semantics:  
all arguments defensible

**Preferred** semantics:  
A and B defensible  
C overruled  
D justified





# Labellings and extensions

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Given an argumentation framework  $AF = \langle Arg, attack \rangle$ :

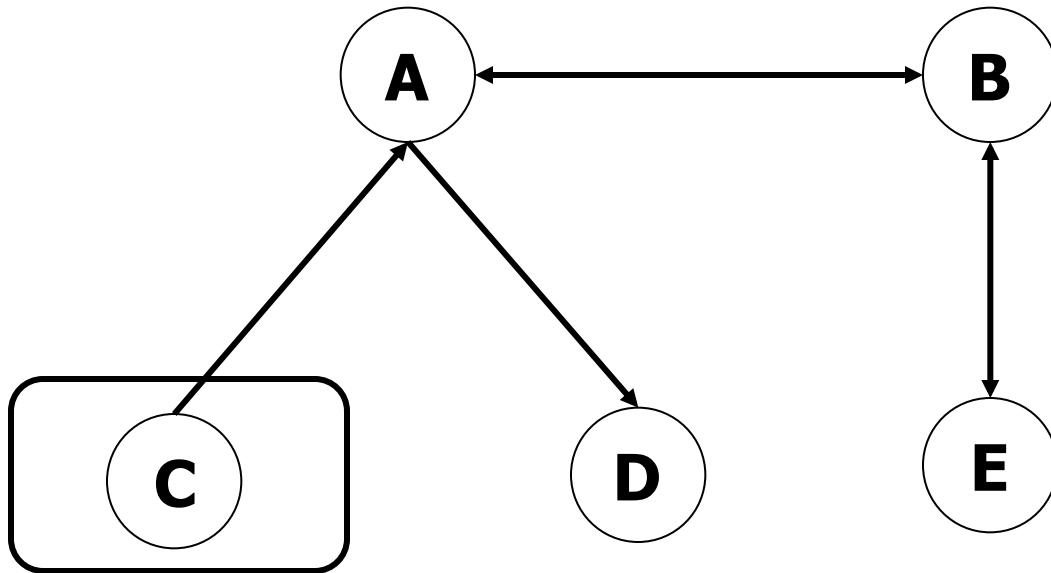
$S \subseteq Arg$  is a stable/preferred/grounded **argument extension** iff  $S = In$  for some stable/preferred/grounded **labelling**



# Grounded extension

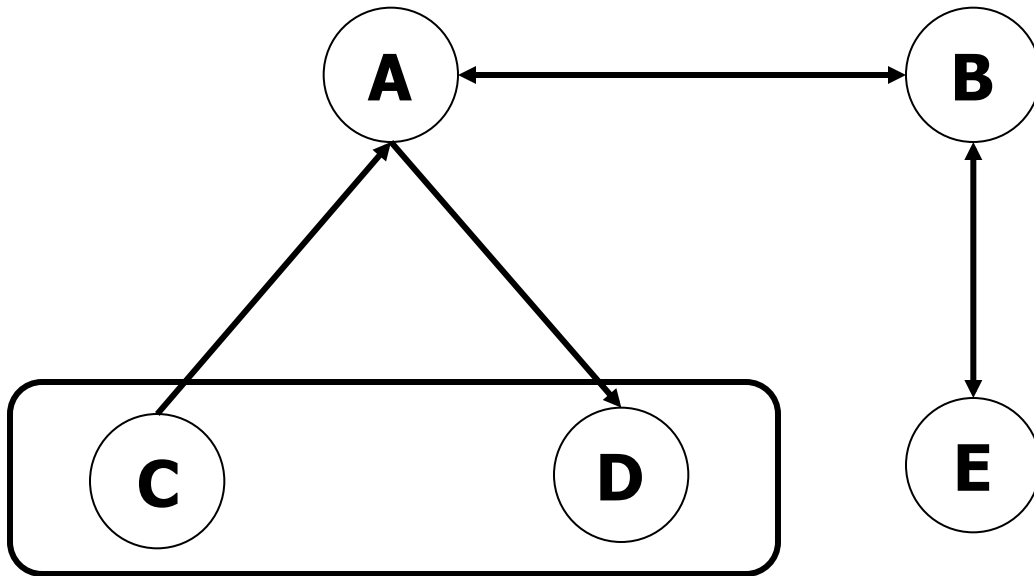
- $A$  is **acceptable wrt**  $S$  (or  $S$  **defends**  $A$ ) if all attackers of  $A$  are attacked by  $S$ 
  - $S$  **attacks**  $A$  if an argument in  $S$  attacks  $A$
- Let  $AF$  be an abstract argumentation framework
  - $F_{AF}^0 = \emptyset$
  - $F_{AF}^{i+1} = \{A \in \text{Args} \mid A \text{ is acceptable wrt } F_{AF}^i\}$
  - $F_{AF}^\infty = \bigcup_{i=0}^{\infty} (F_{AF}^{i+1})$
- If no argument has an infinite number of attackers, then  $F_{AF}^\infty$  is the grounded extension of  $AF$  (otherwise it is included)

S **defends** A if all attackers of A are attacked by a member of S



$$F^1 = \{A\}$$

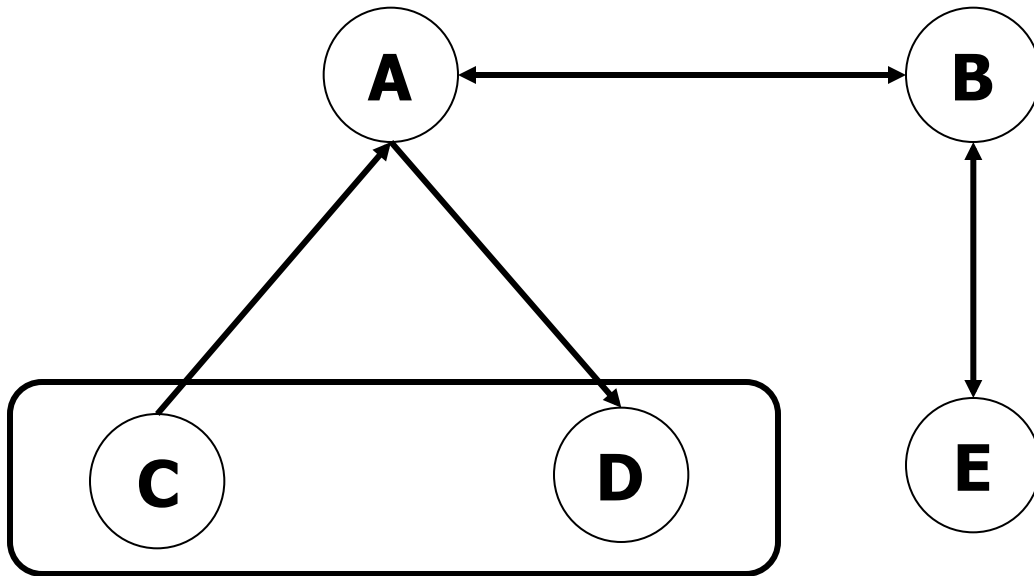
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$$F^1 = \{A\}$$

$$F^2 = \{A, D\}$$

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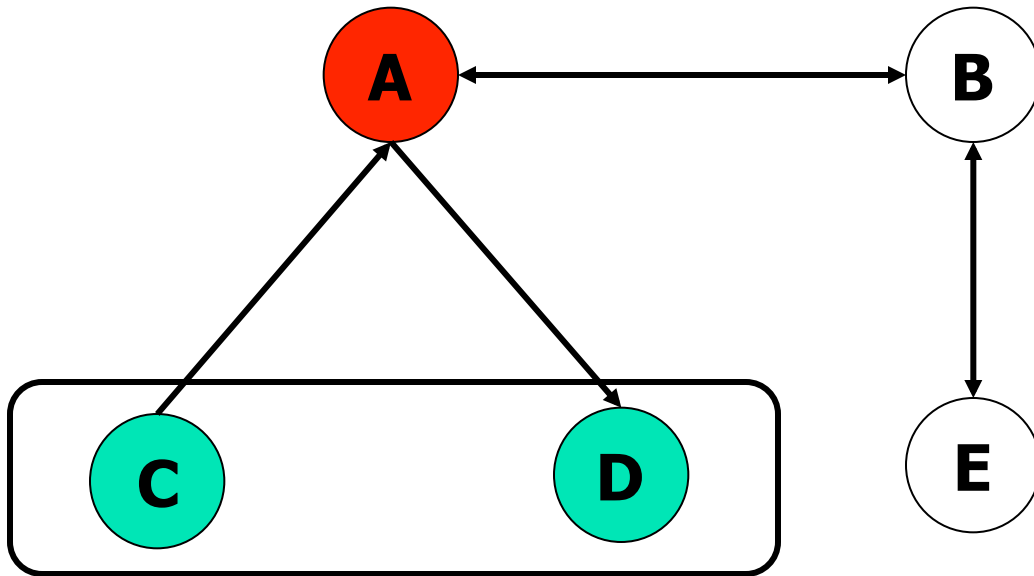
$$F^1 = \{A\}$$

$$F^2 = \{A, D\}$$

$$F^3 = F^2$$

S **defends** A if all defeaters of A are attacked by a member of S

S is **admissible** if it is conflict-free and defends all its members



Grounded





# Stable extensions

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- Dung (1995):
  - $S$  is **conflict-free** if no member of  $S$  attacks a member of  $S$
  - $S$  is a **stable extension** if it is conflict-free and attacks all arguments outside it
- Recall:
  - $S$  is a **stable argument extension** if  $S = In$  for some stable labelling
- **Proposition:**  $S$  is a stable argument extension iff  $S$  is a stable extension



# Preferred extensions

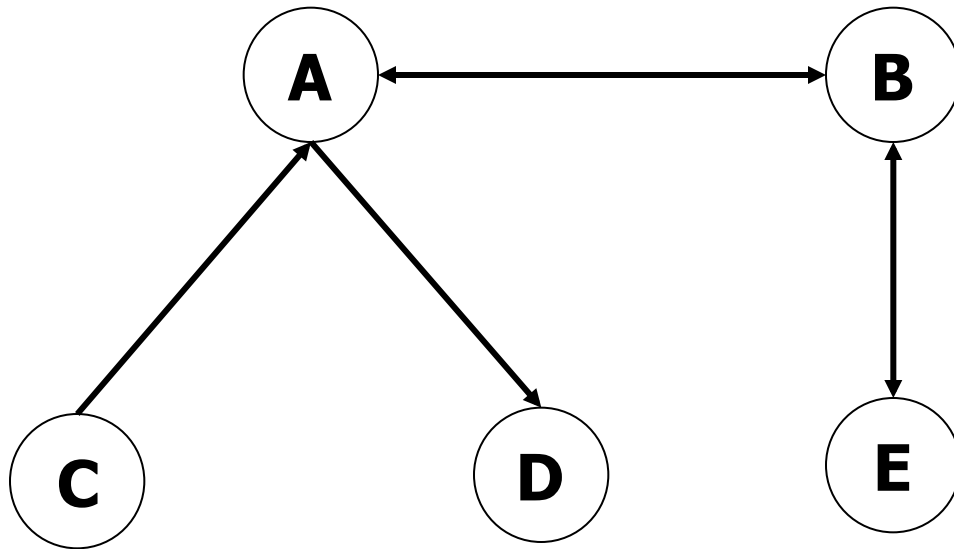
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- Dung (1995):
  - $S$  is **conflict-free** if no member of  $S$  attacks a member of  $S$
  - $S$  is **admissible** if it is conflict-free and all its members are acceptable wrt  $S$
  - $S$  is a **preferred extension** if it is  $\subseteq$ -maximally admissible
- Recall:
  - $S$  is a **preferred argument extension** if  $S = In$  for some preferred labelling
- **Proposition:**  $S$  is a preferred argument extension iff  $S$  is a preferred extension

S **defends** A if all attackers of A are attacked by a member of S

S is **admissible** if it is conflict-free and defends all its members

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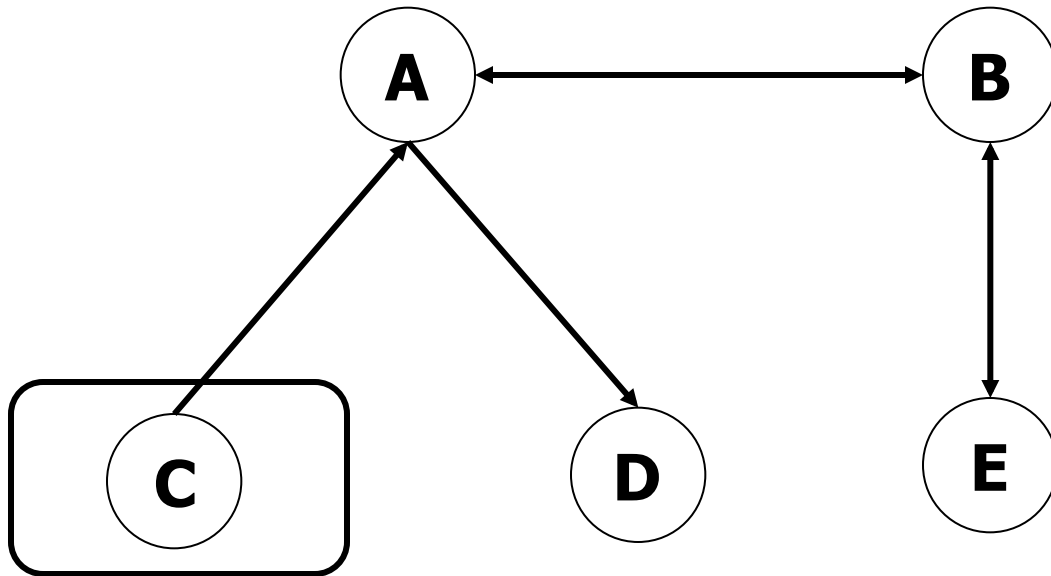


Admissible?

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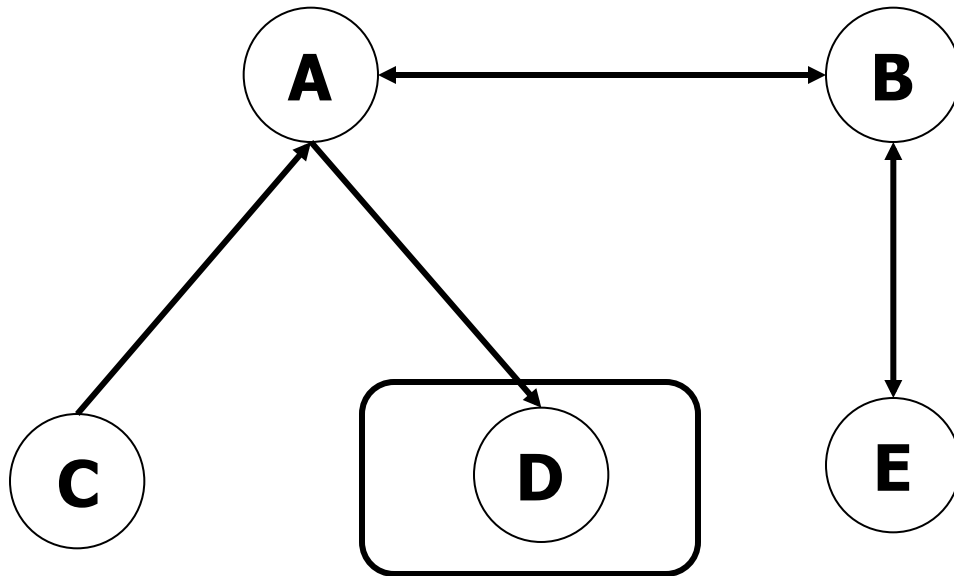


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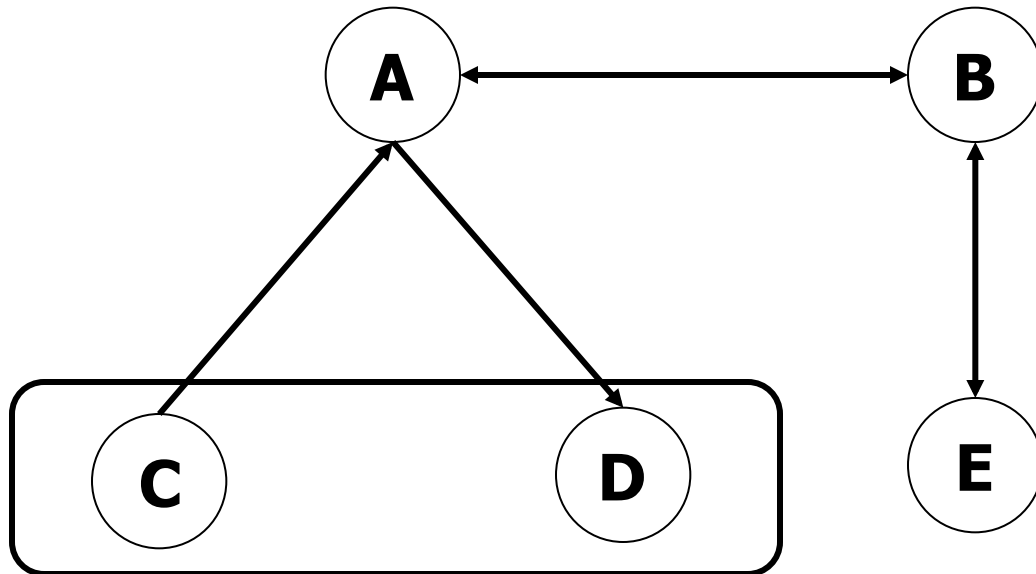


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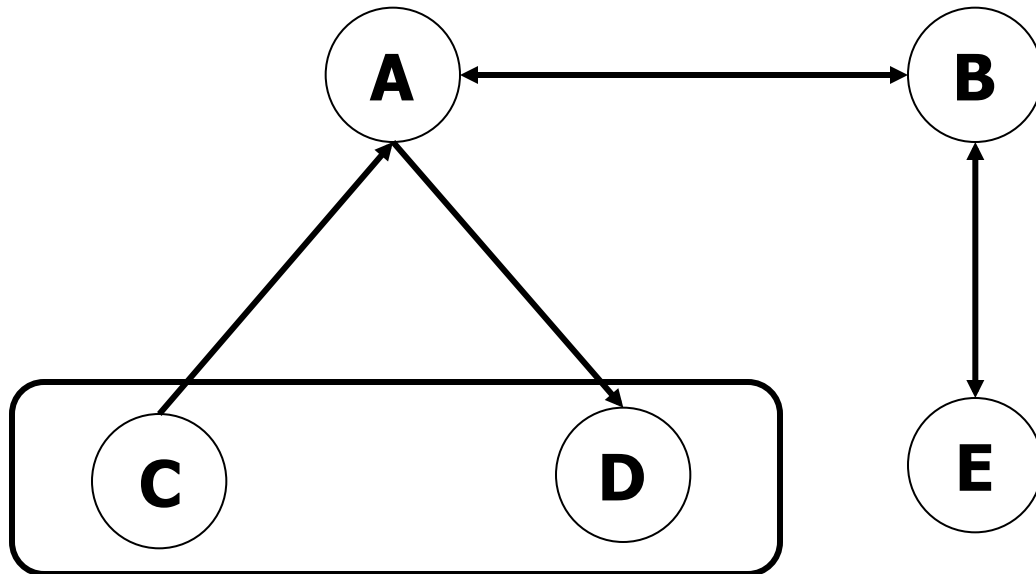


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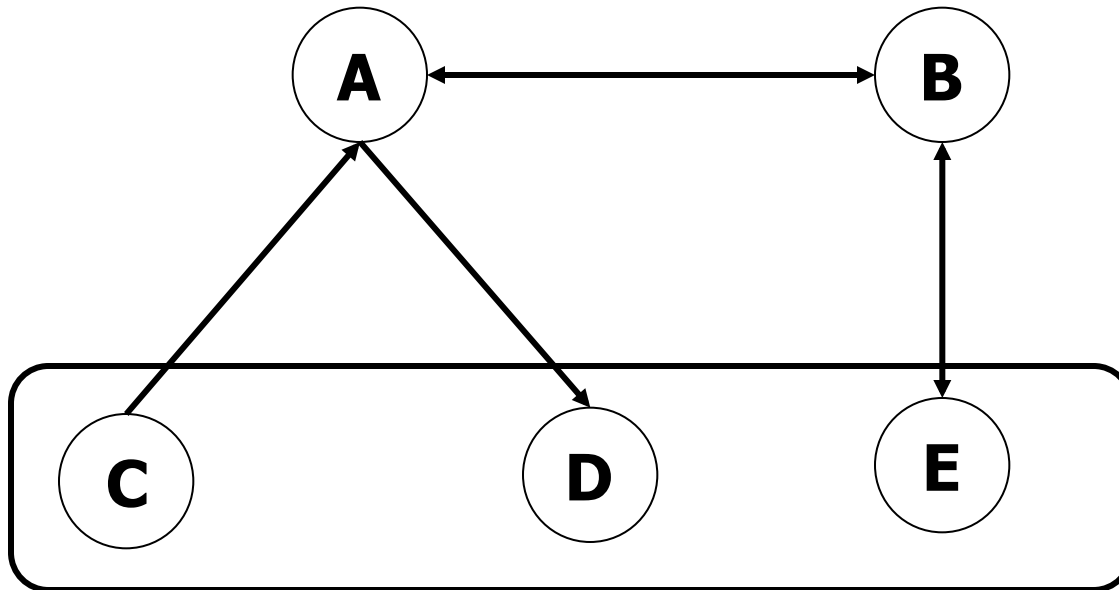
Preferred?

S is **preferred** if it is maximally admissible

S **defends** A if all defeaters of A are attacked by a member of S

S is **admissible** if it is conflict-free and defends all its members

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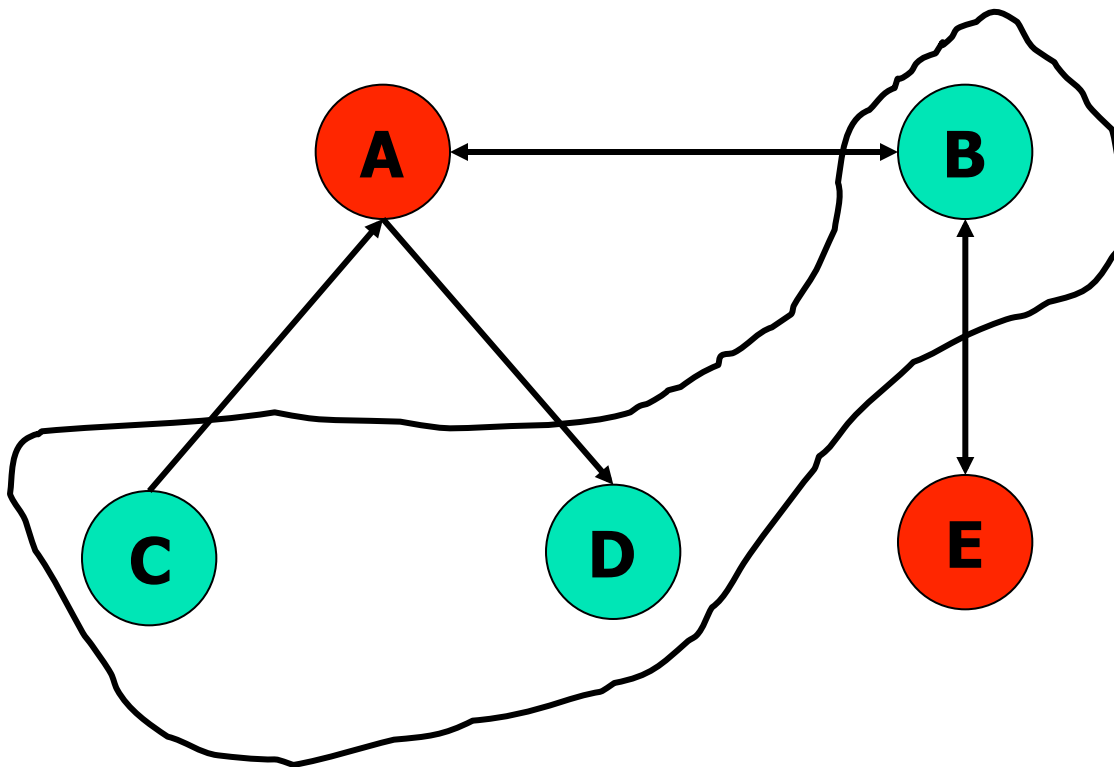
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S is **preferred** if it is maximally admissible



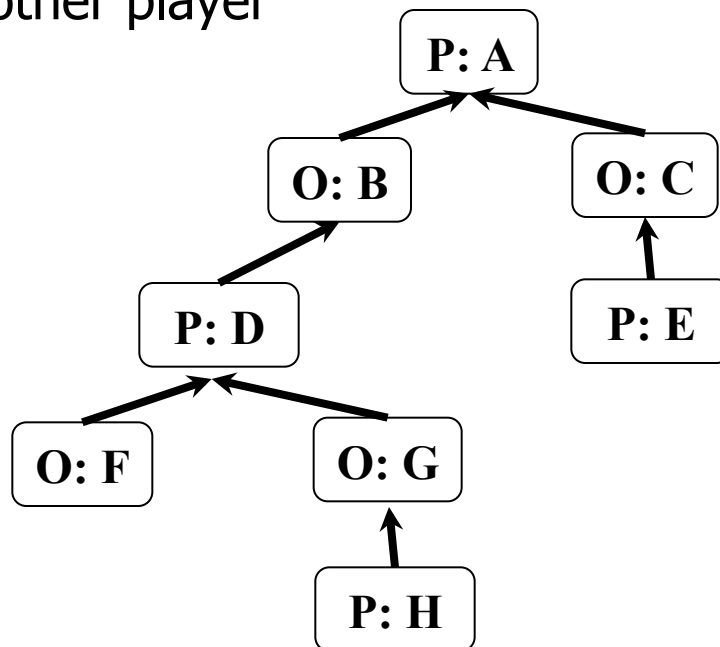
# Proof theory for abstract argumentation

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- **Argument games** between proponent  $P$  and opponent  $O$ :
  - Proponent starts with an argument
  - Then each party replies with a suitable attacker
  - A winning criterion
    - E.g. the other player cannot move
- Acceptability status corresponds to existence of a **winning strategy**.

# Strategies

- A **strategy** for player  $p$  is a partial game tree:
  - Every branch is a game (sequence of allowable moves)
  - The tree only branches after moves by  $p$
  - The children of  $p$ 's moves are all the legal moves by the other player





# Strategies

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- A strategy for player  $p$  is **winning** iff  $p$  wins all games in the strategy
- Let  $\mathbf{S}$  be an argument game:  $A$  is  **$\mathbf{S}$ -provable** iff  $P$  has a winning strategy in an  $\mathbf{S}$ -game that begins with  $A$

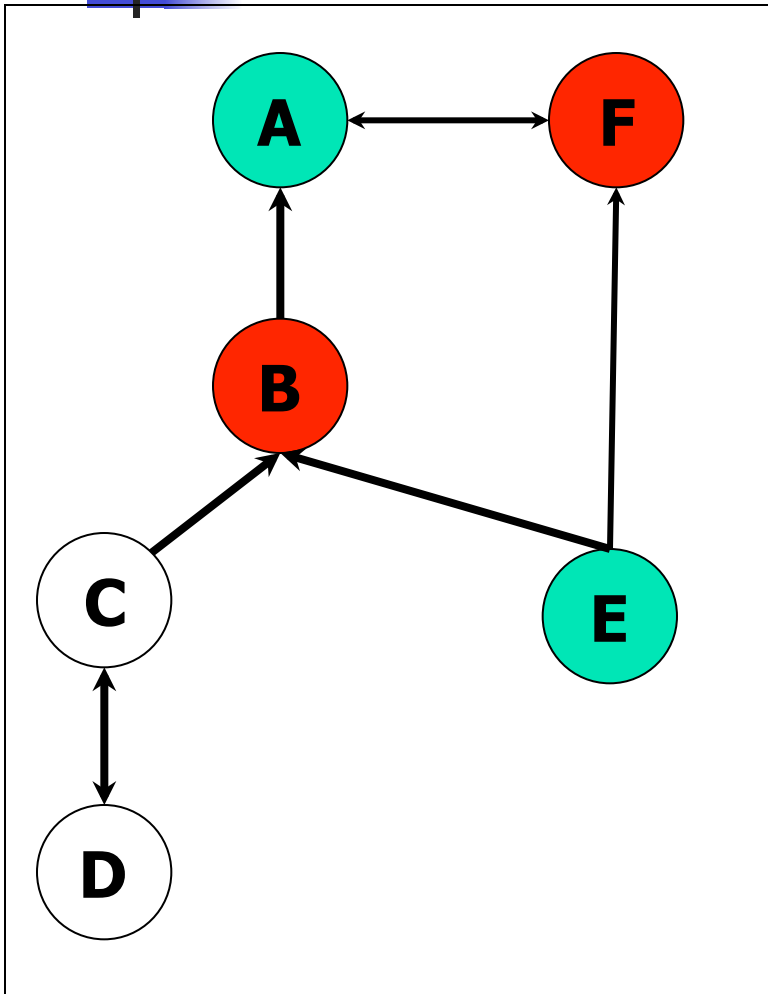


# The G-game for grounded semantics:

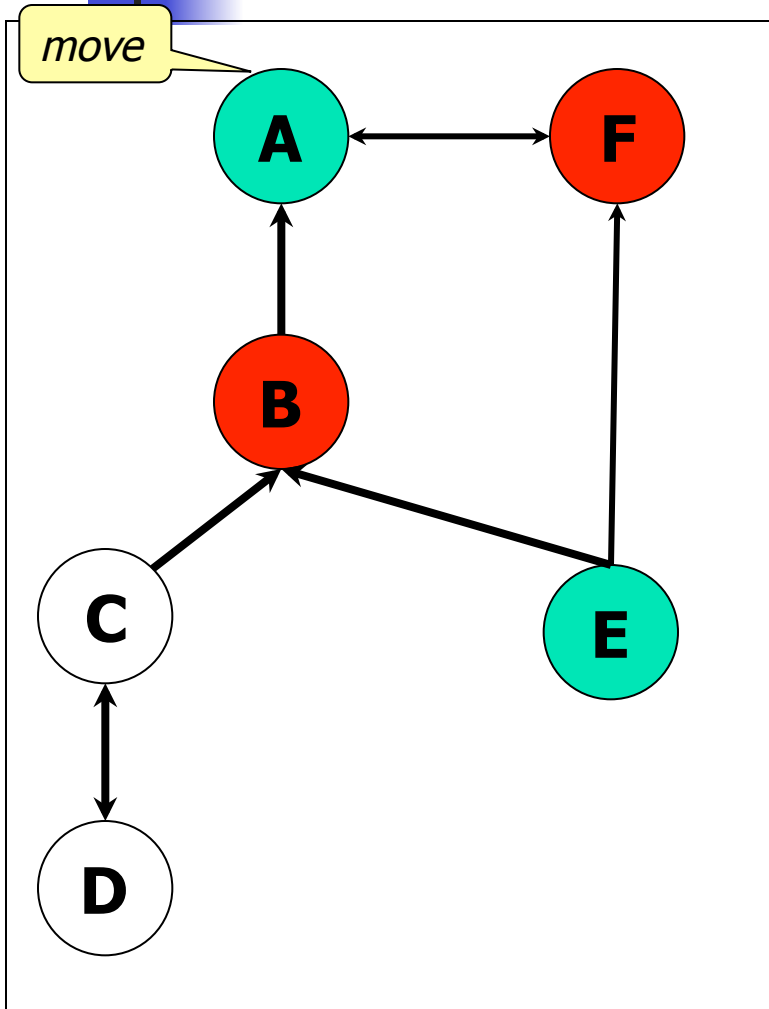
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- A **sound** and **complete** game:
  - Each move must reply to the previous move
  - Proponent cannot repeat his moves
  - Proponent moves strict attackers, opponent moves attackers
  - A player **wins** iff the other player cannot move
- **Proposition:**  $A$  is in the grounded extension iff  $A$  is G-provable

# An attack graph

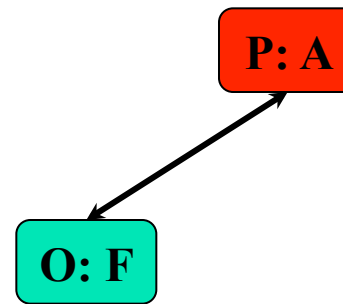
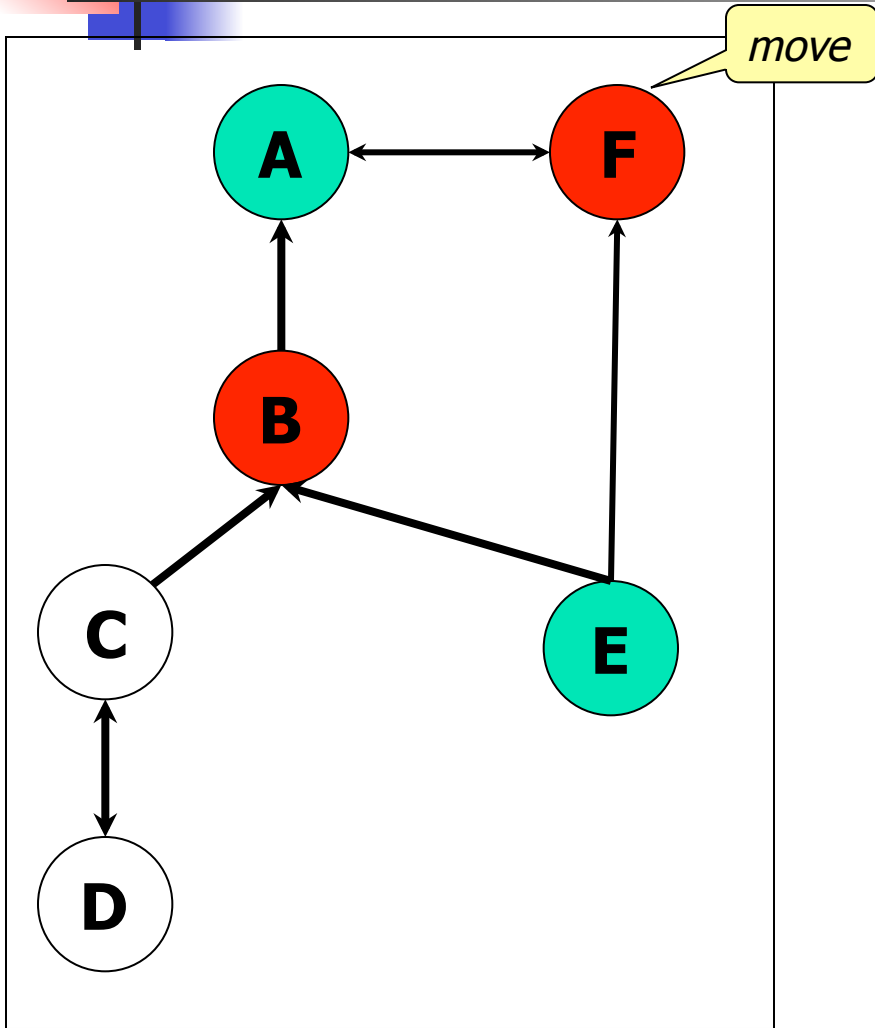


# A game tree



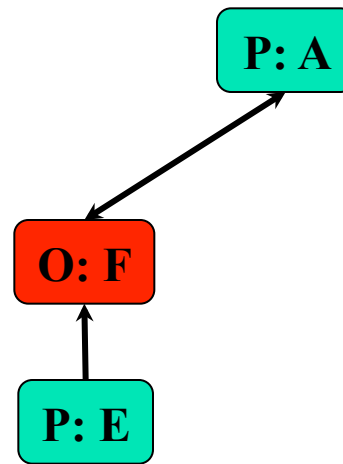
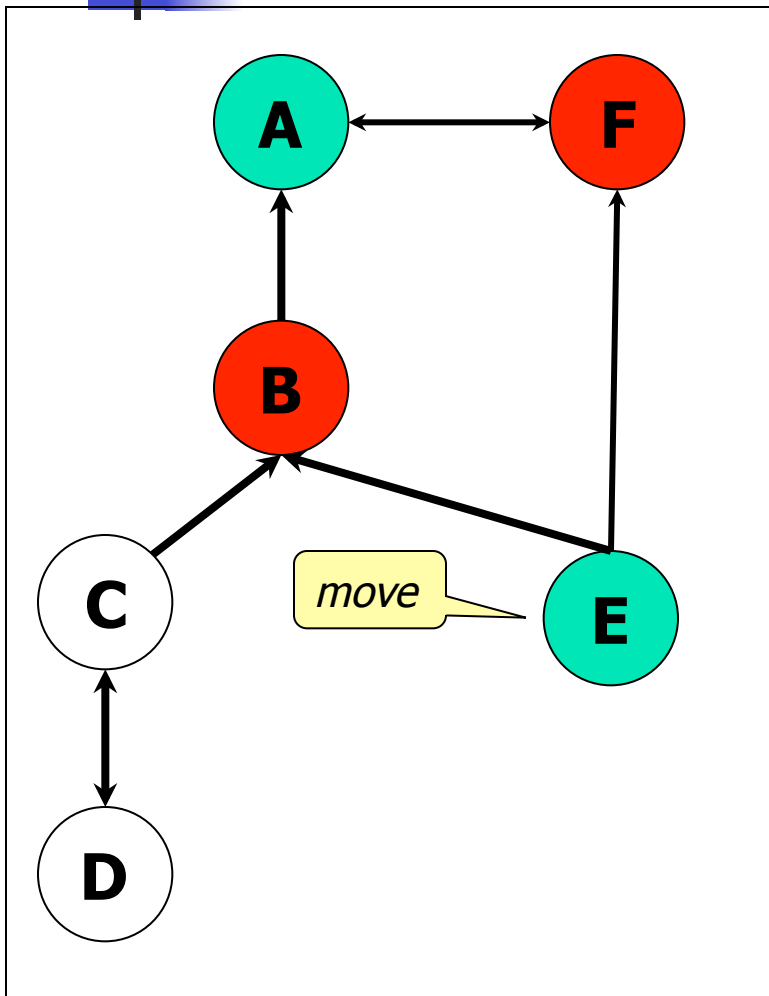
P: A

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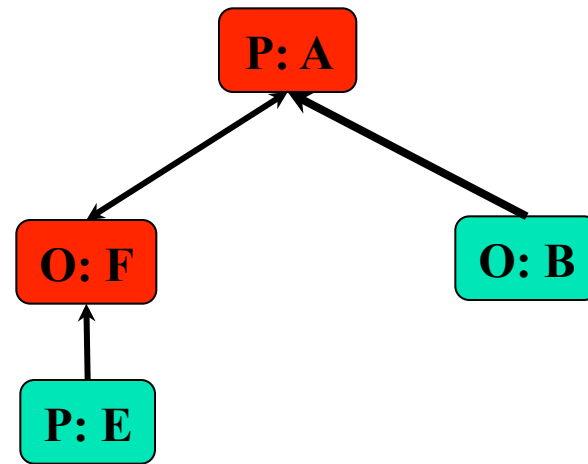
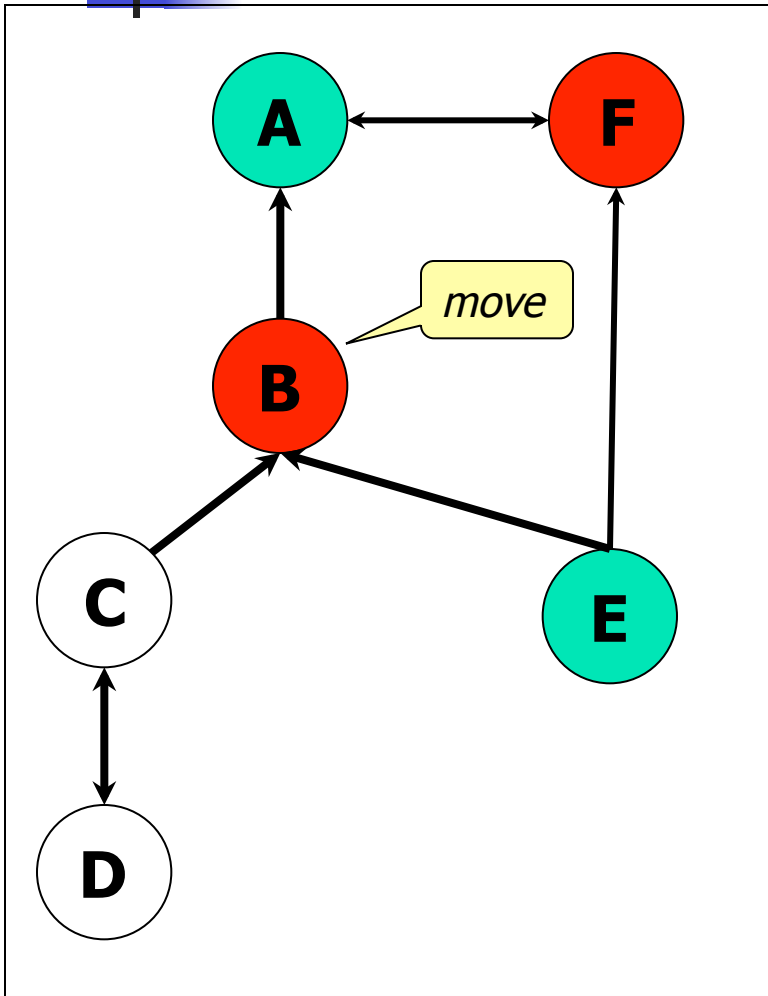




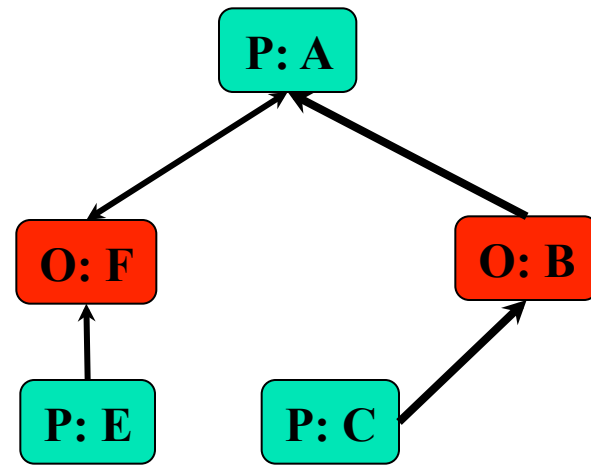
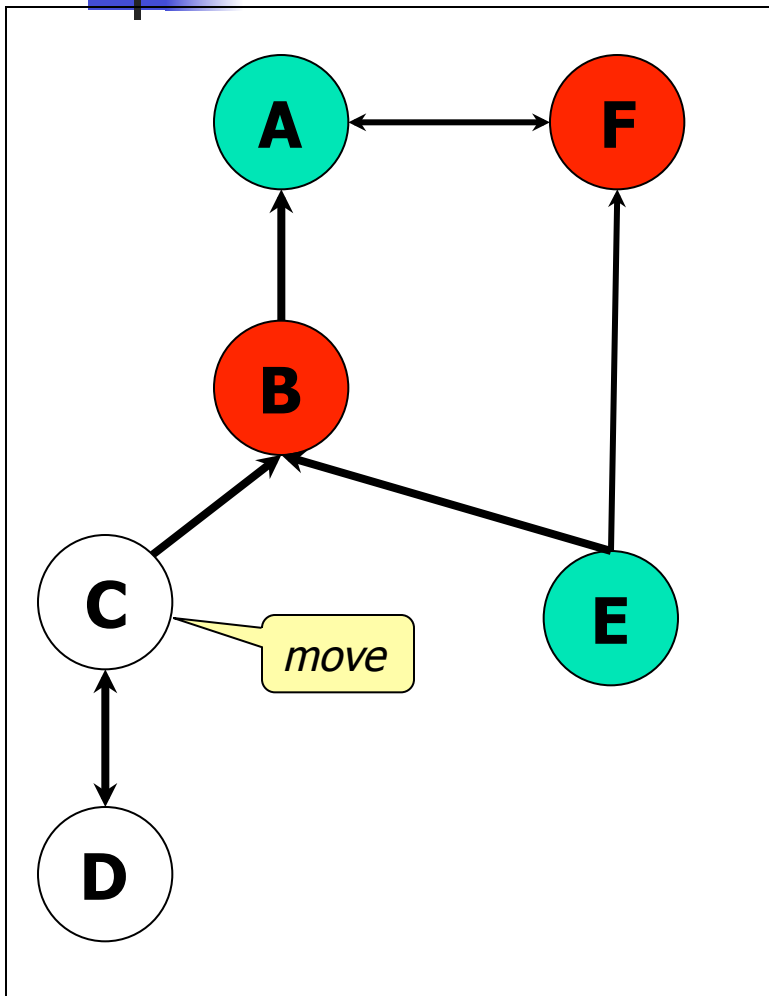
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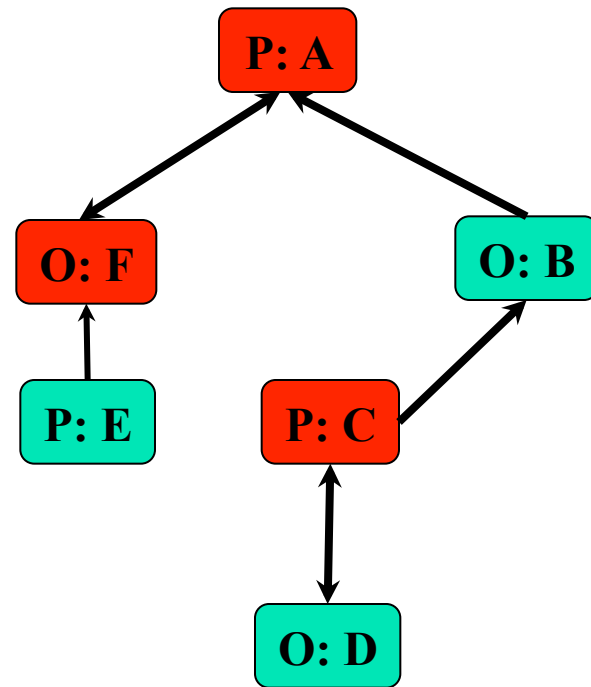
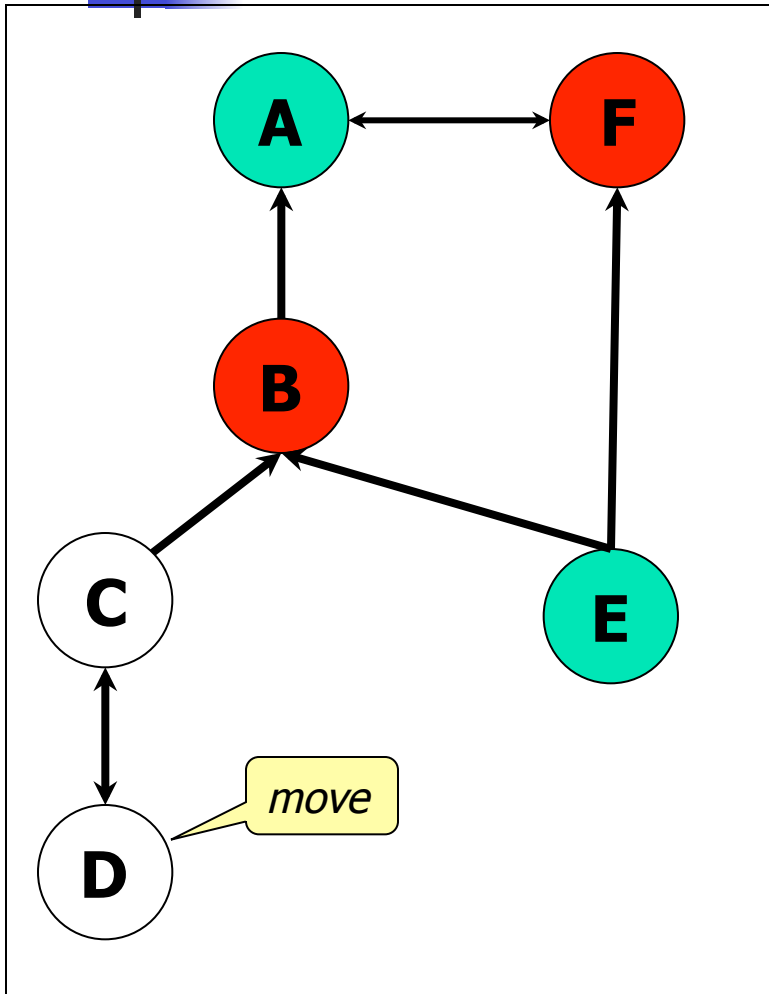
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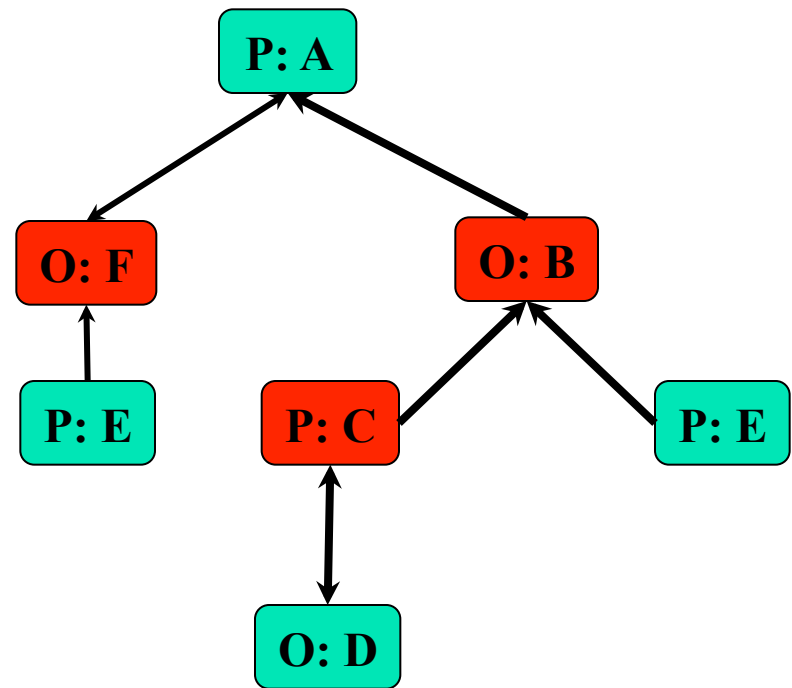
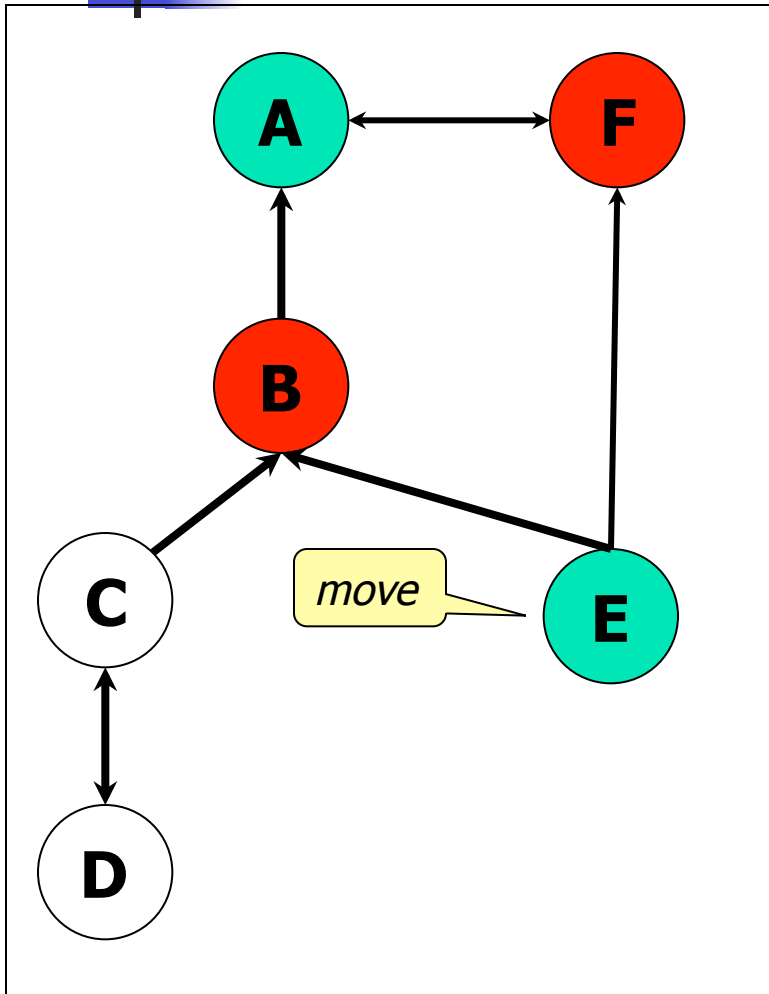
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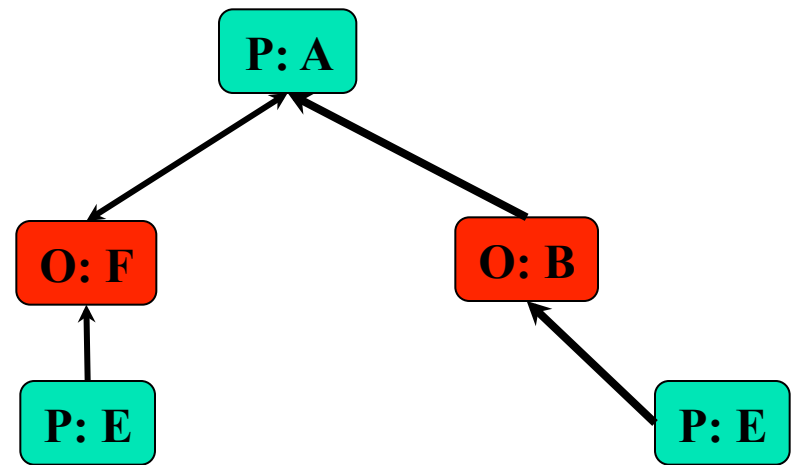
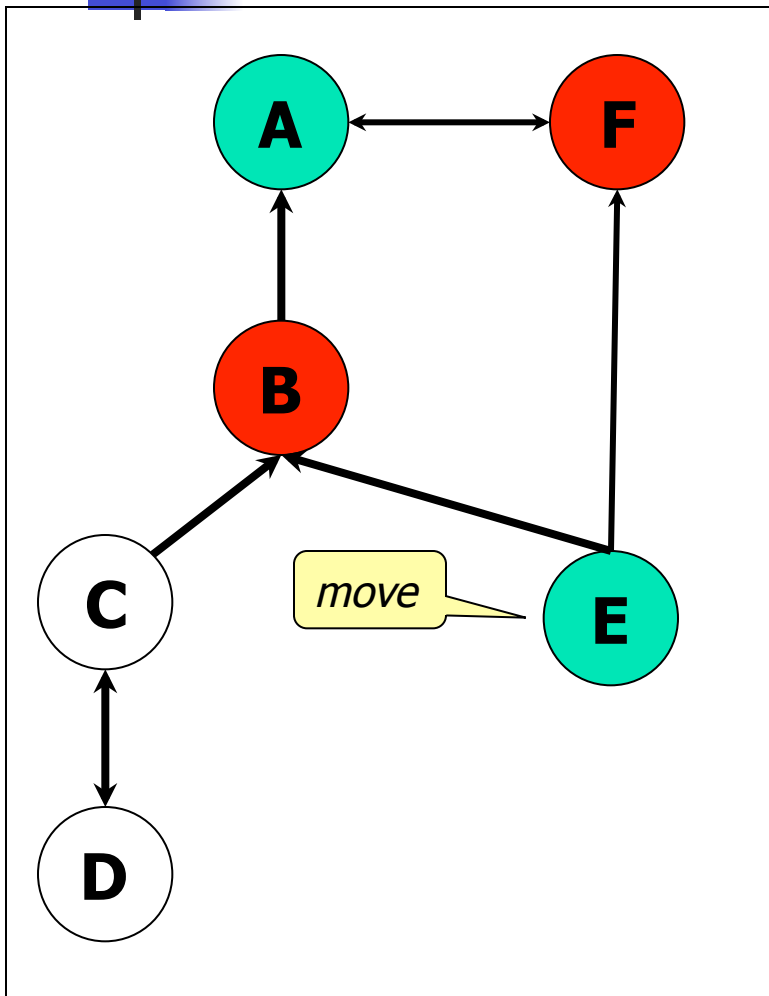
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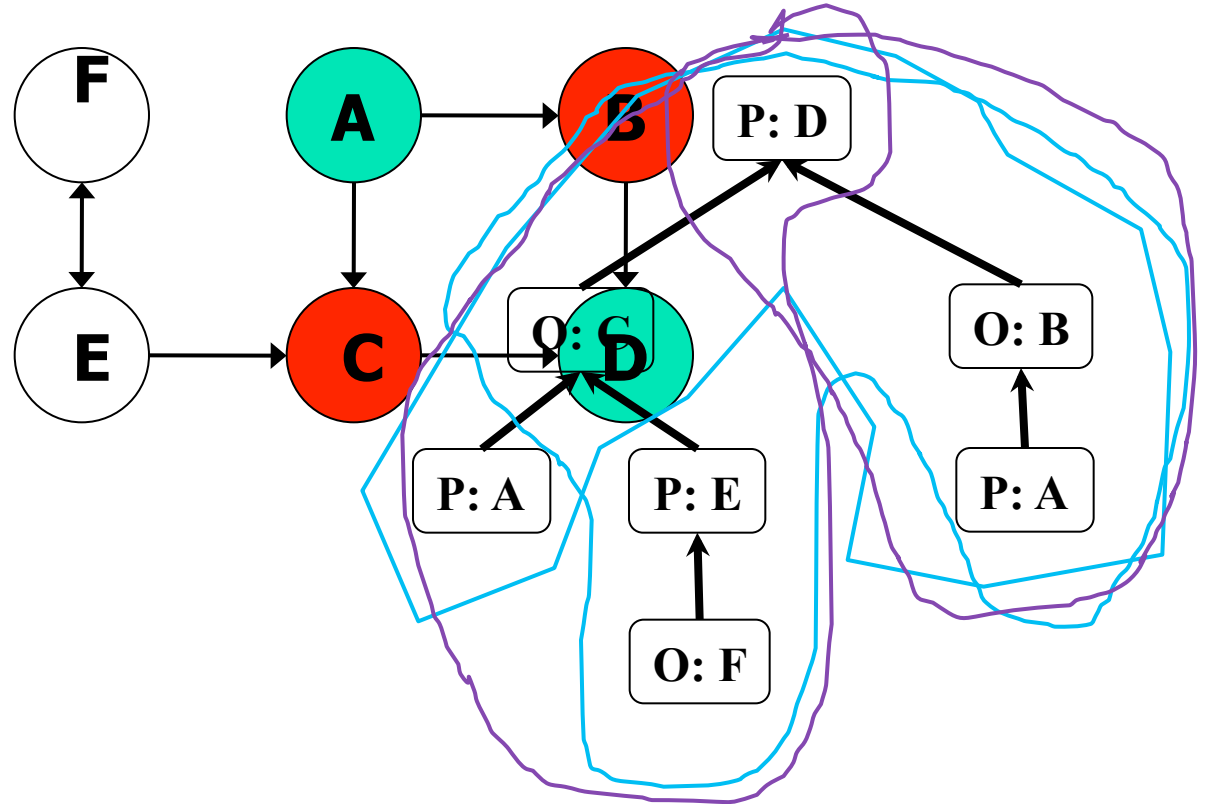
# A game tree



# Proponent's winning strategy



# Exercise



Slide made by Liz Black



# Research on abstract argumentation

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- New semantics
- Algorithms
  - Finding labellings (extensions)
  - Games
- Complexity
- Dynamics (adding or deleting arguments or attacks)
- Addition of new elements to AFs:
  - abstract support relations
  - preferences
- **Reasons to be sceptical:**
  - S. Modgil & H. Prakken, Resolutions in structured Argumentation. In *Proceedings of COMMA 2012*.
  - H. Prakken, Some reflections on two current trends in formal argumentation. In *Festschrift for Marek Sergot*, Springer 2012.
  - H. Prakken, On support relations in abstract argumentation as abstractions of inferential relations. In *Proceedings ECAI 2014*





# Arguing about attack relations

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- Standards for determining defeat relations are often:
  - Domain-specific
  - Defeasible and conflicting
- So determining these standards is **argumentation!**
- Recently Modgil (AIJ 2009) has extended Dung's abstract approach
  - Arguments can also **attack attack relations**

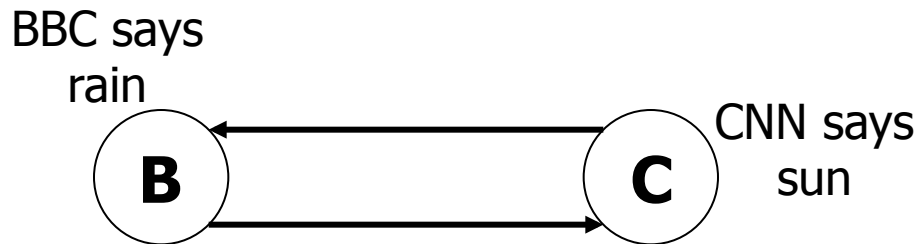




# Will it rain in Calcutta?

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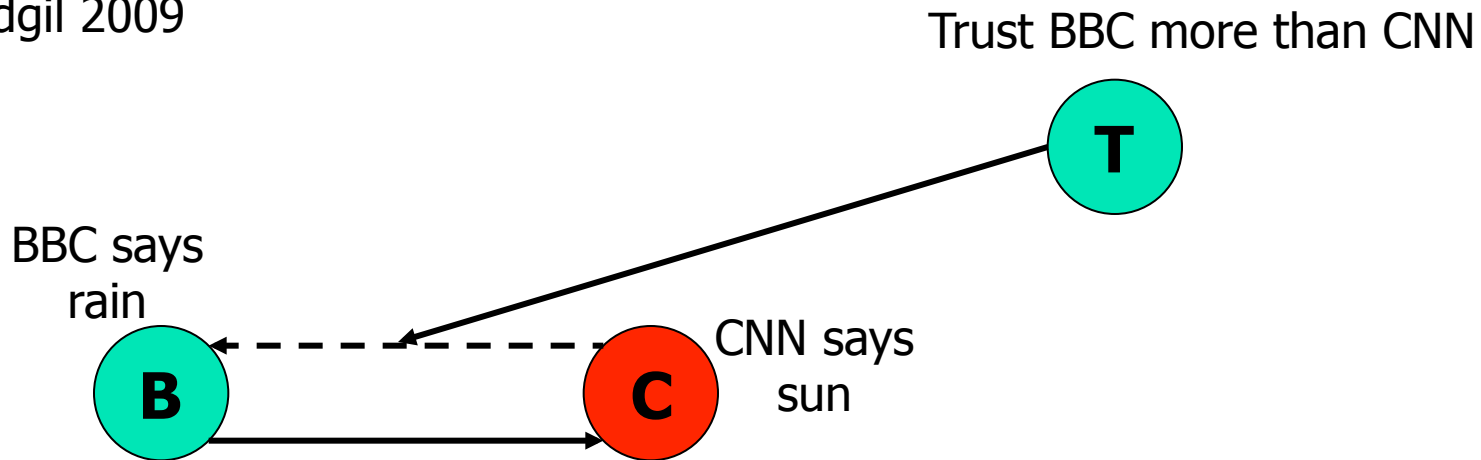
Modgil 2009





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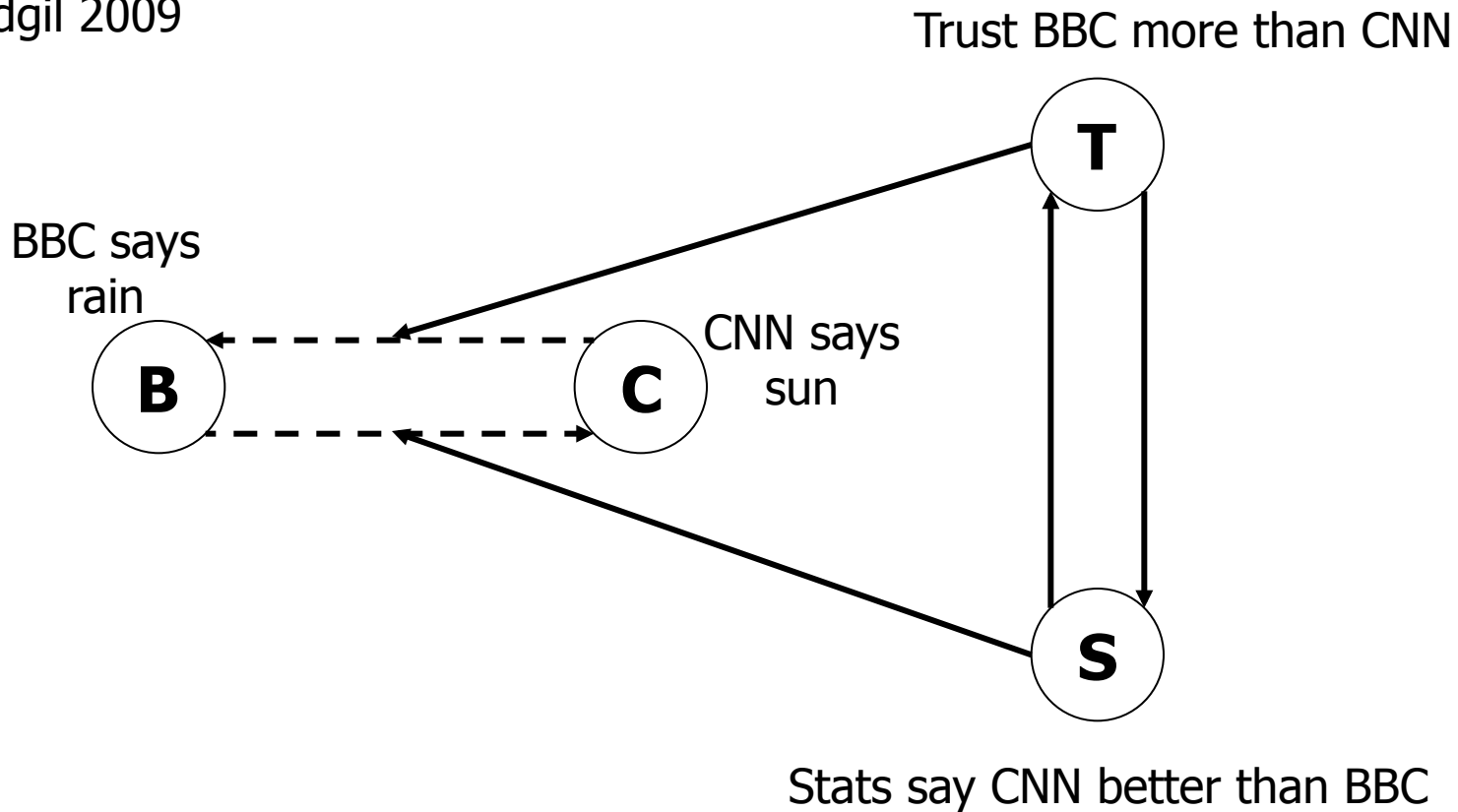
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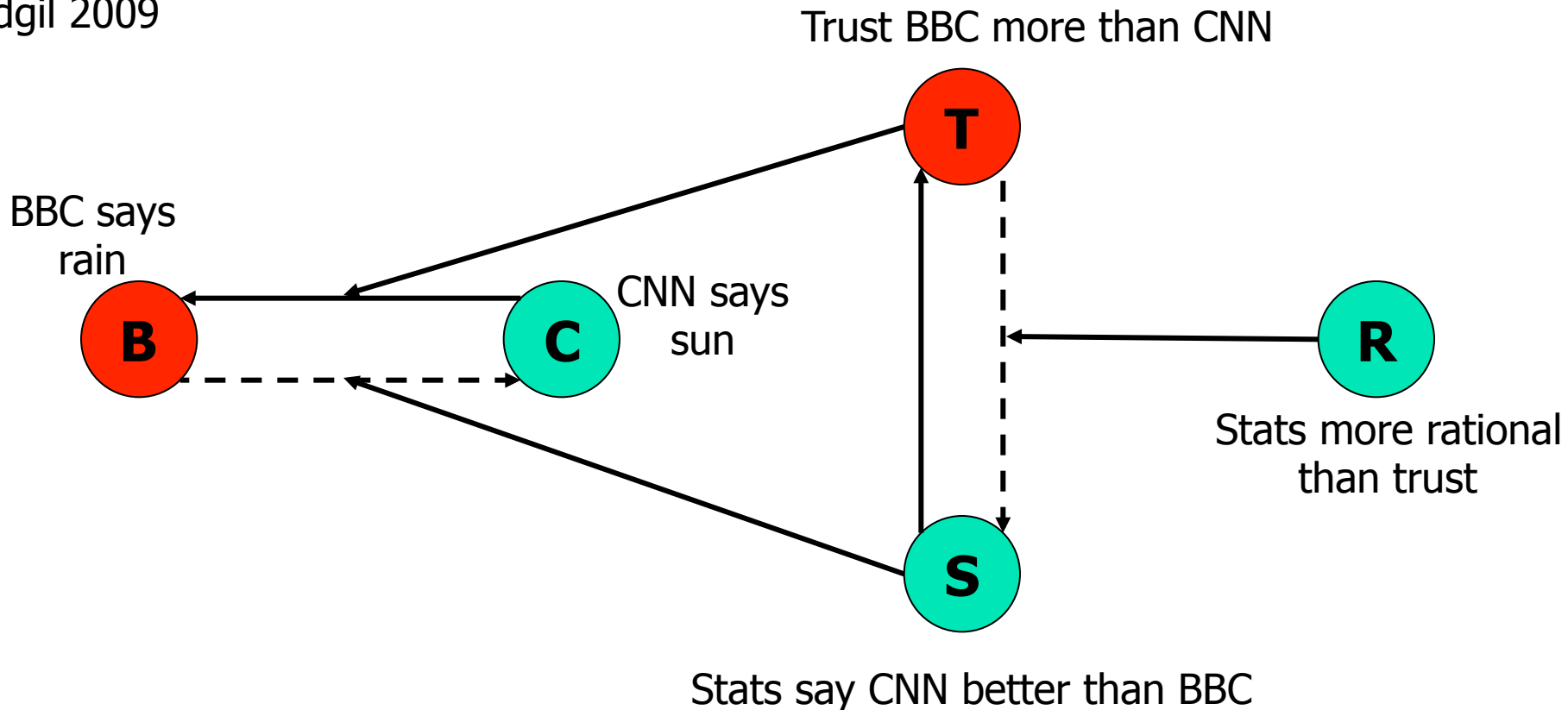
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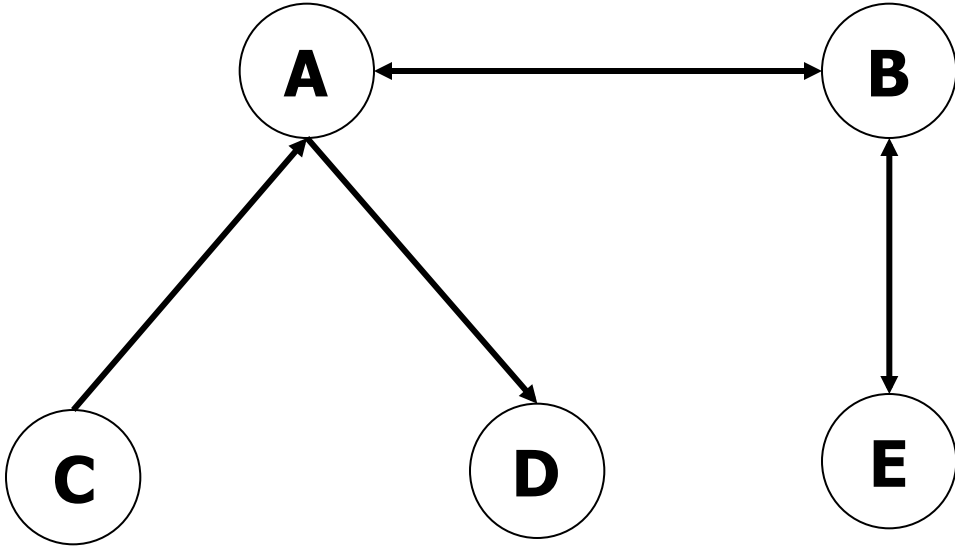
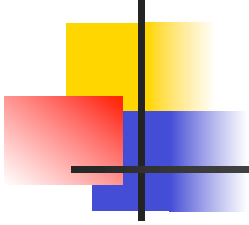


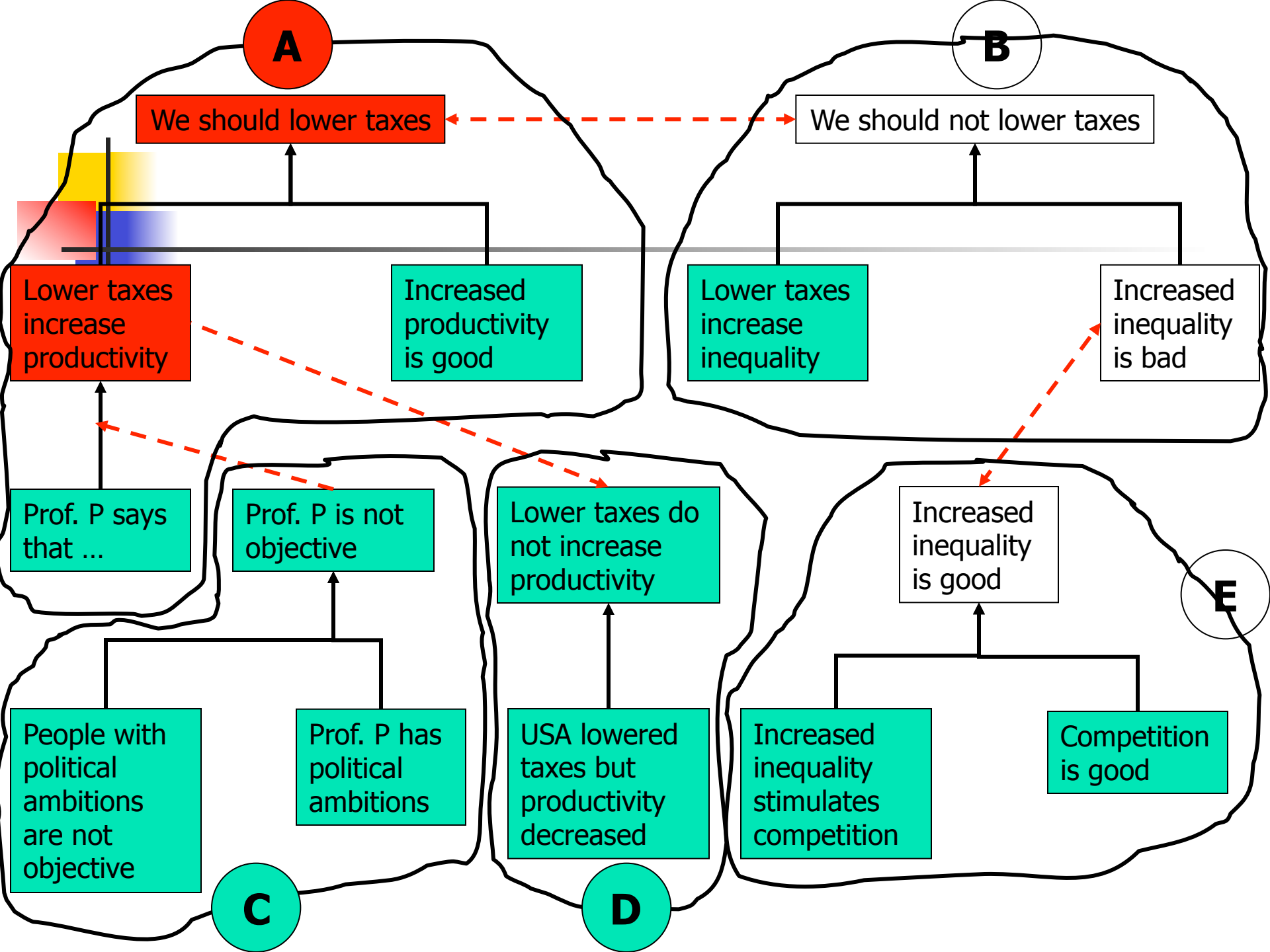


# Will it rain in Calcutta?

Modgil 2009









# The ultimate status of conclusions of arguments

---

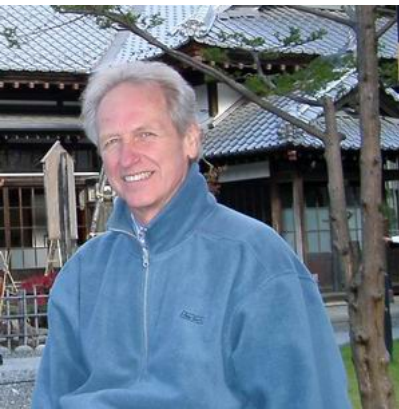
- Arguments:
  - A is **justified** if A is *In* in all labellings
  - A is **overruled** if A is *Out* in all labellings
  - A is **defensible** otherwise
- Conclusions:
  - $\phi$  is **justified** if  $\phi$  is the conclusion of some justified argument
  - $\phi$  is **defensible** if  $\phi$  is not justified and  $\phi$  is the conclusion of some defensible argument
  - $\phi$  is **overruled** if  $\phi$  is not justified or defensible and there exists an overruled argument for  $\phi$
- Justification is **nonmonotonic!**
  - Cn over  $\mathcal{L}$  is **monotonic** iff for all  $p \in \mathcal{L}$ ,  $S, S' \subseteq \mathcal{L}$ : If  $p \in \text{Cn}(S)$  and  $S \subseteq S'$  then  $p \in \text{Cn}(S')$



# Two accounts of the fallibility of arguments



- **Plausible Reasoning**: all fallibility located in the premises
  - Assumption-based argumentation (Kowalski, Dung, Toni, ...)
  - Classical argumentation (Cayrol, Besnard, Hunter, ...)
- **Defeasible reasoning**: all fallibility located in the inferences
  - Pollock, Loui, Vreeswijk, Prakken & Sartor, DeLP, ...
- ASPIC+ combines these accounts





# “Nonmonotonic” v. “Defeasible”

---

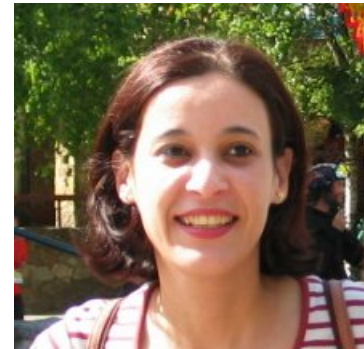
- Nonmonotonicity is a property of **consequence notions**
- Defeasibility is a property of **inference rules**
  - An inference rule is **defeasible** if there are situations in which its conclusion does not have to be accepted even though all its premises must be accepted.



# Rationality postulates for structured argumentation

---

- Extensions should be closed under subarguments
- Their conclusion sets should be:
  - Consistent
  - Closed under deductive inference





# The ‘base logic’ approach (Hunter, COMMA 2010)

---



- Adopt a **single** base logic
- Define **arguments** as **consequence** in the adopted base logic
- Then the **structure** of arguments is given by the base logic



# Classical argumentation (Besnard, Hunter, ...)

---

- Assume a possibly inconsistent KB in the **language of classical logic**
- Arguments are **classical proofs** from **consistent** (and subset-minimal) subsets of the KB
- Various notions of attack
- Possibly add preferences to determine which attacks result in defeat
  - E.g. Modgil & Prakken, AIJ-2013.
- Approach recently abstracted to **Tarskian abstract logics**
  - Amgoud & Besnard (2009-2013)



# Classical argumentation formalised

---

- Given  $\mathcal{L}$  a propositional logical language and  $\vdash$  standard-logical consequence over  $\mathcal{L}$ :
- An **argument** is a pair  $(S,p)$  such that
  - $S \subseteq \mathcal{L}$  and  $p \in \mathcal{L}$
  - $S \vdash p$
  - $S$  is consistent
  - No  $S' \subset S$  is such that  $S' \vdash p$
- Various notions of attack, e.g.:
  - “**Direct defeat**”: argument  $(S,p)$  **attacks** argument  $(S',p')$  iff  $p \vdash \neg q$  for some  $q \in S'$
  - “**Direct undercut**”: argument  $(S,p)$  **attacks** argument  $(S',p')$  iff  $p = \neg q$  for some  $q \in S'$
- Only these two attacks satisfy consistency, so classical argumentation is only optimal for **plausible reasoning**

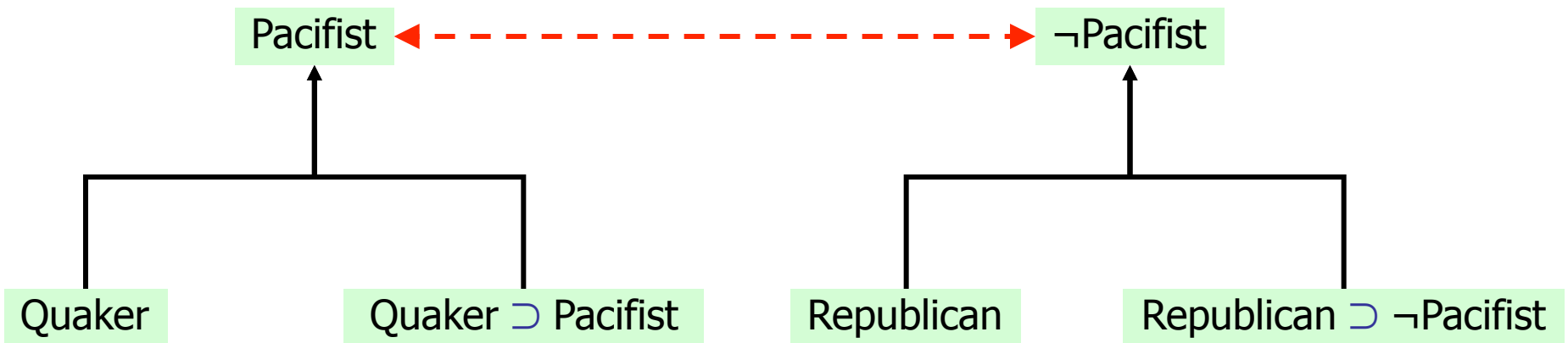
# Modelling default reasoning in classical argumentation

- Quakers are usually pacifist
- Republicans are usually not pacifist
- Nixon was a quaker and a republican



# A modelling in classical logic

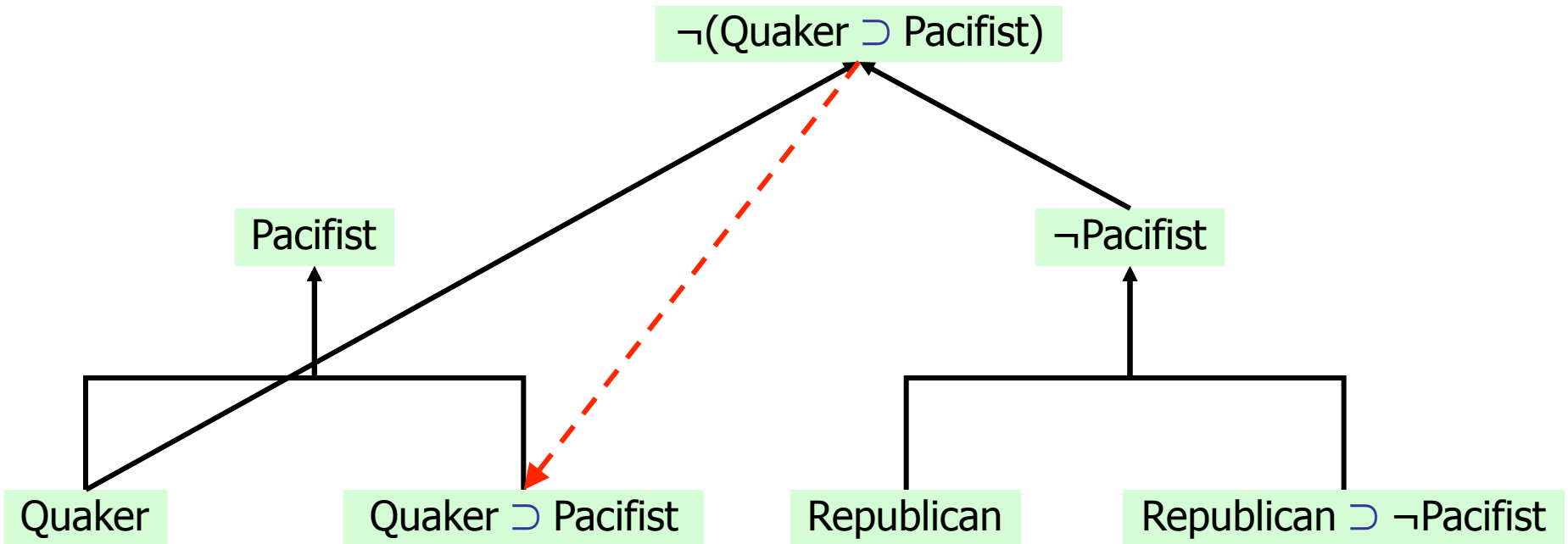
- Quaker  $\supset$  Pacifist
- Republican  $\supset \neg$ Pacifist
- Facts: Quaker, Republican





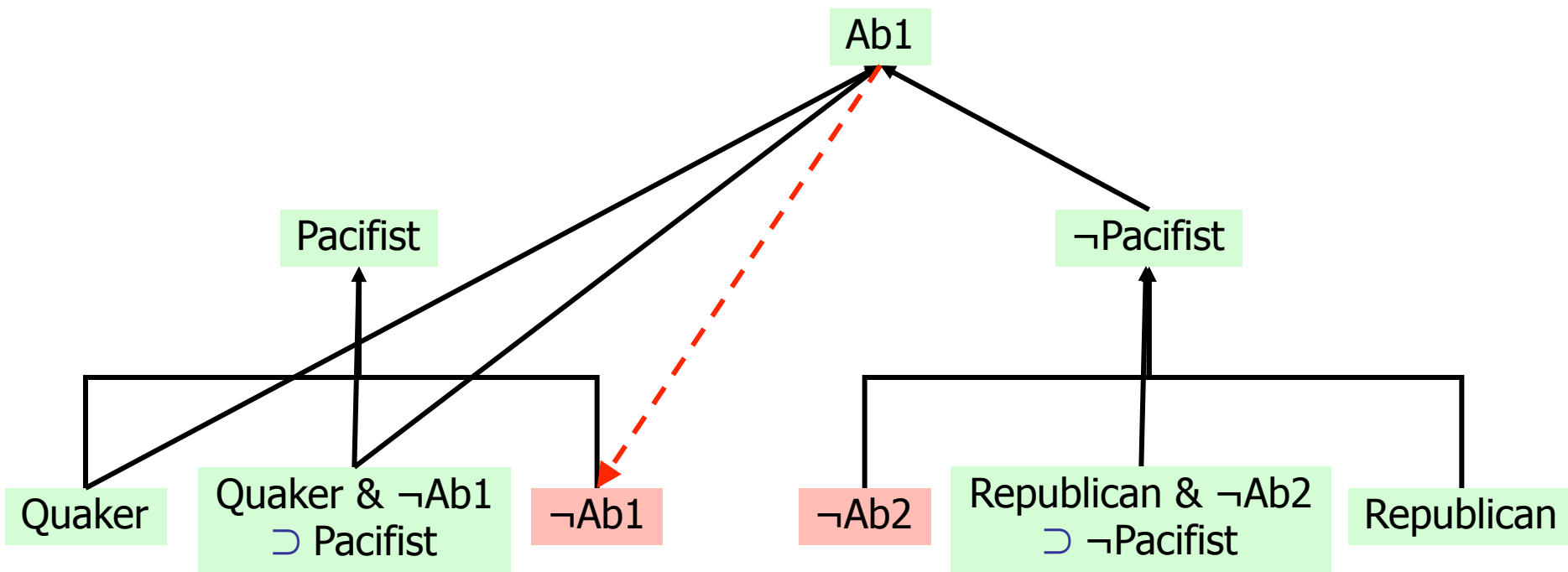
# A modelling in classical logic

- Quaker  $\supset$  Pacifist
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- Facts: Quaker, Republican



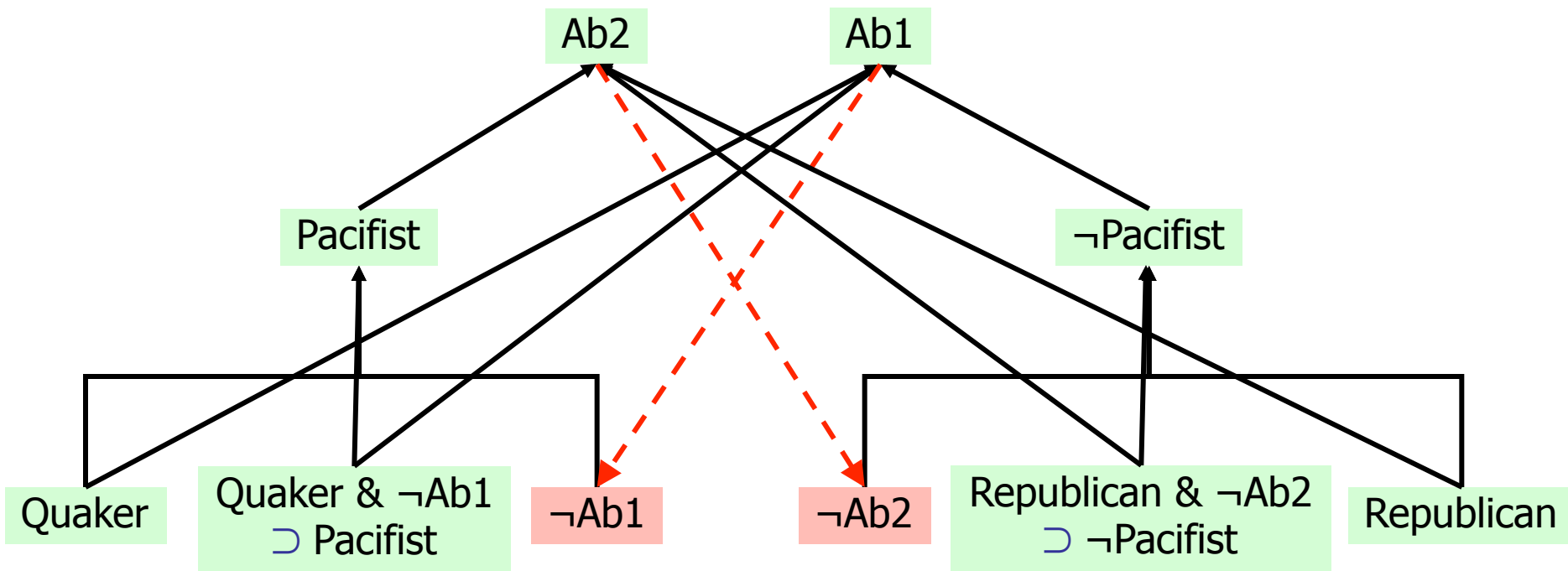
# A modelling in classical logic

- Quaker &  $\neg Ab1 \supset$  Pacifist
- Republican &  $\neg Ab2 \supset \rightarrow \neg Pacifist$
- Facts: Quaker, Republican
- **Assumptions:**  $\neg Ab1, \neg Ab2$  (attackable)



# A modelling in classical logic

- Quaker &  $\neg Ab1 \supset$  Pacifist
- Republican &  $\neg Ab2 \supset \rightarrow \neg$ Pacifist
- Facts: Quaker, Republican
- **Assumptions:**  $\neg Ab1, \neg Ab2$  (attackable)





# Extensions v. maximal consistent subsets

---

- With classical (and Tarskian) argumentation preferred and stable extensions and maximal conflict-free sets **coincide with maximal consistent subsets** of the knowledge base
  - Cayrol (1995)
  - Amgoud & Besnard (2013)
- If ‘real’ argumentation is more than identifying mcs, then deductive argumentation when combined with Dung **misses something**.
  - Modgil (& Prakken) 2013: with preferences they coincide with Brewka’s preferred subtheories
  - But is real argumentation identifying preferred subtheories?

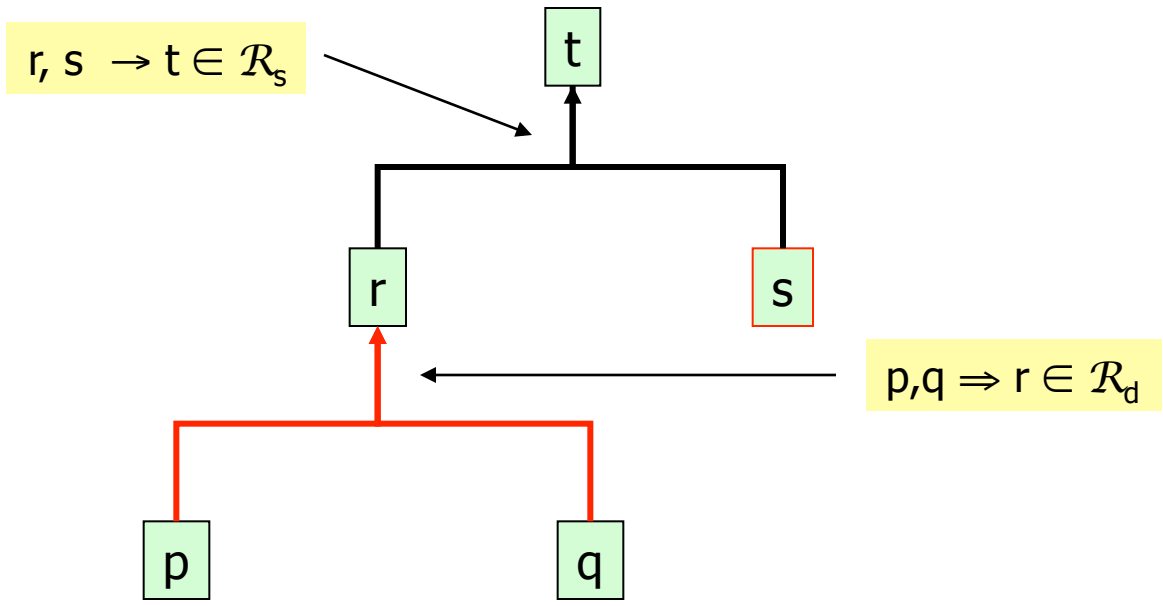
# The ASPIC+ framework



- **Arguments:** Trees where
  - Nodes are statements in some logical language  $\mathcal{L}$
  - Links are applications of inference rules
    - Strict rules  $\rightarrow$
    - Defeasible rules  $\Rightarrow$
- Constructed from a **knowledge base**  $\mathcal{K} \subseteq \mathcal{L}$ 
  - Axiom (necessary) premises + ordinary (contingent) premises
- **Attack:**
  - On ordinary premises
  - On defeasible inferences (undercutting)
  - On conclusions of defeasible inferences (rebutting)
- **Defeat:** attack + argument ordering
- **Argument evaluation** with Dung (1995)

$\mathcal{R}_s:$   $r, s \rightarrow t$   
 $\mathcal{R}_d:$   $p, q \Rightarrow r$

$\mathcal{K}_n = \{p, q\}$      $\mathcal{K}_p = \{s\}$



$\mathcal{R}_s:$   $r, s \rightarrow t$

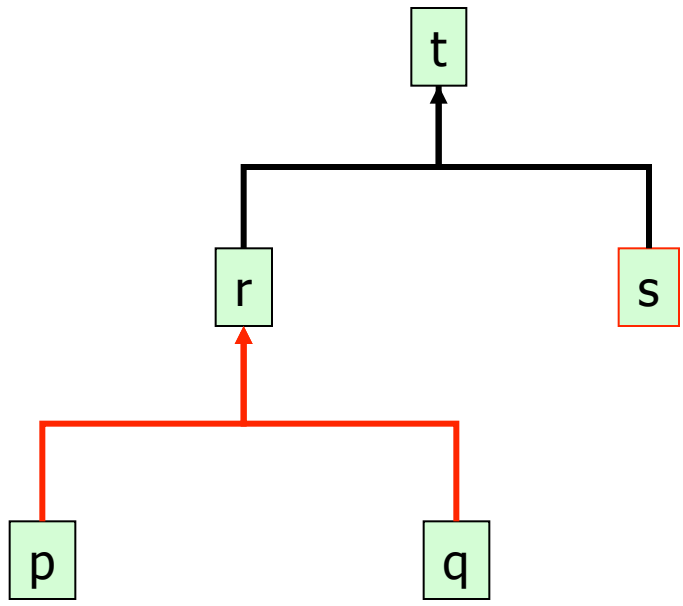
$\mathcal{R}_d:$   $p, q \Rightarrow r$

$\mathcal{K}_n = \{p, q\}$       $\mathcal{K}_p = \{s\}$

**Attack:**

- Undermining:** on ordinary premises
- Rebutting:** on defeasible inferences
- Undercutting:** on conclusions of defeasible inferences

$n(\phi_1, \dots, \phi_n \Rightarrow \phi) \in \mathcal{L}$



Attack + preferences = defeat





# Consistency in ASPIC+ (with symmetric negation)

---

- For any  $S \subseteq \mathcal{L}$ 
  - $S$  is (directly) **consistent** iff  $S$  does not contain two formulas  $\phi$  and  $-\phi$ .
  - ...





# Rationality postulates for ASPIC+

---

- Subargument closure always satisfied
- Consistency and strict closure:
  - **without** preferences satisfied if
    - $\mathcal{R}_s$  closed under transposition or closed under contraposition;  
and
    - $\mathcal{K}_n$  is indirectly consistent
  - **with** preferences satisfied if **in addition** the argument ordering is '**reasonable**'
    - Versions of the weakest- and last link ordering are reasonable
- So ASPIC+ is good for **both** plausible and defeasible reasoning



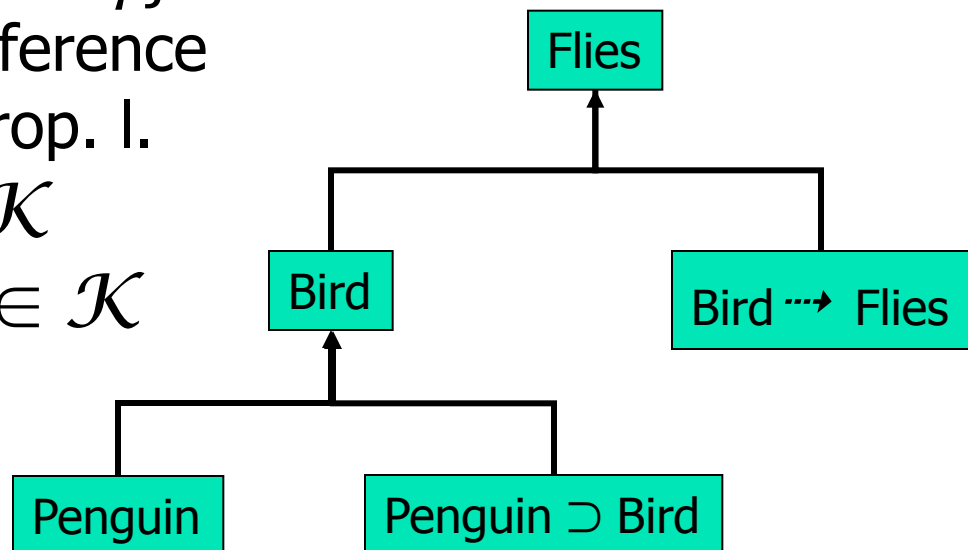
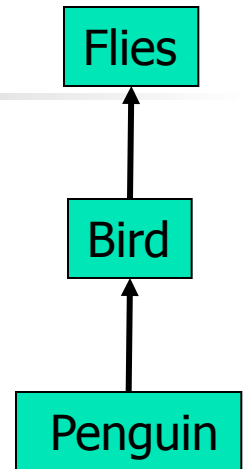
# Two uses of defeasible rules

---

- For **domain-specific** information
  - Defeasible generalisations, norms, ...
- For **general patterns** of presumptive reasoning
  - Pollock's defeasible reasons:
    - perception, memory, induction, statistical syllogism, temporal persistence
  - Argument schemes

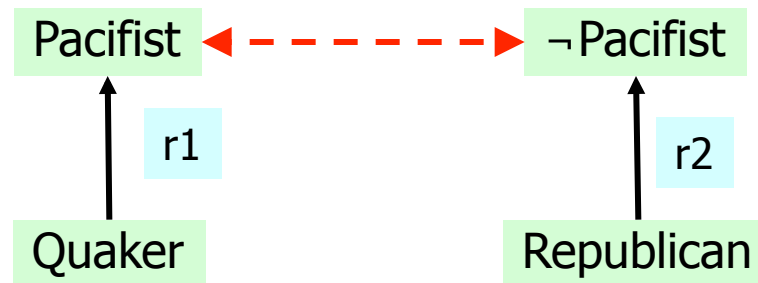
# Domain-specific vs. inference general inference rules

- d1: Bird  $\Rightarrow$  Flies
- s1: Penguin  $\rightarrow$  Bird
- Penguin  $\in \mathcal{K}$
  
- $\mathcal{R}_d = \{\phi, \phi \rightsquigarrow \psi \Rightarrow \psi\}$
- $\mathcal{R}_s =$  all valid inference rules of prop. 1.
  
- Bird  $\rightsquigarrow$  Flies  $\in \mathcal{K}$
- Penguin  $\supset$  Bird  $\in \mathcal{K}$
- Penguin  $\in \mathcal{K}$

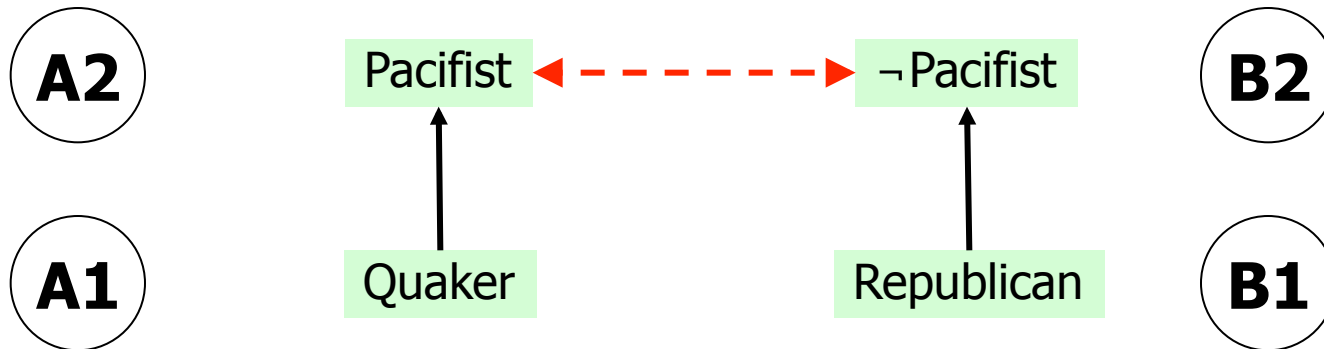


# Preferred extensions do not always coincide with mcs

- $r1: \text{Quaker} \Rightarrow \text{Pacifist}$
- $r2: \text{Republican} \Rightarrow \neg \text{Pacifist}$
- $S \rightarrow p \in \mathcal{R}_s$  iff  $S \models p$  in Prop. L and  $S$  is finite
- $\mathcal{K}: \text{Quaker}, \text{Republican}$



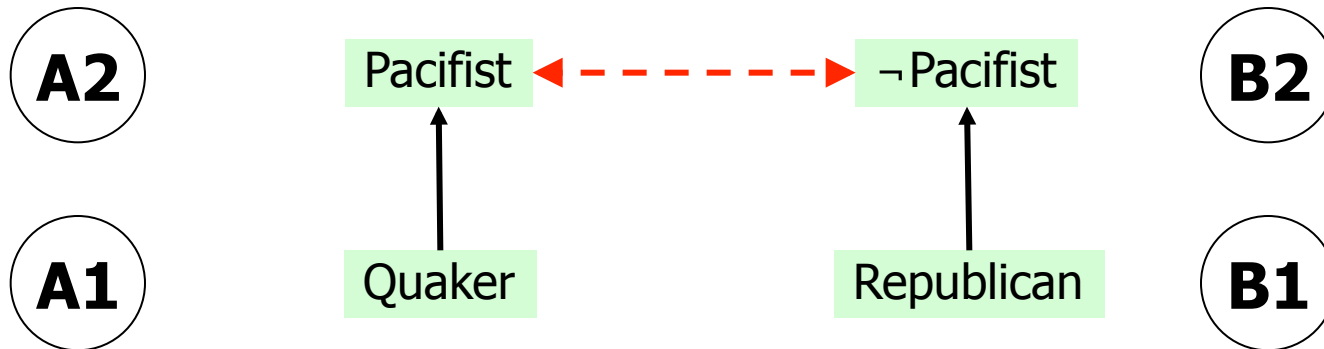
# Preferred/stable extensions do not always coincide with mcs



$$E1 = \{A1, A2, B1, \dots\}$$

$$E2 = \{A1, B1, B2, \dots\}$$

# Preferred/stable extensions do not always coincide with mcs



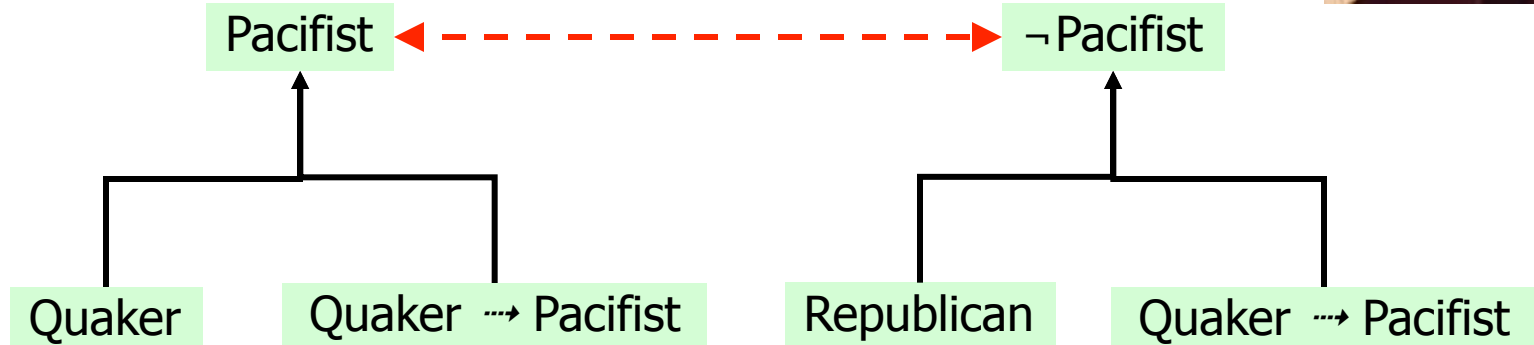
$\text{Conc}(E1) = \text{Th}(\{\text{Quaker}, \text{Republican}, \text{Pacifist}\})$

$\text{Conc}(E2) = \text{Th}(\{\text{Quaker}, \text{Republican}, \neg\text{Pacifist}\})$

$\text{mcs}(\mathcal{K}) = \{\{\mathcal{K}\}\} = \{\{\text{Quaker}, \text{Republican}\}\}$

# Preferred extensions do not always coincide with mcs

- $\mathcal{R}_d = \{\phi, \phi \rightsquigarrow \psi \Rightarrow \psi\}$
- $S \rightarrow p \in \mathcal{R}_s$  iff  $S \models p$  in Prop. L and  $S$  is finite
- $\mathcal{K}$ : Quaker, Republican,  
Quaker  $\rightsquigarrow$  Pacifist, Republican  $\rightsquigarrow$   $\neg$ Pacifist





# Can defeasible reasoning be reduced to plausible reasoning?

---

- To **classical** argumentation?
  - Problems with contrapositive inferences
- To **assumption-based** argumentation?
  - Problems with preferences
- In **both cases**:
  - less complex metatheory
  - but more complex representations





# Default contraposition in classical argumentation

---

- Men are usually not rapists
  - .
- John is a rapist
- Assume when possible that things are normal
- What can we conclude about John's sex?



# Default contraposition in classical argumentation

---

- Men are usually not rapists
  - $M \ \& \ \neg Ab \supset \neg R$
- John is a rapist ( $R$ )
- Assume when possible that things are normal
  - $\neg Ab$



# Default contraposition in classical argumentation

---

- Men are usually not rapists
  - $M \& \neg Ab \supset \neg R$
- John is a rapist ( $R$ )
- Assume when possible that things are normal
  - $\neg Ab$
- The first default implies that rapists are usually not men
  - $R \& \neg Ab \supset \neg M$
- So John is not a man



# Default contraposition in classical argumentation

---

- Heterosexual adults are usually not married  
=>
  - Non-married adults are usually not heterosexual
- This type of sensor usually does not give false alarms =>
  - False alarms are usually not given by this type of sensor

Statisticians call these inferences “**base rate fallacies**”

# Assumption-based argumentation (Dung, Mancarella & Toni 2007)

- A **deductive system** is a pair  $(\mathcal{L}, \mathcal{R})$  where
  - $\mathcal{L}$  is a logical language
  - $\mathcal{R}$  is a set of rules  $(\phi_1, \dots, \phi_n \rightarrow \phi)$  over  $\mathcal{L}$
- An **assumption-based argumentation framework** is a tuple  $(\mathcal{L}, \mathcal{R}, \mathcal{A}, \sim)$  where
  - $(\mathcal{L}, \mathcal{R})$  is a deductive system
  - $\mathcal{A} \subseteq \mathcal{L}$ ,  $\mathcal{A} \neq \emptyset$ , a set of **assumptions**
  - No rule has an assumption as conclusion
  - $\sim$  is a total mapping from  $\text{Pow}(\mathcal{L})$  into  $\mathcal{L}$ .  $\sim a$  is the **contrary** of  $a$ .
- An **argument**  $S \vdash p$  is a deduction of  $p$  from a set  $S \subseteq \mathcal{A}$ .
- Argument  $S \vdash p$  **attacks** argument  $S' \vdash p'$  iff  $p = \sim q$  for some  $q \in S'$

# Reduction of ASPIC+ defeasible rules to ABA rules (Dung & Thang, JAIR 2014)

- Assumptions:
  - $\mathcal{L}$  consists of literals
  - No preferences
  - No rebuttals of undercutters

1-1 correspondence  
between complete  
extensions of ASPIC+  
and ABA

$$p_1, \dots, p_n \Rightarrow q$$

becomes

$$d_i, p_1, \dots, p_n, \text{not}\neg q \rightarrow q$$

where:

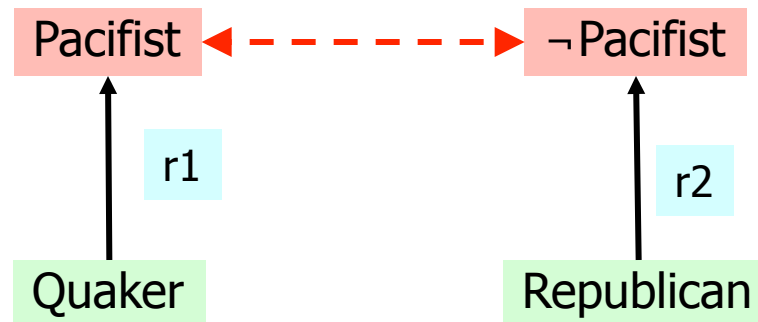
$$d_i = n(p_1, \dots, p_n \Rightarrow q)$$

$d_i, \text{not}\neg q$  are assumptions

$$\phi = \sim \text{not}\phi, \phi = \sim \neg\phi, \neg\phi = \sim\phi$$

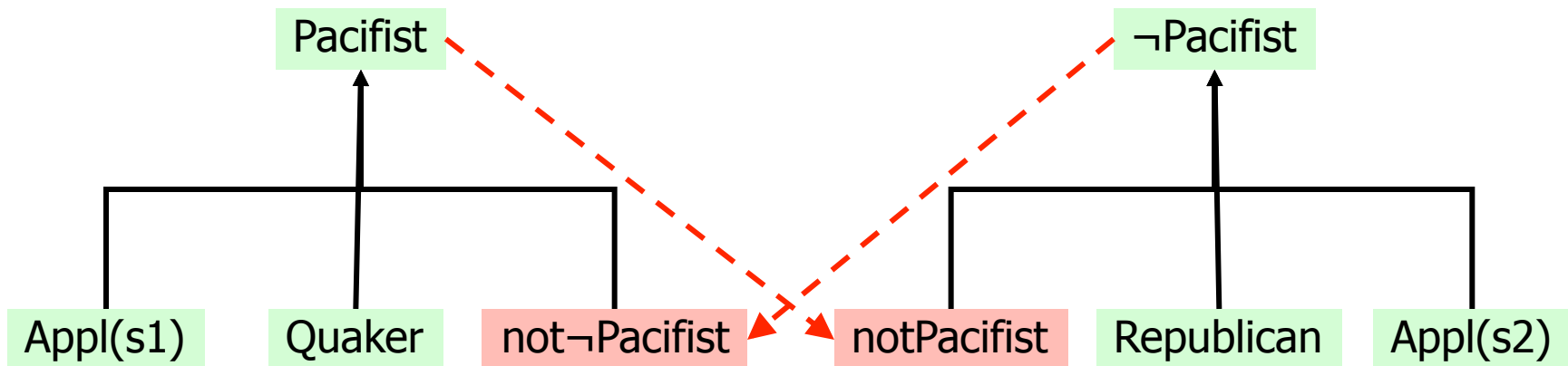
# From defeasible to strict rules: example

- r1: Quaker  $\Rightarrow$  Pacifist
- r2: Republican  $\Rightarrow$   $\neg$ Pacifist



# From defeasible to strict rules: example

- $s1: \text{Appl}(s1), \text{Quaker}, \text{not}\neg\text{Pacifist} \rightarrow \text{Pacifist}$
- $s2: \text{Appl}(s2), \text{Republican}, \text{notPacifist} \rightarrow \neg\text{Pacifist}$







# Can ASPIC+ preferences be reduced to ABA assumptions?

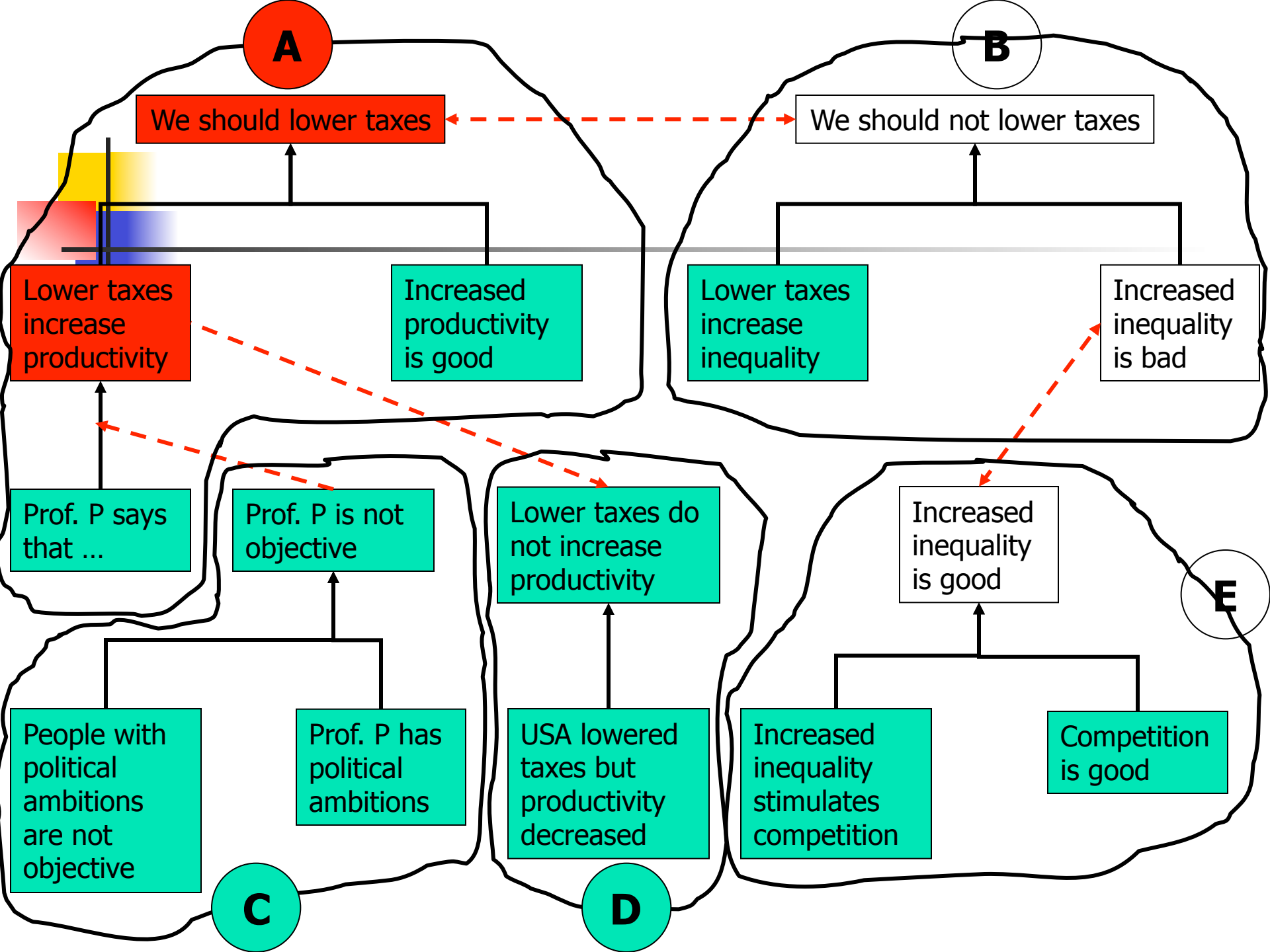
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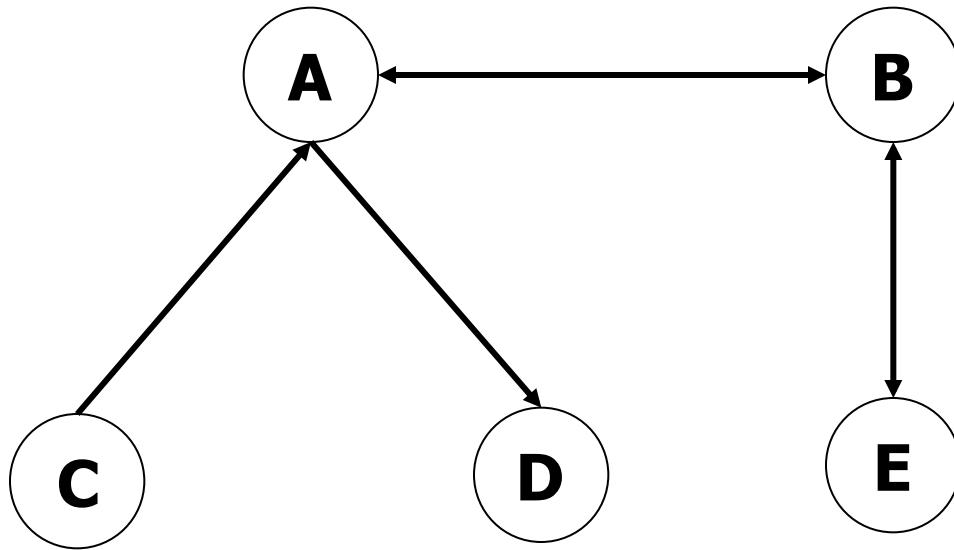
d1: Bird  $\Rightarrow$  Flies  
d2: Penguin  $\Rightarrow \neg$ Flies  
d1 < d2

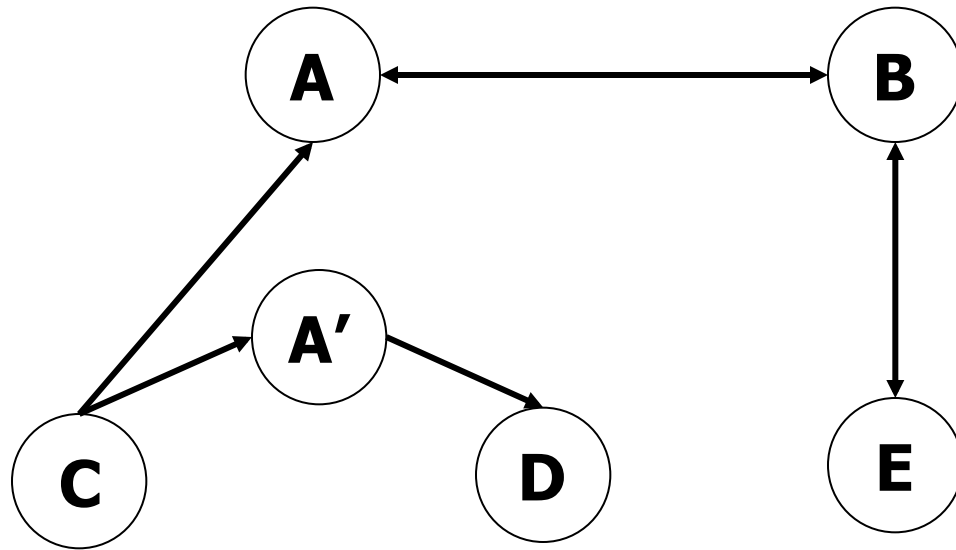
Becomes

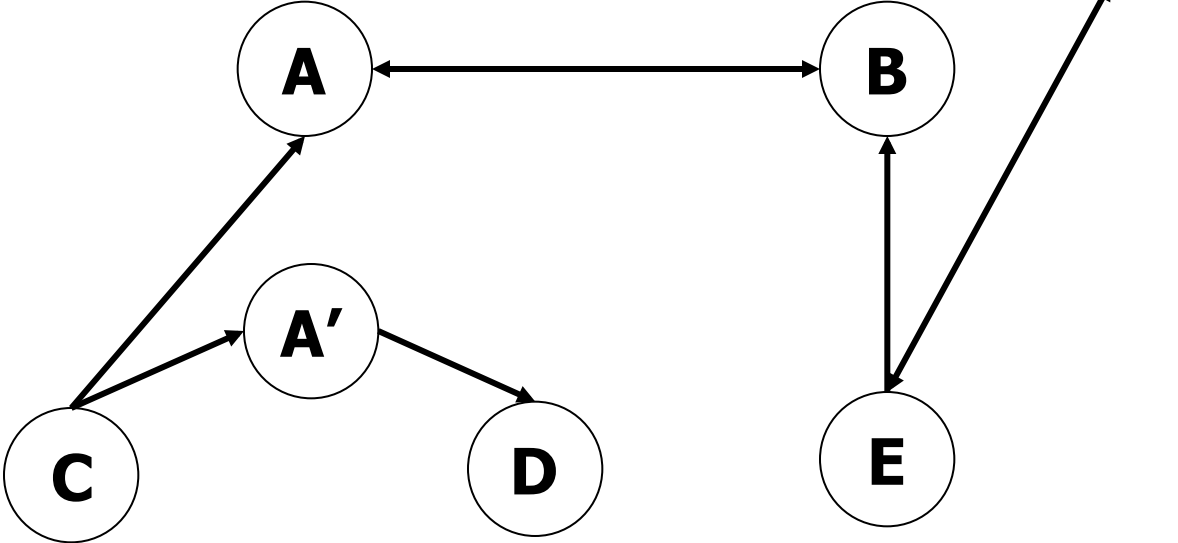
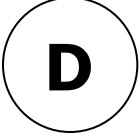
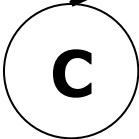
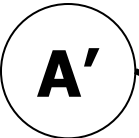
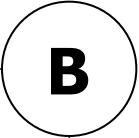
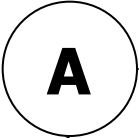
d1: Bird, notPenguin  $\Rightarrow$  Flies  
d2: Penguin  $\Rightarrow \neg$ Flies

Only works in special cases, e.g.  
not with weakest-link ordering











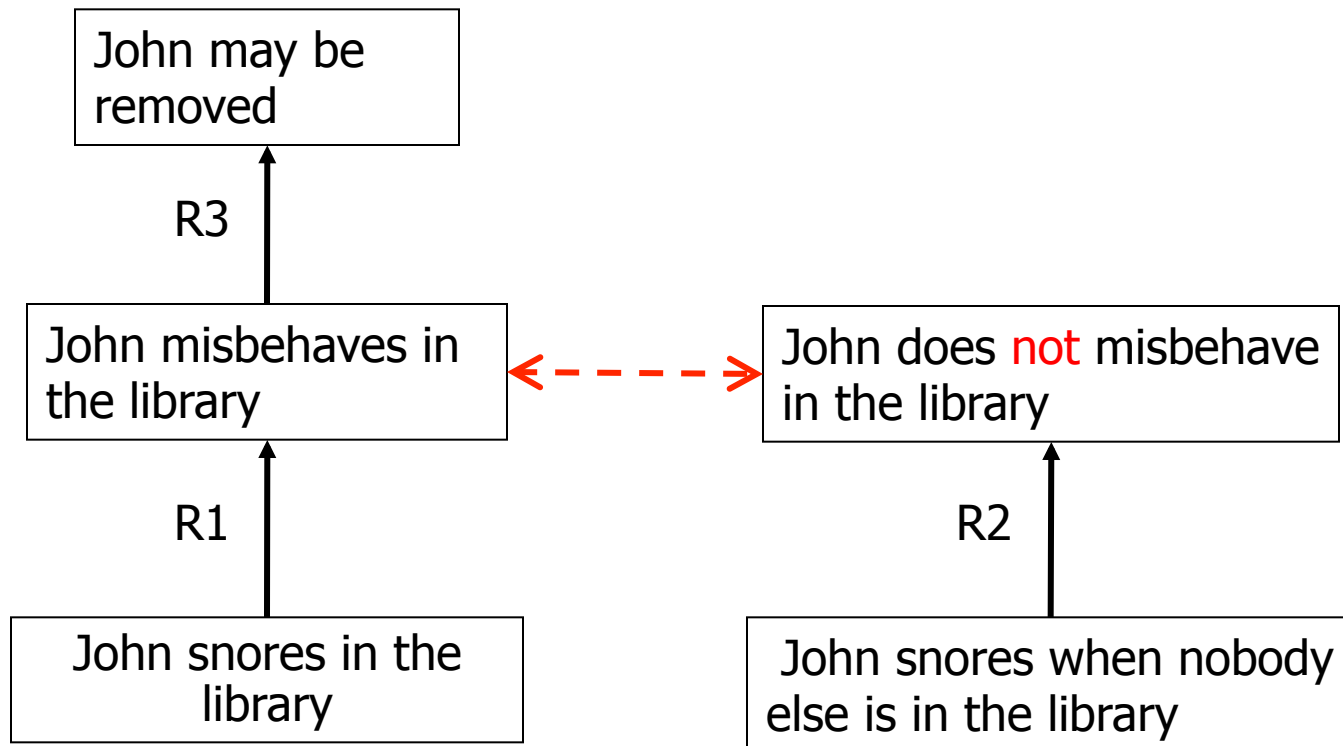
# Preferences in abstract argumentation

---

- PAFs: extend  $(args, attack)$  to  $(args, attack, \leq_a)$ 
  - $\leq_a$  is an ordering on args
  - A *defeats* B iff A attacks B and not  $A < B$
  - Apply Dung's theory to  $(args, defeat)$
- **Implicitly assumes that:**
  - All attacks are preference-dependent
  - All attacks are independent from each other
- Assumptions **not satisfied in general**  $\Rightarrow$ 
  - Properties not inherited by all instantiations
  - possibly violation of rationality postulates

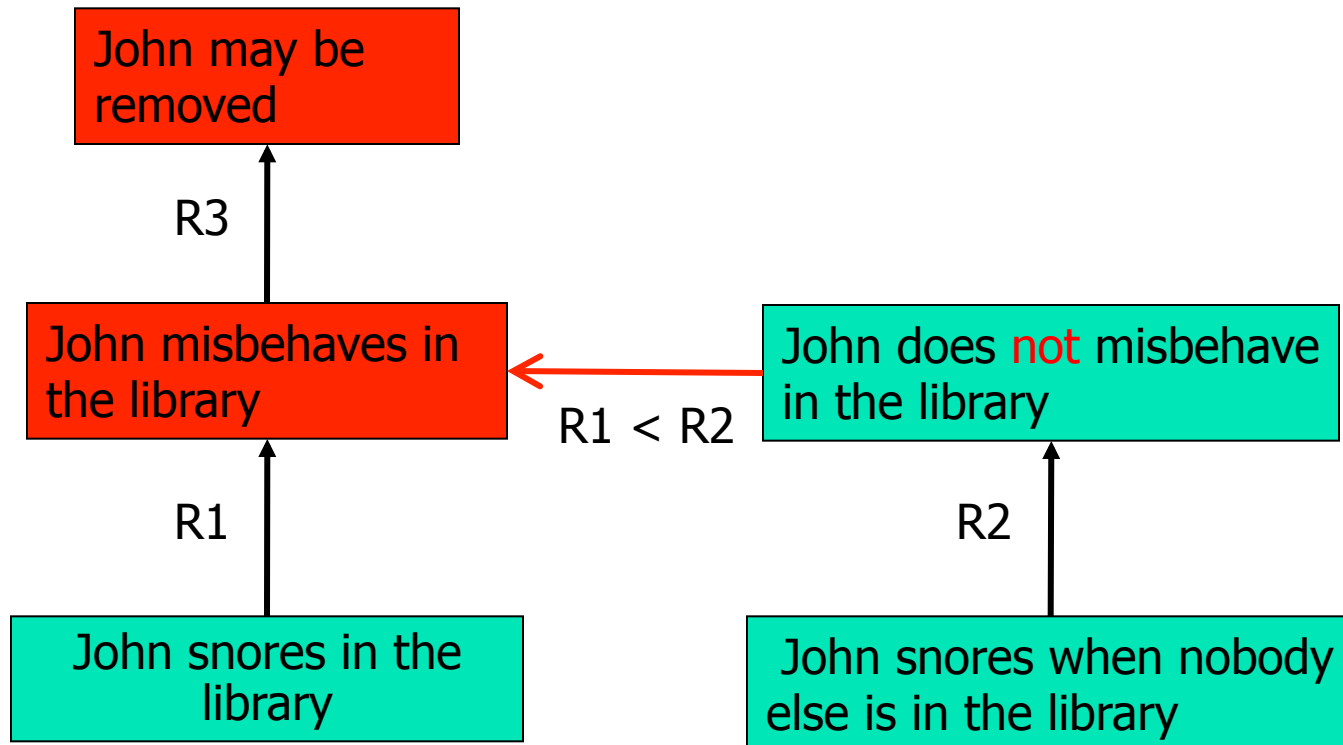
R1: If you snore, you misbehave  
R2: If you snore when nobody else is around, you don't misbehave  
R3: If you misbehave in the library, the librarian may remove you

R1 < R2 < R3



R1: If you snore, you misbehave  
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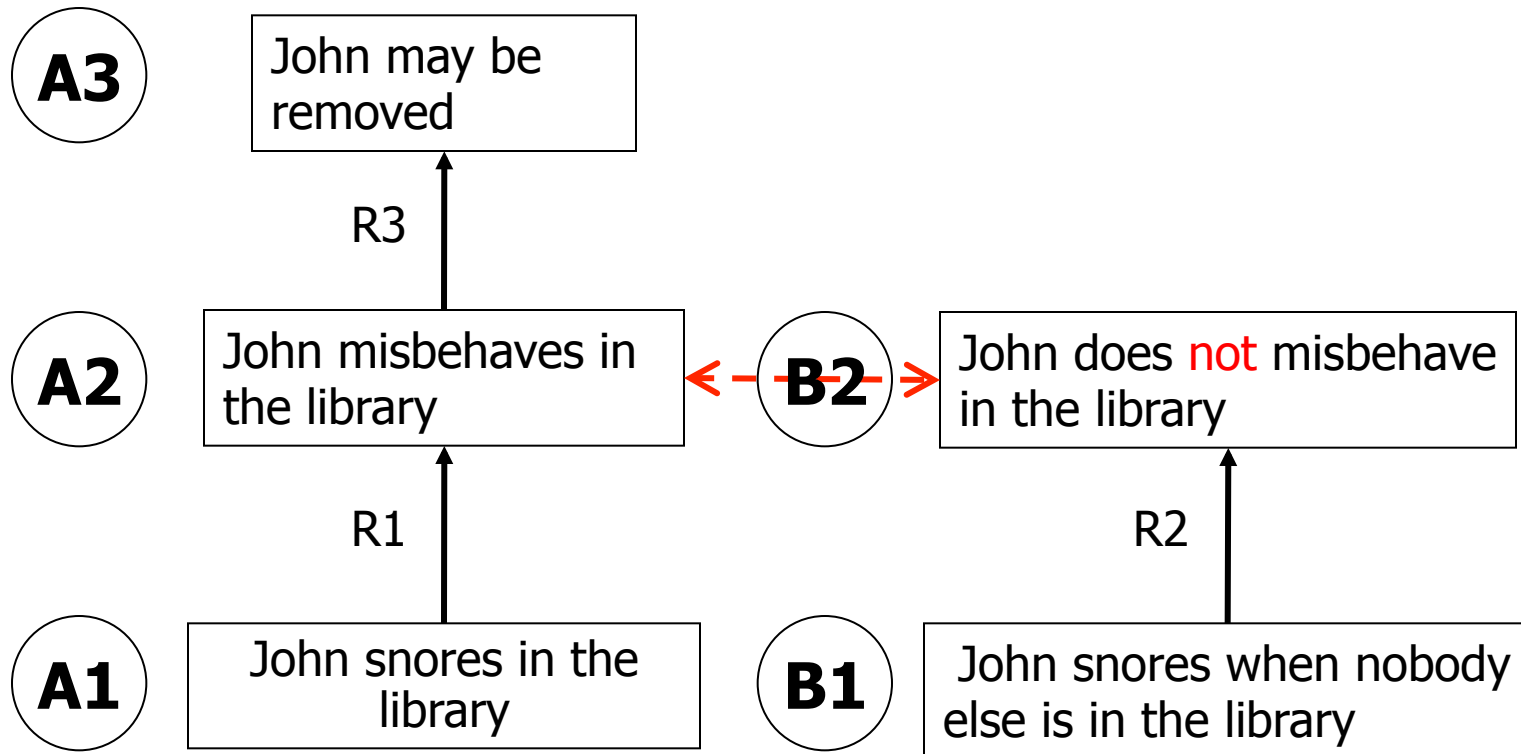
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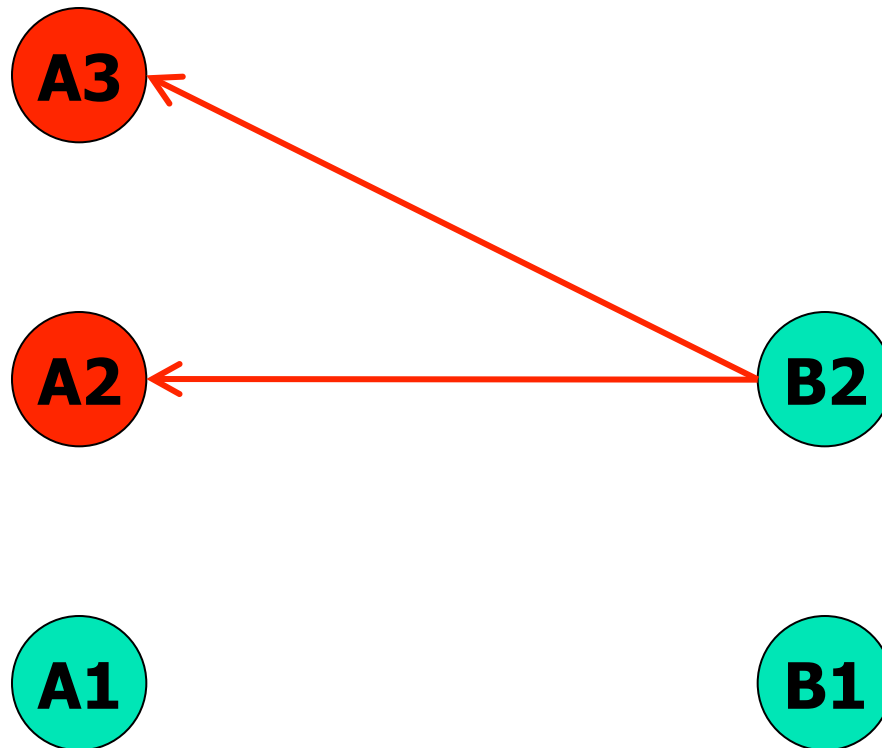
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R1 < R2 < R3

so A2 < B2 < A3 (with last link)

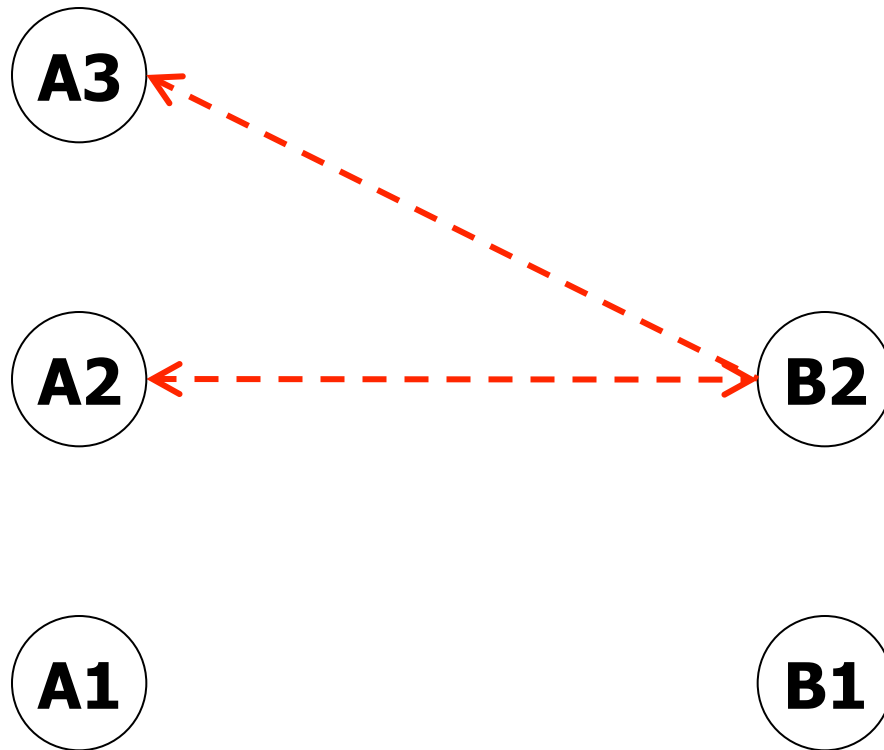


The defeat graph  
in ASPIC+

R1: If you snore, you misbehave  
R2: If you snore when nobody else is around, you don't misbehave  
R3: If you misbehave in the library, the librarian may remove you

R1 < R2 < R3

so A2 < B2 < A3 (with last link)



The attack graph  
in PAFs

R1: If you snore, you misbehave  
R2: If you snore when nobody else is around, you don't misbehave  
R3: If you misbehave in the library, the librarian may remove you

R1 < R2 < R3

so A2 < B2 < A3 (with last link)

A3

A2

A1

B2

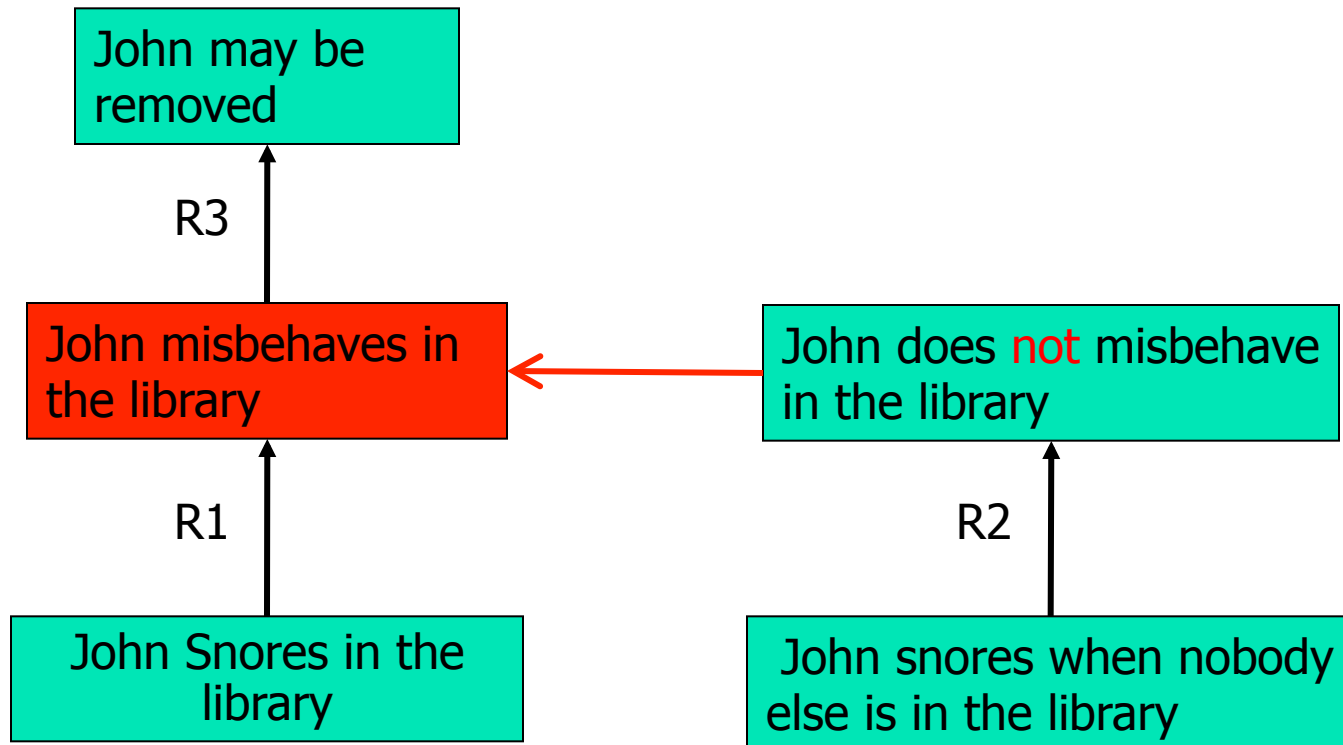
B1

The defeat graph  
in PAFs

R1: If you snore, you misbehave  
R2: If you snore when nobody else is around, you don't misbehave  
R3: If you misbehave in the library, the librarian may remove you

R1 < R2 < R3

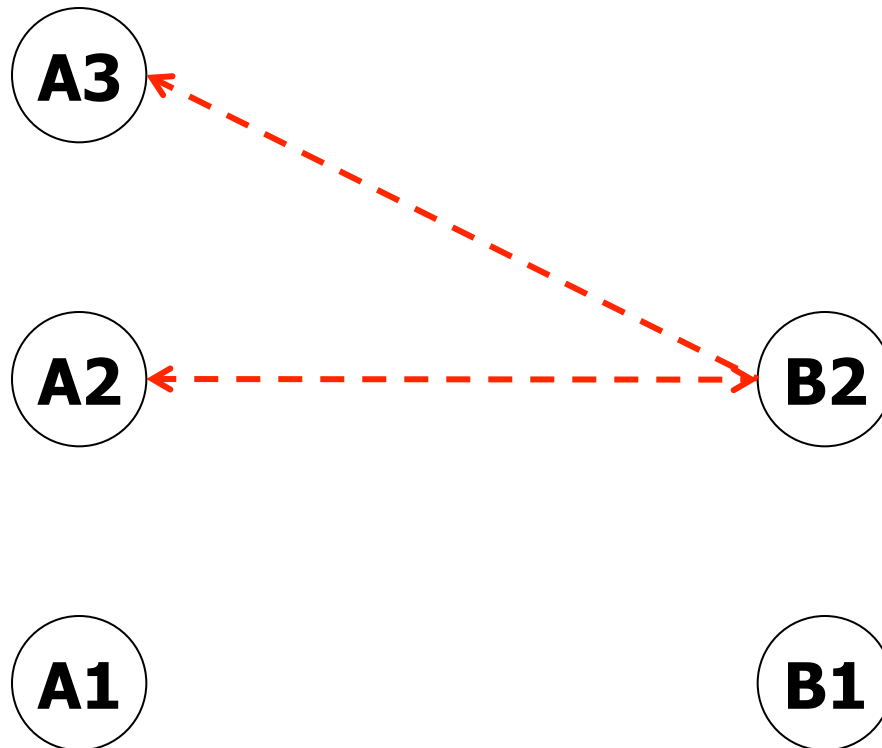
so A2 < B2 < A3 (with last link)



R1: If you snore, you misbehave  
R2: If you snore when nobody else is around, you don't misbehave  
R3: If you misbehave in the library, the librarian may remove you

R1 < R2 < R3

so A2 < B2 < A3 (with last link)



PAFs don't recognize that  
B2's attacks on  
A2 and A3 are the same

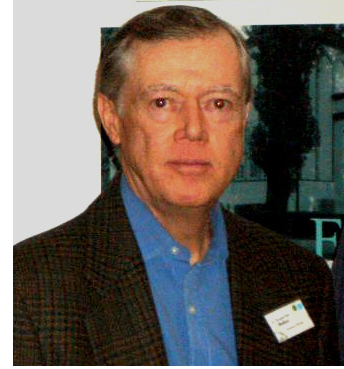


# Work outside the Dung paradigm

---

- Defeasible Logic Programming (Simari et al.)
  - Arguments roughly as in ASPIC+ but no Dung semantics
- Carneades (Gordon et al.)
  - Arguments pro and con a claim
- Abstract Dialectical Frameworks (Brewka & Woltran)
- ...

# Argument(ation) schemes: general form



Premise 1,

... ,

Premise n

Therefore (presumably), conclusion

- But also **critical questions**





# Argument schemes in ASPIC

---

- Argument schemes are **defeasible inference rules**
- Critical questions are **pointers to counterarguments**
  - Some point to **undermining** attacks
  - Some point to **rebutting** attacks
  - Some point to **undercutting** attacks



# Reasoning with default generalisations

---

P  
If P then normally/usually/typically Q  
So (presumably), Q

- What experts say is usually true
  - People with political ambitions are usually not objective about security
  - People with names typical from country C usually have nationality C
  - People who flea from a crime scene when the police arrives are normally involved in the crime
  - Chinese people usually don't like coffee
- 
- But defaults can have **exceptions**
  - And there can be **conflicting** defaults



# Perception

---

P is observed

Therefore (presumably), P

- **Critical questions:**
  - Are the observer's senses OK?
  - Are the circumstances such that reliable observation of P is impossible?
  - ...



# Inducing generalisations

---

Almost all observed P's were Q's  
Therefore (presumably), If P then usually Q

A ballpoint shot with this type of bow will usually cause this type of eye injury

In 16 of 17 tests the ballpoint shot with this bow caused this type of eye injury

- Critical questions:
  - Is the **size** of the sample large enough?
  - was the sample selection **biased**?

# Expert testimony (Walton 1996)



E is expert on D

E says that P

P is within D

Therefore (presumably), P is the case

- **Critical questions:**
  - Is E biased?
  - Is P consistent with what other experts say?
  - Is P consistent with known evidence?

# Supporting and using generalisations

Defeasible  
modus ponens

V's injury was caused by a fall

This type of eye injury is  
usually caused by a fall

V has this type of injury

Expert  
testimony  
scheme

E says that his type of injury  
is usually caused by a fall

E is an expert on  
this type of injury



# Arguments from consequences

---

Action A causes G,

G is good (bad)

Therefore (presumably), A should (not) be done

- Critical questions:
  - Does A also have bad (good) consequences?
  - Are there other ways to bring about G?
  - ...



# Combining multiple good/bad consequences

---

Action A results in C1

...

Action A results in Cn

C1 is good

...

Cn is good

**Therefore,**

Action A is good

Action A results in C1

...

Action A results in Cn

C1 is bad

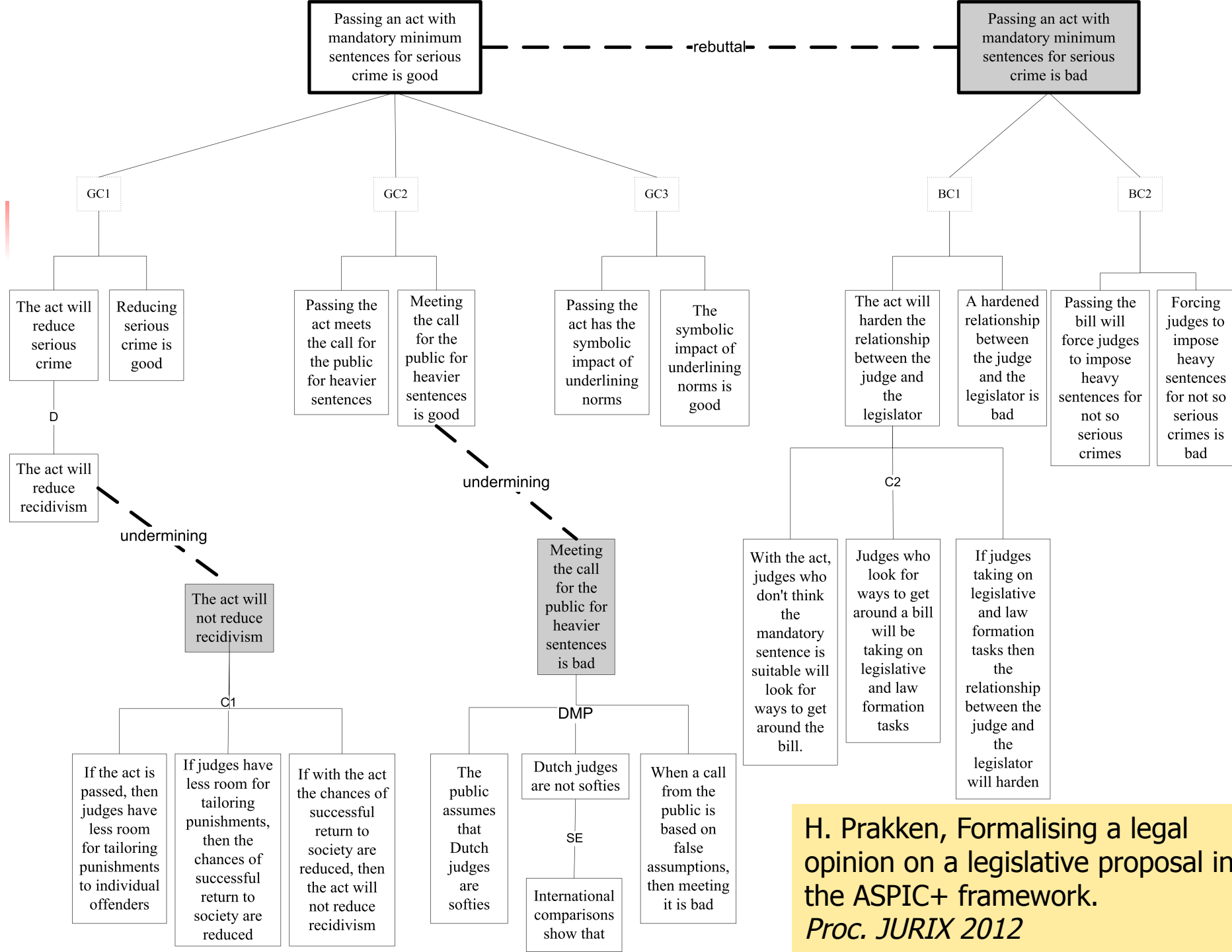
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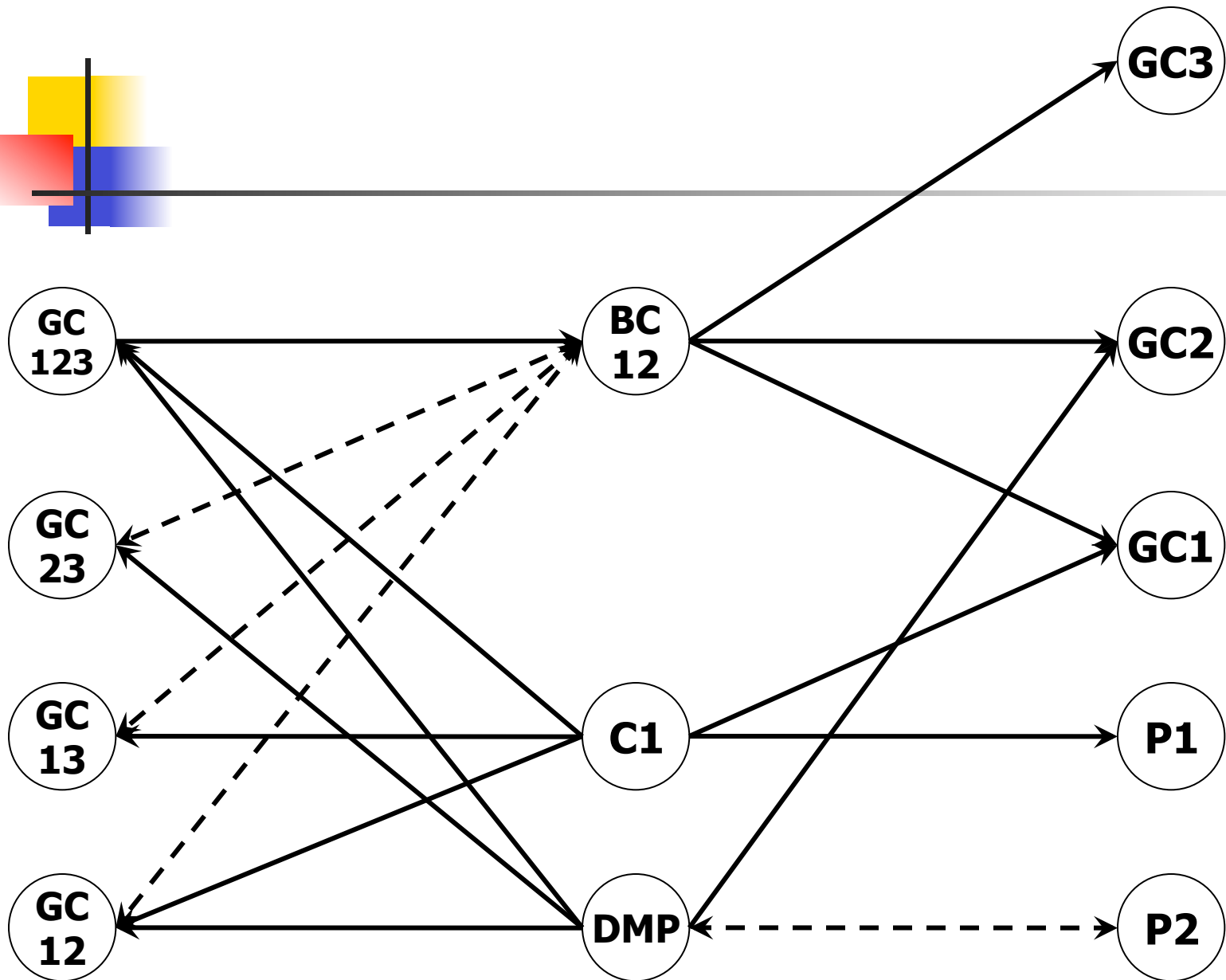
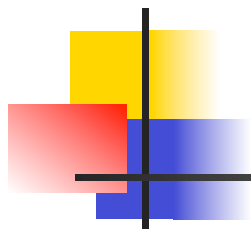
Cm is bad

**Therefore,**

Action A is bad

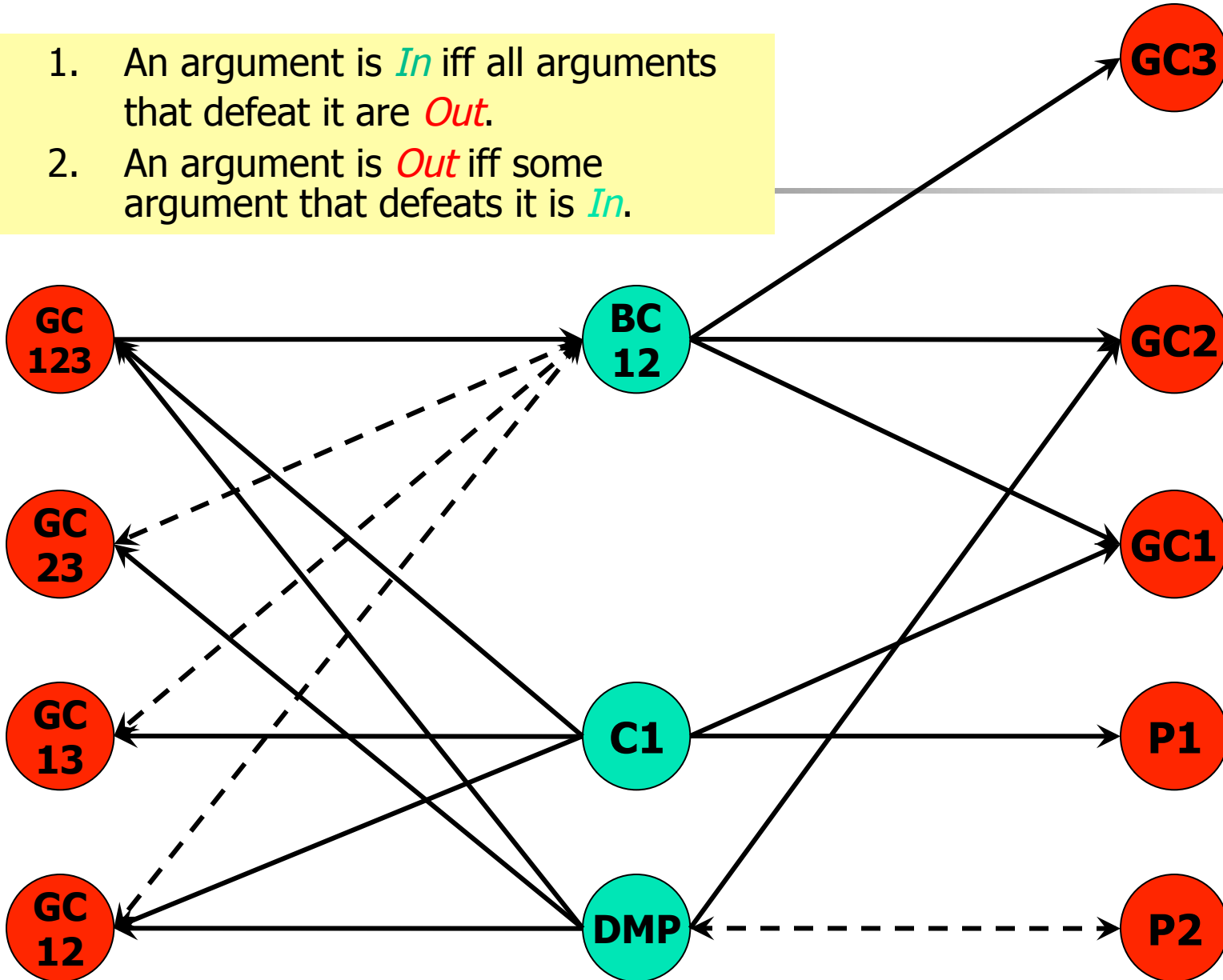






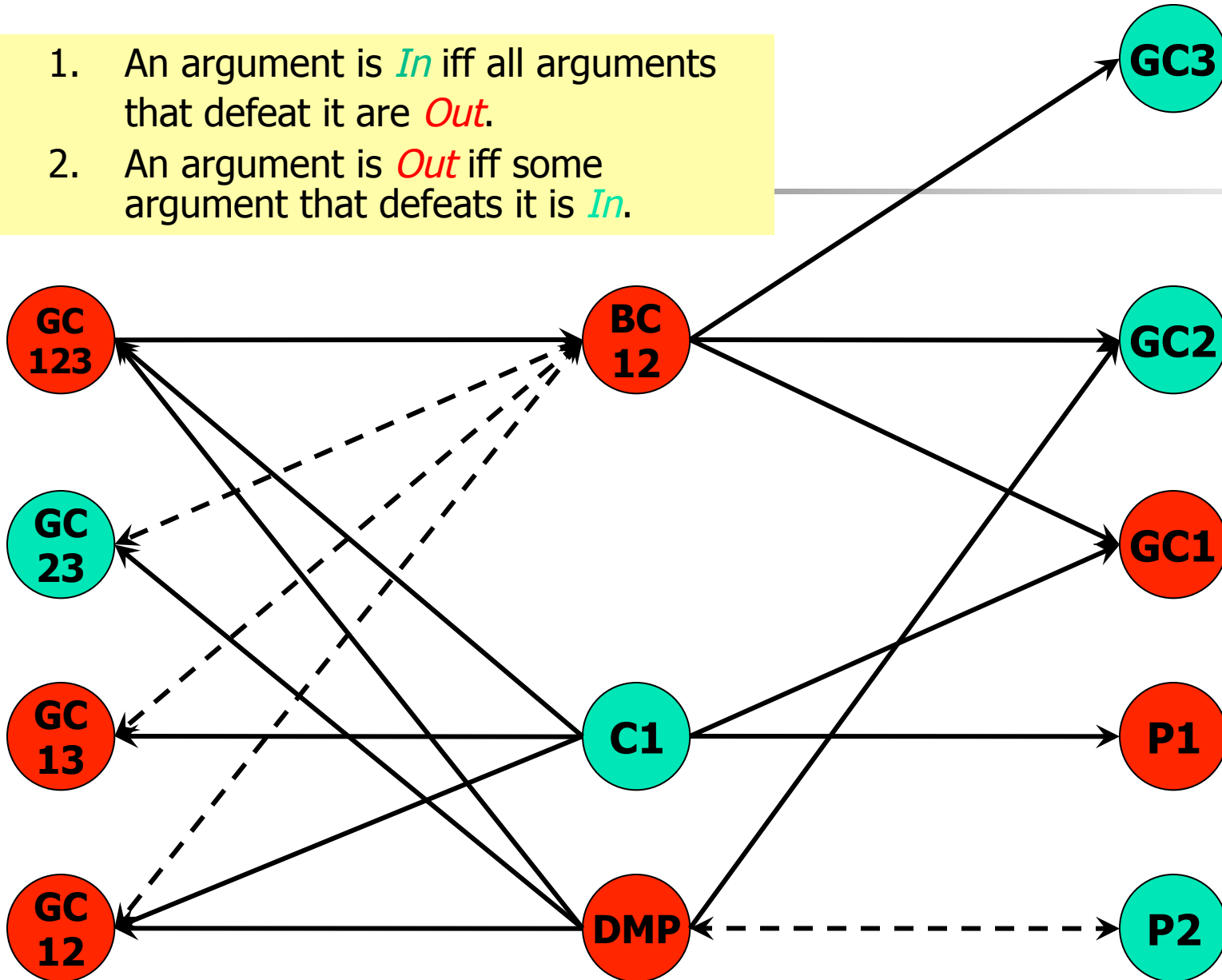
# Preferred labelling 1

1. An argument is *In* iff all arguments that defeat it are *Out*.
2. An argument is *Out* iff some argument that defeats it is *In*.



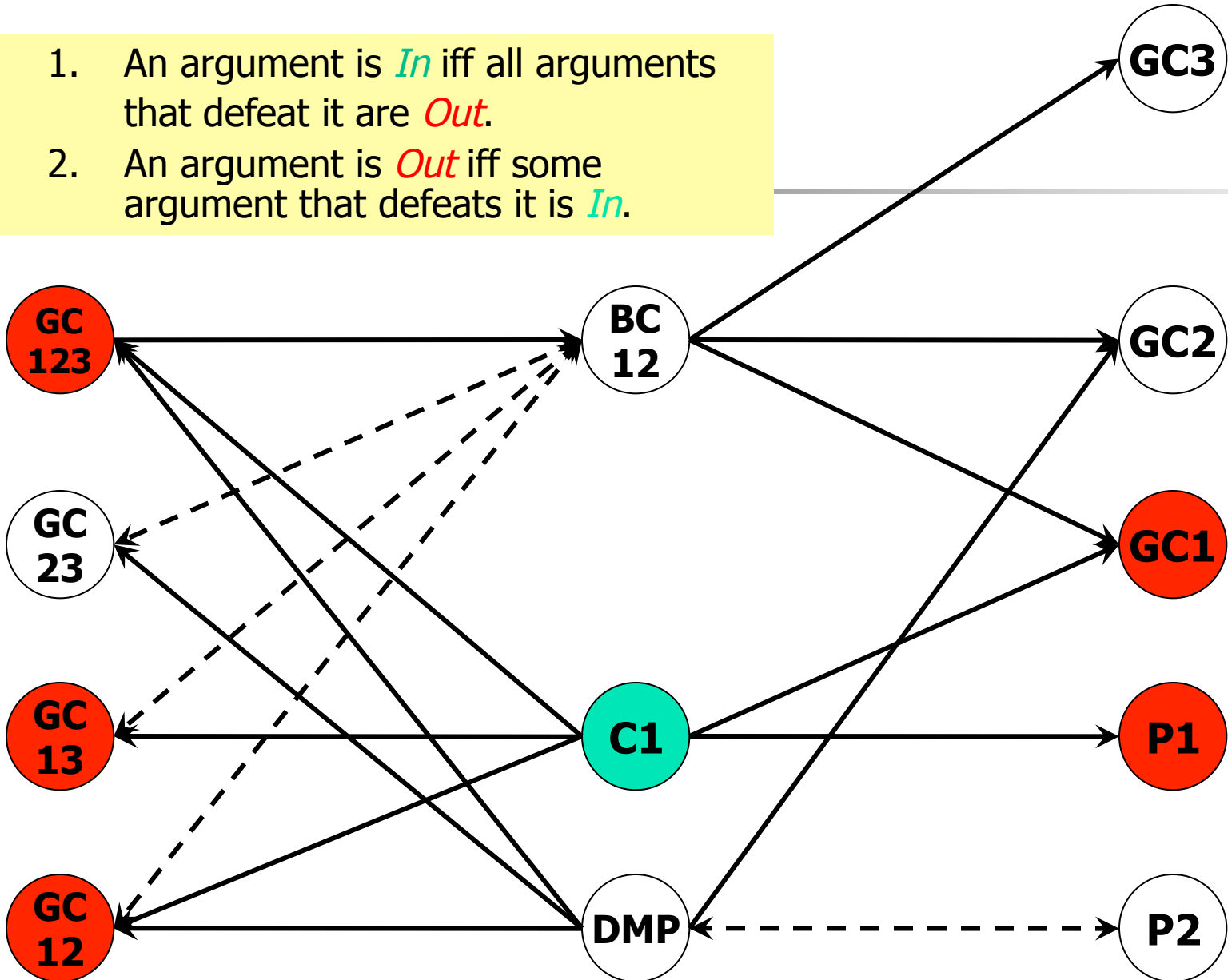
## Preferred labelling 2

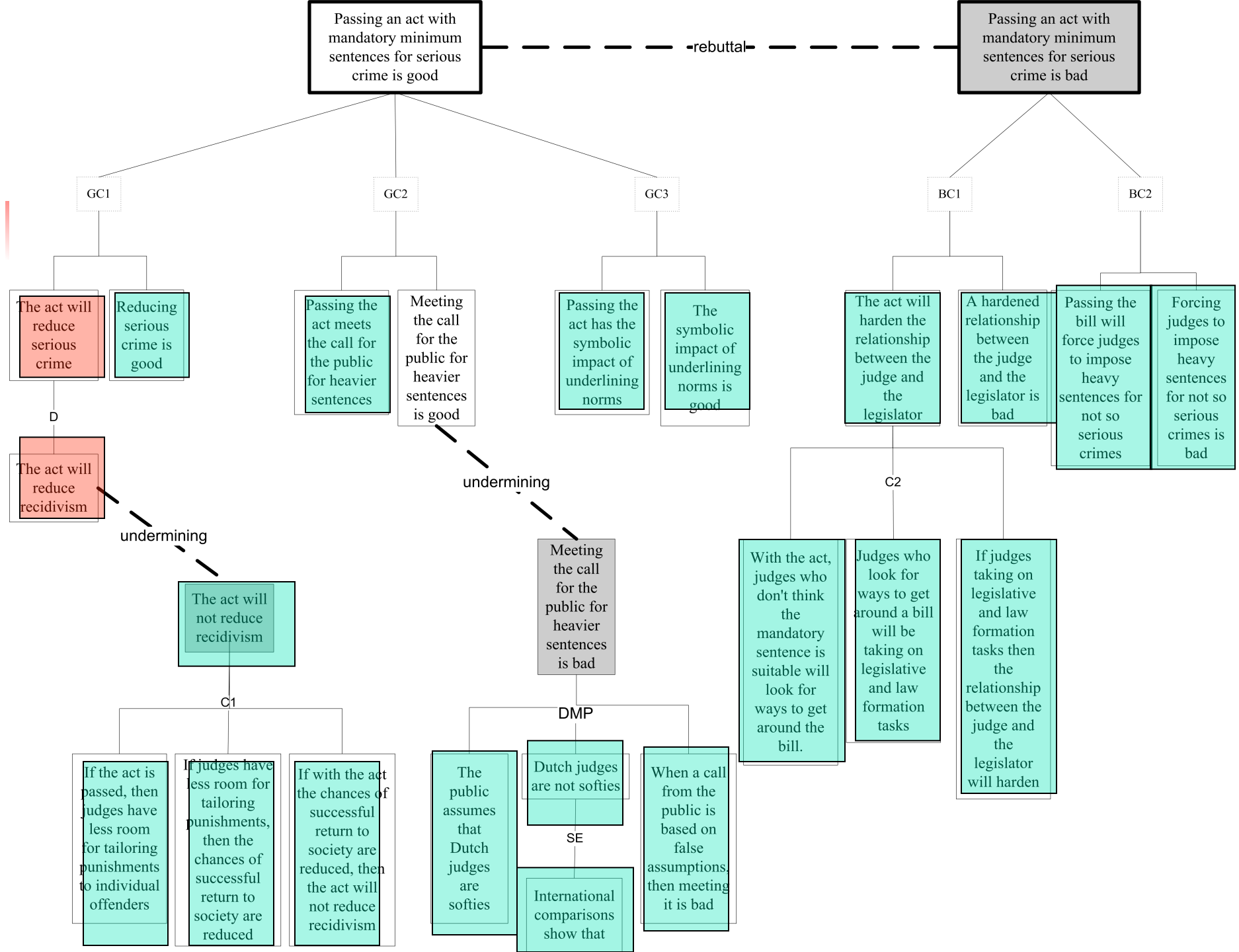
1. An argument is *In* iff all arguments that defeat it are *Out*.
2. An argument is *Out* iff some argument that defeats it is *In*.



# Grounded labelling

1. An argument is *In* iff all arguments that defeat it are *Out*.
2. An argument is *Out* iff some argument that defeats it is *In*.







# Summary

---

- A **formal metatheory** of structured argumentation is emerging
- Better understanding needed of **philosophical** underpinnings and **practical** applicability
  - Not all argumentation can be naturally reduced to plausible reasoning
  - The 'one base logic' approach is only suitable for plausible reasoning
- Important **research issues**:
  - Aggregation of arguments
  - Relation with probability theory



# Interaction

---



- **Argument games** verify status of argument (or statement) given a single theory (knowledge base)
- But **real argumentation dialogues** have
  - Distributed information
  - Dynamics
  - Real players!
  - Richer communication languages



# Example



P: Tell me all you know about recent trading in explosive materials (**request**)

P: **why** don't you want to tell me?

P: **why** aren't you allowed to tell me?

P: You may be right in general (**concede**) but in this case there is an exception **since** this is a matter of national importance

P: **since** we have heard about a possible terrorist attack

P: OK, I agree (**offer accepted**).

O: No I won't (**reject**)

O: **since** I am not allowed to tell you

O: **since** sharing such information could endanger an investigation

O: **Why** is this a matter of national importance?

O: I **concede** that there is an exception, so I **retract** that I am not allowed to tell you. I will tell you **on the condition** that you don't exchange the information with other police officers (**offer**)

# Example



P: Tell me all you know about recent trading in explosive materials (request)

P: why don't you want to tell me?

P: why aren't you allowed to tell me?

P: You may be right in general (concede) but in this case there is an exception since this is a matter of national importance

P: since we have heard about a possible terrorist attack

P: OK, I agree (offer accepted).

O: No I won't (reject)

O: since I am not allowed to tell you

O: since sharing such information could endanger an investigation

O: Why is this a matter of national importance?

O: I concede that there is an exception, so I retract that I am not allowed to tell you. I will tell you on the condition that you don't exchange the information with other police officers (offer)

# Example



P: Tell me all you know about recent trading in explosive materials (request)

P: why don't you want to tell me?

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P: since we have heard about a possible terrorist attack

P: OK, I agree (offer accepted).

O: No I won't (reject)

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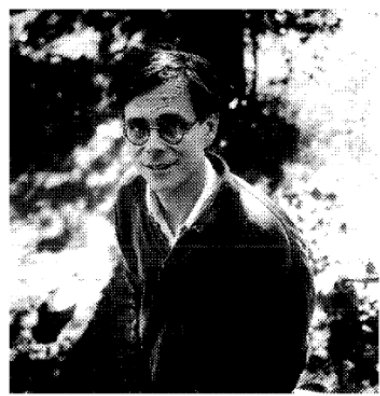
O: Why is this a matter of national importance?

O: I concede that there is an exception, so I retract that I am not allowed to tell you. I will tell you on the condition that you don't exchange the information with other police officers (offer)



# Types of dialogues (Walton & Krabbe)

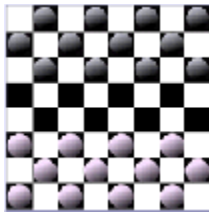
| <i>Dialogue Type</i>       | <i>Dialogue Goal</i>    | <i>Initial situation</i> |
|----------------------------|-------------------------|--------------------------|
| <i>Persuasion</i>          | resolution of conflict  | conflict of opinion      |
| <i>Negotiation</i>         | making a deal           | conflict of interest     |
| <i>Deliberation</i>        | reaching a decision     | need for action          |
| <i>Information seeking</i> | exchange of information | personal ignorance       |
| <i>Inquiry</i>             | growth of knowledge     | general ignorance        |

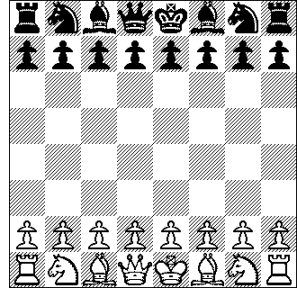


# Dialogue systems (according to Carlson 1983)

---

- Dialogue systems define the conditions under which an **utterance** is **appropriate**
- An utterance is **appropriate** if it promotes the **goal** of the **dialogue** in which it is made  
→
- Appropriateness defined not at speech act level but at dialogue level  
→
- Dialogue **game** approach
  - **Protocol** should promote the goal of the dialogue





# Dialogue game systems

- A communication language
  - Well-formed utterances
- Rules for when an utterance is allowed
  - Protocol
- Effect rules
- Turntaking rules
- Termination + outcome rules

Agent design:  
strategies for selecting from the allowed utterances



# Effect rules

---

- Specify **commitments**
  - “Claim  $p$ ” and “Concede  $p$ ” commits to  $p$
  - “ $p$  since  $Q$ ” commits to  $p$  and  $Q$
  - “Retract  $p$ ” ends commitment to  $p$
  - ...
- Commitments used for:
  - Determining outcome
  - Enforcing ‘dialogical consistency’
  - ...



# Public semantics for dialogue protocols

---

- **Public semantics:** can protocol compliance be externally observed?
- Commitments are a participant's **publicly declared** standpoints, so not the same as beliefs!
- Only commitments and dialogical behaviour should count for move legality:
  - "Claim  $p$  is allowed only if you believe  $p$ "  
vs.
  - "Claim  $p$  is allowed only if you are not committed to  $\neg p$  and have not challenged  $p$ "





# More and less strict protocols

---

- **Single-multi move**: one or more moves per turn allowed
- **Single-multi-reply**: one or more replies to the same move allowed
- **Deterministic**: no choice from legal moves
- **Deterministic in communication language**: no choice from speech act types
- Only reply to moves from previous turn?



# Some properties that can be studied

---

- Correspondence with players' **beliefs**
  - If union of beliefs implies  $p$ , can/will agreement on  $p$  result?
  - If players agree on  $p$ , does union of beliefs imply  $p$ ?
  - **Disregarding** vs. **assuming** player strategies



# Example 1

---

Knowledge bases

Paul:  $r$

Olga:  $s$

Inference rules

$p \Rightarrow q$

$r \Rightarrow p$

$s \Rightarrow \neg r$

P1:  $q$  since  $p$

Paul  $\cup$  Olga does not justify  $q$   
but they could agree on  $q$

Olga is **credulous**: she **concedes** everything for which she cannot construct a (defensible or justified) counterargument

# Example 1

Knowledge bases

Paul:  $r$

Olga:  $s$

Inference rules

$p \Rightarrow q$

$r \Rightarrow p$

$s \Rightarrow \neg r$

P1:  $q$  since  $p$

O1: concede  $p, q$

Paul  $\cup$  Olga does not justify  $q$   
but they could agree on  $q$



# Example 1

---

Knowledge bases

Paul:  $r$

Olga:  $s$

Inference rules

$p \Rightarrow q$

$r \Rightarrow p$

$s \Rightarrow \neg r$

P1:  $q$  since  $p$

Paul  $\cup$  Olga does not justify  $q$   
but they could agree on  $q$

Olga is **sceptical**: she **challenges**  
everything for which she cannot  
construct a (defensible or  
justified) argument

# Example 1

Knowledge bases

Paul:  $r$

Olga:  $s$

Inference rules

$p \Rightarrow q$

$r \Rightarrow p$

$s \Rightarrow \neg r$

P1:  $q$  since  $p$

O1: why  $p$ ?

Paul  $\cup$  Olga does not justify  $q$   
but they could agree on  $q$

# Example 1

Knowledge bases

Paul:  $r$

Olga:  $s$

Inference rules

$p \Rightarrow q$

$r \Rightarrow p$

$s \Rightarrow \neg r$

P1:  $q$  since  $p$

O1: why  $p$ ?

P2:  $p$  since  $r$

Paul  $\cup$  Olga does not justify  $q$   
but they could agree on  $q$

# Example 1

Knowledge bases

Paul: r

Olga: s

Inference rules

$p \Rightarrow q$

$r \Rightarrow p$

$s \Rightarrow \neg r$

Paul  $\cup$  Olga does not justify q  
but they could agree on q

P1: q since p

O1: why p?

P2: p since r

O2:  $\neg r$  since s





# Example 2

---

Knowledge bases

Paul:

$p$

$q$

Olga:

$p$

$q \supset \neg p$

Inference rules

Modus ponens

...

P1: claim  $p$

Paul  $\cup$  Olga does not justify  $p$  but they will agree on  $p$  if players are **conservative**, that is, if they stick to their beliefs if possible

# Example 2

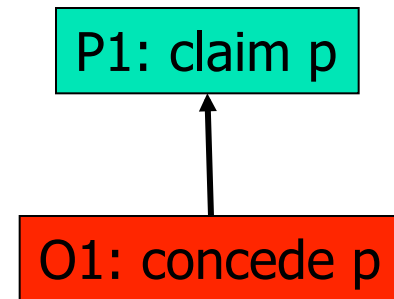
Knowledge bases

Paul:  
p  
q

Olga:  
p  
 $q \supset \neg p$

Inference rules

Modus ponens  
...



Paul  $\cup$  Olga does not justify p but they will agree on p if players are **conservative**, that is, if they stick to their beliefs if possible



# Example 2

---

Knowledge bases

Paul:

$p$

$q$

Olga:

$p$

$q \supset \neg p$

Inference rules

Modus ponens

...

P1: claim  $p$

O1: what about  $q$ ?

Possible solution (for **open-minded** agents, who are prepared to critically test their beliefs):

# Example 2

Knowledge bases

Paul:

$p$

$q$

Olga:

$p$

$q \supset \neg p$

Inference rules

Modus ponens

...

P1: claim  $p$

O1: what about  $q$ ?

P2: claim  $q$

Possible solution (for **open-minded** agents, who are prepared to critically test their beliefs):

# Example 2

Knowledge bases

Inference rules

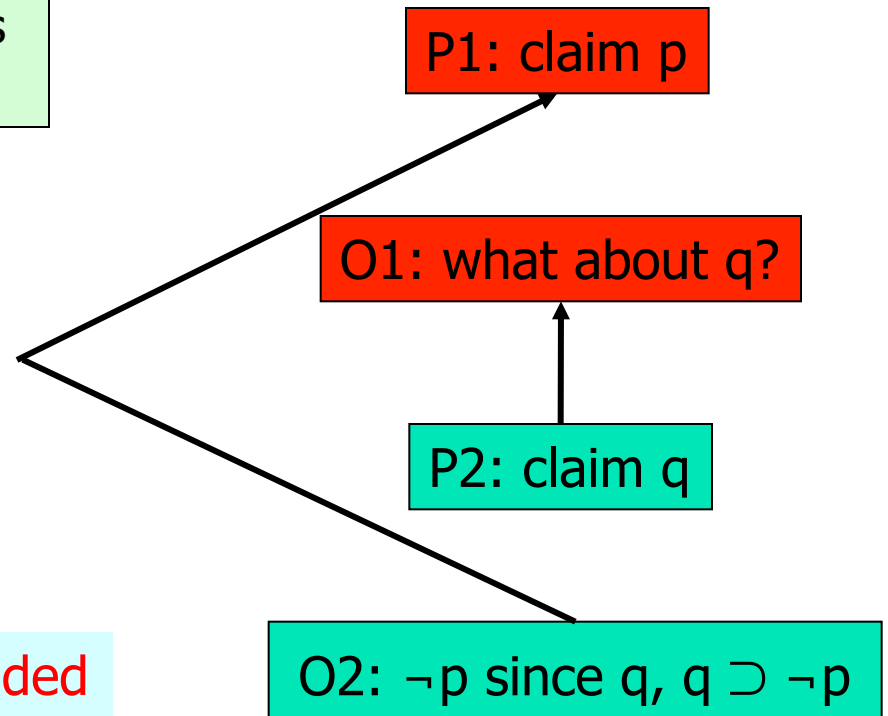
Paul:  
p  
q

Modus ponens  
...

Olga:  
p  
 $q \supset \neg p$

Problem: how to ensure relevance?

Possible solution (for **open-minded** agents, who are prepared to critically test their beliefs):



# Automated Support of Regulated Data Exchange. A Multi-Agent Systems Approach



PhD Thesis Pieter Dijkstra (2012)

Faculty of Law

University of Groningen



rijksuniversiteit  
 groningen



# The communication language

| <b>Speech act</b>       | <b><i>Attack</i></b>   | <b><i>Surrender</i></b>   |
|-------------------------|--|---|
| request( $\varphi$ )    | offer ( $\varphi'$ ), reject( $\varphi$ )                                    | -   |
| offer( $\varphi$ )      | offer( $\varphi'$ ) ( $\varphi \neq \varphi'$ ), reject( $\varphi$ )         | accept( $\varphi$ )   |
| reject( $\varphi$ )     | offer( $\varphi'$ ) ( $\varphi \neq \varphi'$ ),<br>why-reject ( $\varphi$ ) | -   |
| accept( $\varphi$ )     | -  | -   |
| why-reject( $\varphi$ ) | claim ( $\varphi'$ )   | -   |
| claim( $\varphi$ )      | why( $\varphi$ )   | concede( $\varphi$ )  |
| why( $\varphi$ )        | $\varphi$ since S (an argument)  | retract( $\varphi$ )  |
| $\varphi$ since S       | why( $\varphi$ ) ( $\varphi \in S$ )<br>$\varphi'$ since S' (a defeater)     | concede( $\varphi$ )<br>concede $\varphi'$ ( $\varphi' \in S$ ) |
| concede( $\varphi$ )    | -  | -   |
| retract( $\varphi$ )    | -  | -   |
| deny( $\varphi$ )       | -  | -   |

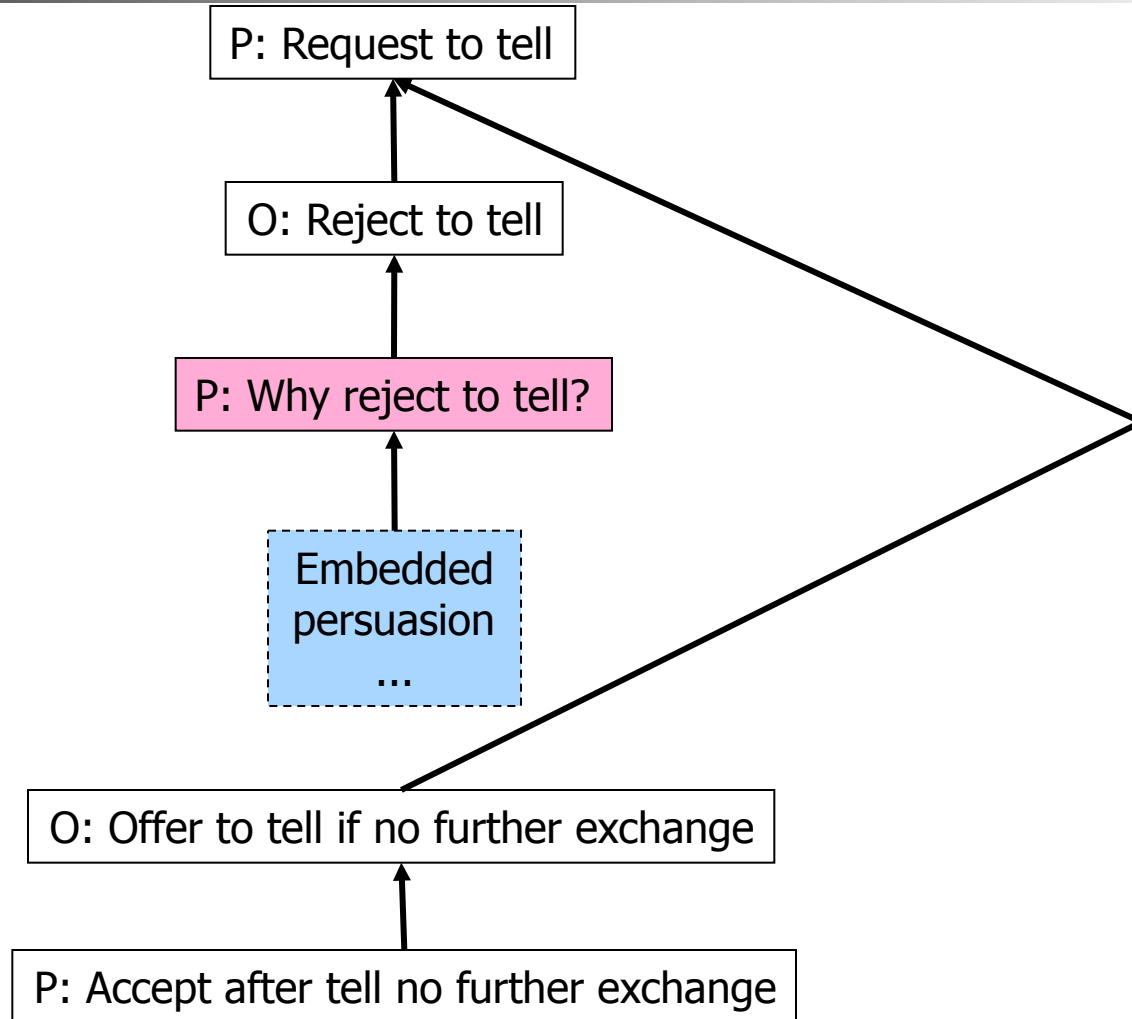


# The protocol

- Start with a request
- Reply to an earlier move of the other agent
- Pick your replies from the table
- Finish persuasion before resuming negotiation
- **Turntaking:**
  - In nego: after each move
  - In pers: various rules possible
- **Termination:**
  - In nego: if offer is accepted or someone withdraws
  - In pers: if main claim is retracted or conceded



# Example dialogue formalised





# Persuasion part formalised

O: ***Claim*** Not allowed to tell

---

# Persuasion part formalised

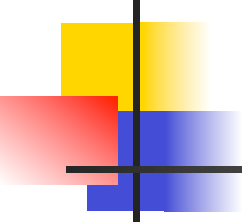


---

O: **Claim** Not allowed to tell

P: **Why** not allowed to tell?

# Persuasion part formalised



O: **Claim** Not allowed to tell

P: **Why** not allowed to tell?

O: Not allowed to tell **since** telling endangers investigation &  
What endangers an investigation is not allowed

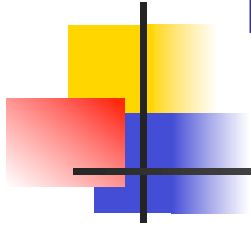
# Persuasion part formalised

O: **Claim** Not allowed to tell

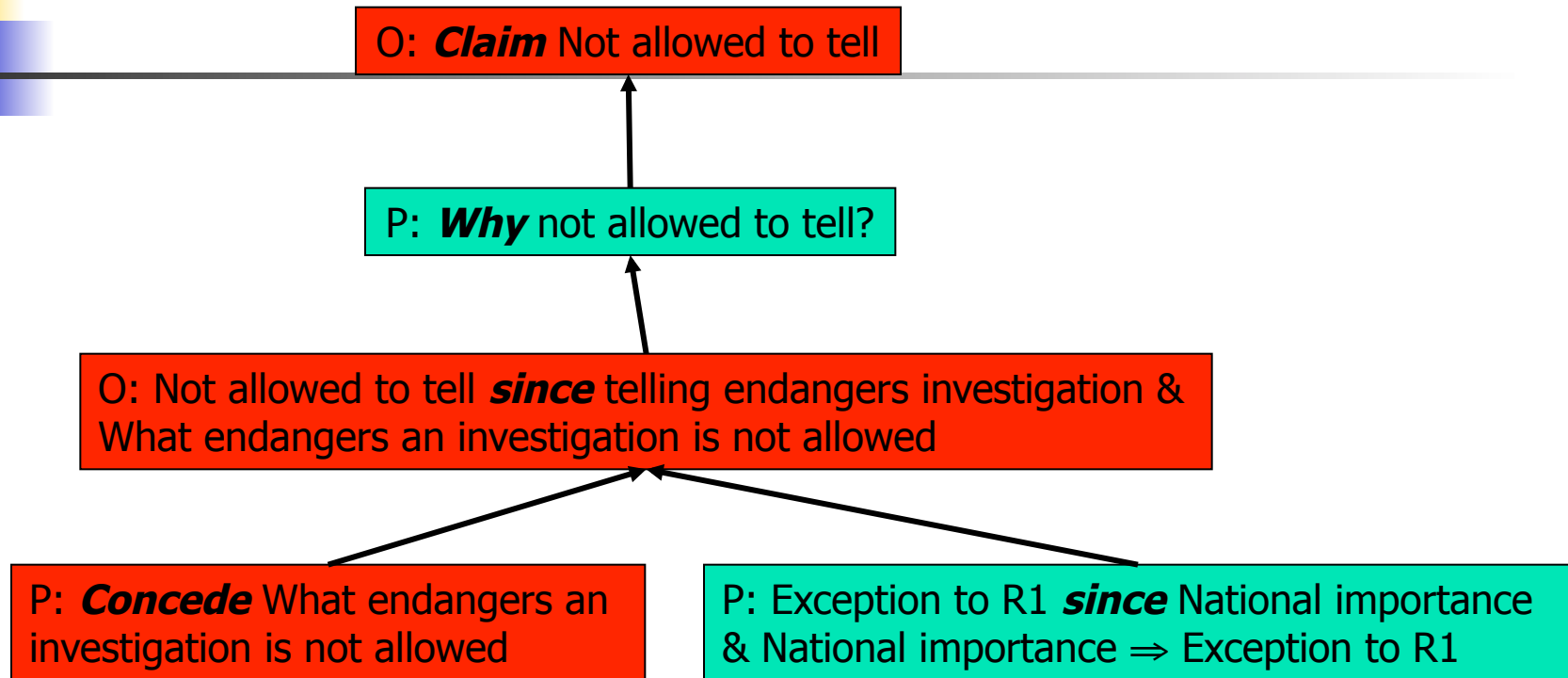
P: **Why** not allowed to tell?

O: Not allowed to tell **since** telling endangers investigation &  
What endangers an investigation is not allowed

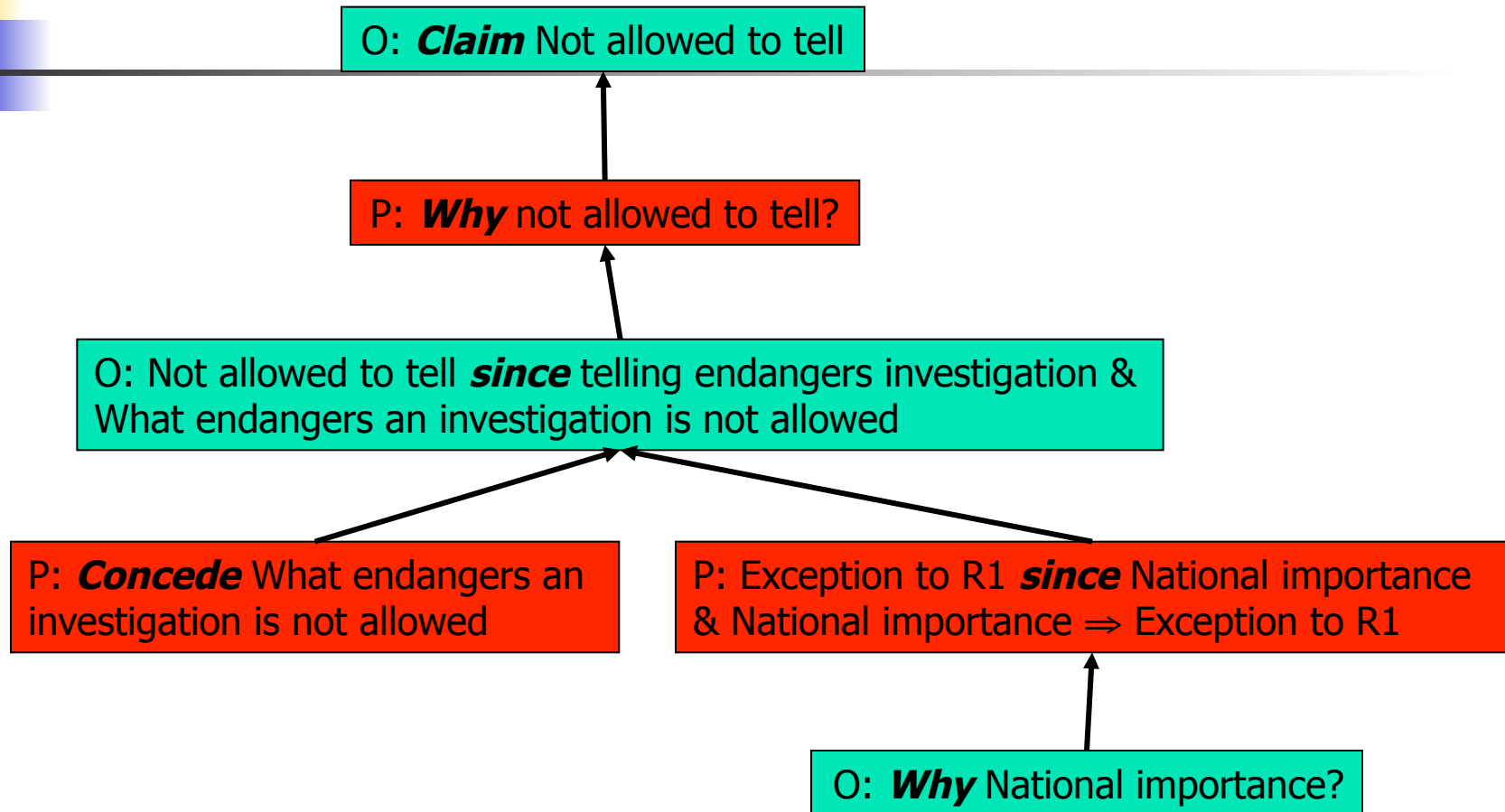
P: **Concede** What endangers an investigation is not allowed



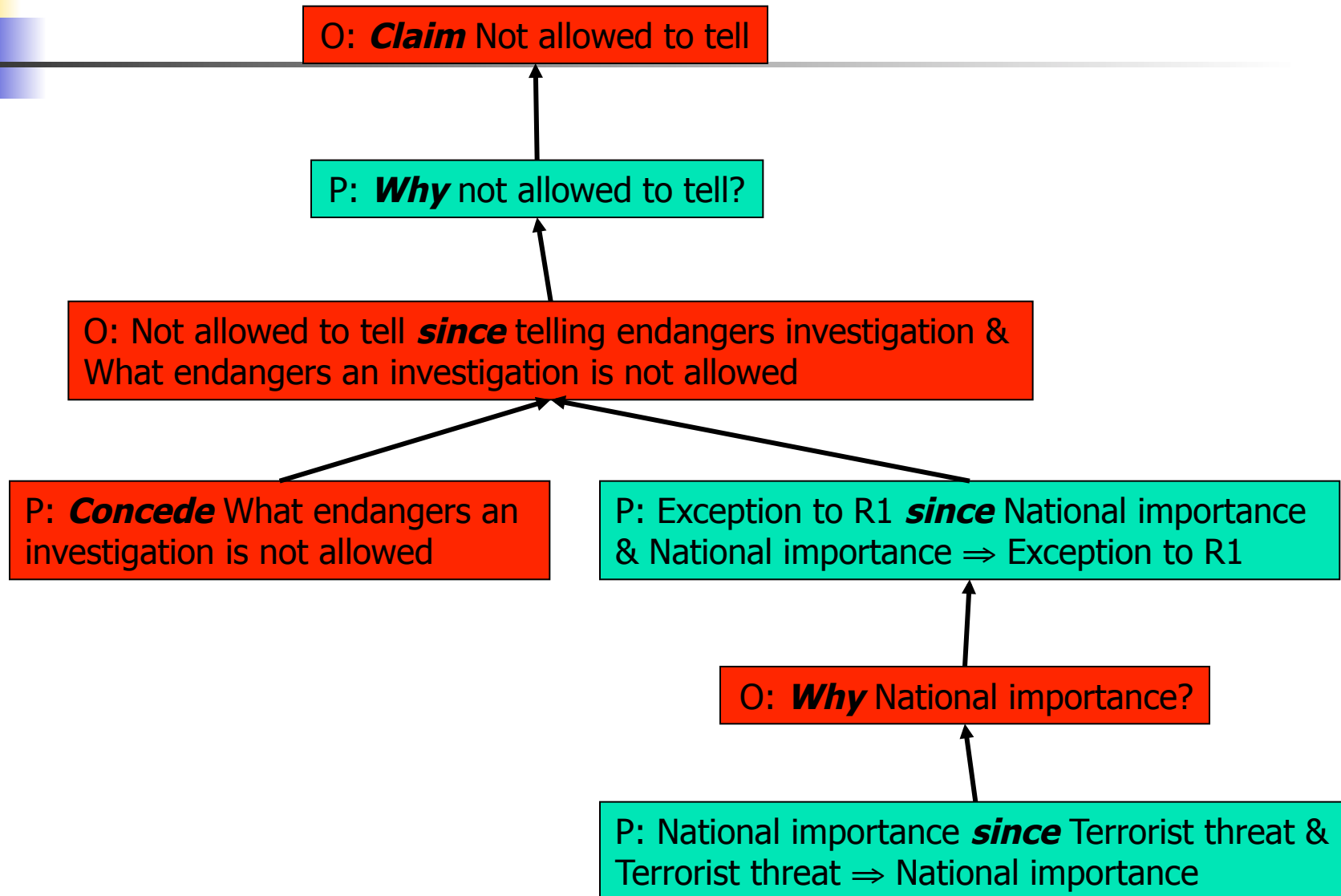
# Persuasion part formalised



# Persuasion part formalised

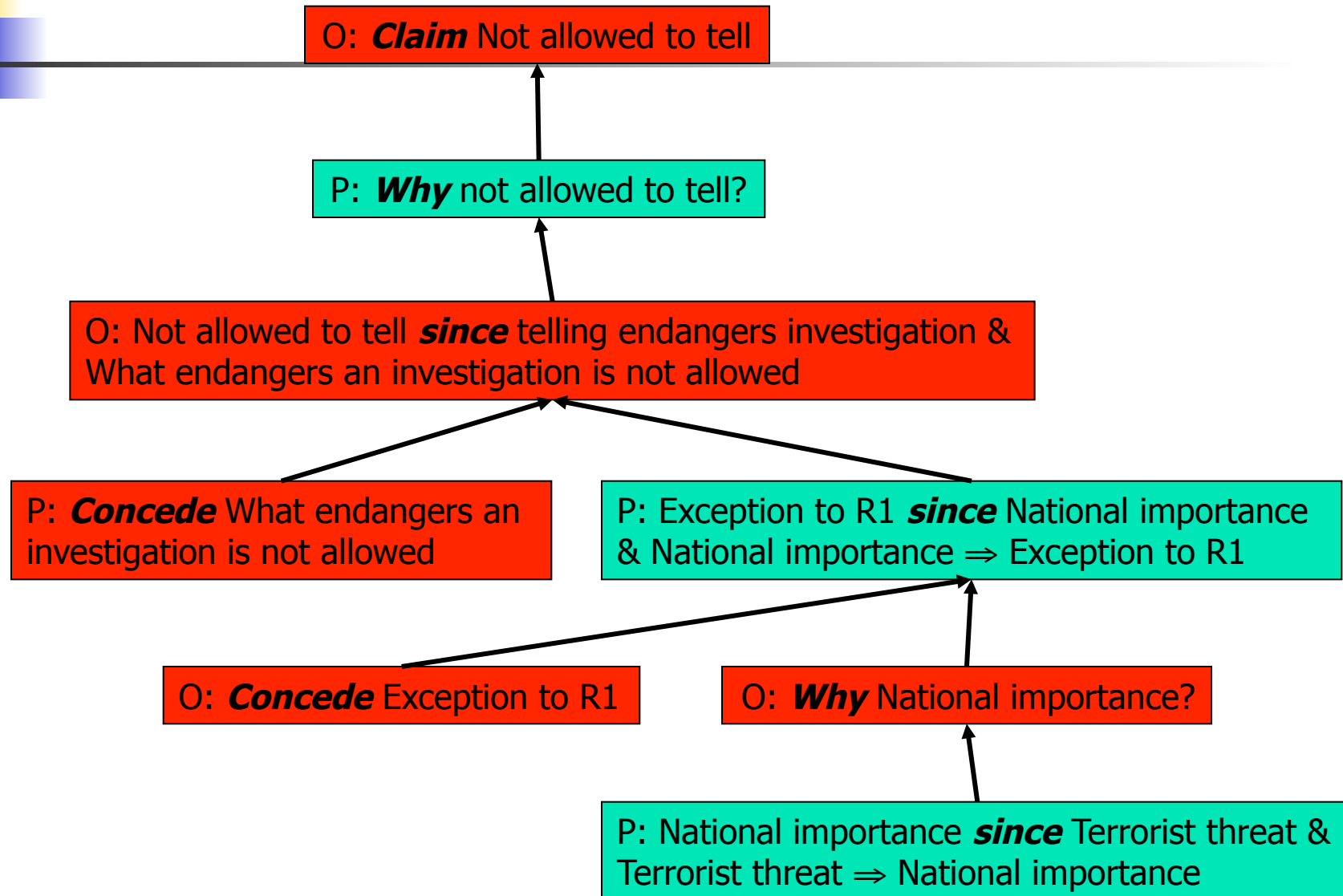


# Persuasion part formalised

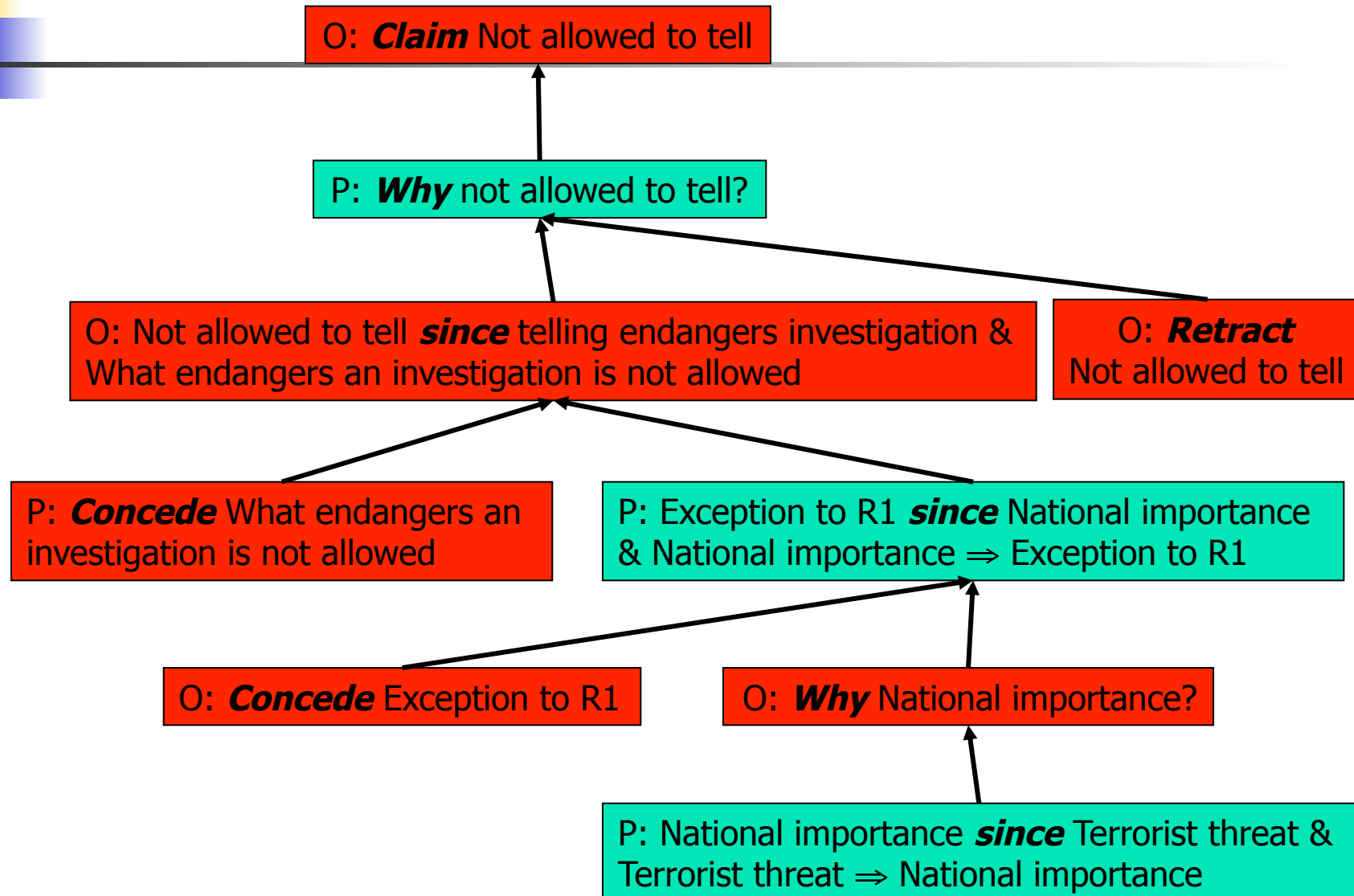




# Persuasion part formalised



# Persuasion part formalised





# Conclusion

---

- Argumentation has two sides:
  - **Inference**
    - semantics
    - strict vs defeasible inferences
    - preferences
  - **Dialogue**
    - language + protocol
    - agent design
- Both sides can be formally and computationally modelled
  - But not in the same way
  - Metatheory of inference much more advanced than of dialogue



# Reading (1)

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- **Collections**

- T.J.M. Bench-Capon & P.E. Dunne (eds.), *Artificial Intelligence* 171 (2007), Special issue on Argumentation in Artificial Intelligence
- I. Rahwan & G.R. Simari (eds.), *Argumentation in Artificial Intelligence*. Berlin: Springer 2009.
- A. Hunter (ed.), *Argument and Computation* 5 (2014), special issue on Tutorials on Structured Argumentation

- **Abstract argumentation**

- P.M. Dung, On the acceptability of arguments and its fundamental role in nonmonotonic reasoning, logic programming and n-person games. *Artificial Intelligence* 77 (1995): 321-357
- P. Baroni, M.W.A. Caminada & M. Giacomin. An introduction to argumentation semantics. *The Knowledge Engineering Review* 26: 365-410 (2011)



# Reading (2)

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- **Classical and Tarskian argumentation**
  - Ph. Besnard & A. Hunter, *Elements of Argumentation*. Cambridge, MA: MIT Press, 2008.
  - N Gorgiannis & A Hunter (2011) Instantiating abstract argumentation with classical logic arguments: postulates and properties, *Artificial Intelligence* 175: 1479-1497.
  - L. Amgoud & Ph. Besnard, Logical limits of abstract argumentation frameworks. *Journal of Applied Non-Classical Logics* 23(2013): 229-267.
- **ASPIC+**
  - H. Prakken, An abstract framework for argumentation with structured arguments. *Argument and Computation* 1 (2010): 93-124.
  - S. Modgil & H. Prakken, A general account of argumentation with preferences. *Artificial Intelligence* 195 (2013): 361-397



# Reading (3)

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- **Assumption-based argumentation**

- A. Bondarenko, P.M. Dung, R.A. Kowalski & F. Toni, An abstract, argumentation-theoretic approach to default reasoning, *Artificial Intelligence* 93 (1997): 63-101.
- P.M. Dung, P. Mancarella & F. Toni, Computing ideal sceptical argumentation, *Artificial Intelligence* 171 (2007): 642-674.

- **Dialogue**

- S. Parsons, M. Wooldridge & L. Amgoud, Properties and complexity of some formal inter-agent dialogues. *Journal of Logic and Computation* 13 (2003): 347-376.
- H. Prakken, Coherence and flexibility in dialogue games for argumentation. *Journal of Logic and Computation* 15 (2005): 1009-1040.
- H. Prakken, Formal systems for persuasion dialogue. *The Knowledge Engineering Review* 21 (2006): 163-188.